

Ratios of W and Z cross sections at large boson p_T
(as a constraint on PDFs and background to new physics)

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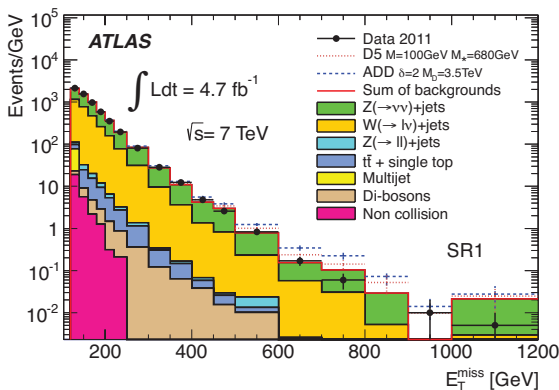
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PDF4LHC Meeting
CERN, Geneva, 17th April 2013

In collaboration with Sarah Alam Malik, [arXiv:1304.2424](#).

$Z(\rightarrow \nu\bar{\nu}) + \text{jets}$ background to new physics

- Many searches for new physics (SUSY, LEDs, WIMPs, ...) involve looking for missing transverse energy with jets.
- Major irreducible SM background is $Z(\rightarrow \nu\bar{\nu}) + \text{jets}$.



[ATLAS, arXiv:1210.4491]

Data-driven methods to estimate $Z(\rightarrow \nu\bar{\nu})+\text{jets}$

Idea: Measure process X with similar kinematic properties, then correct by ratio of $Z(\rightarrow \nu\bar{\nu})+\text{jets}$ to X taken from theory.

- ① $Z(\rightarrow \ell\bar{\ell})+\text{jets}$. Only need to multiply by $(Z \rightarrow \nu\bar{\nu})/(Z \rightarrow \ell\bar{\ell})$ ratio of branching fractions, but large statistical uncertainty.
- ② $\gamma+\text{jets}$. More statistics, but Z/γ ratio has larger theoretical uncertainties. Studied by Z. Bern *et al.* [[arXiv:1106.1423](#), [arXiv:1206.6064](#)] ($\Rightarrow < 10\%$ QCD and $< 15\%$ EW uncertainties). Also study of Z/γ ratio by S. Ask *et al.* [[arXiv:1107.2803](#)].
- ③ $W(\rightarrow \ell\nu)+\text{jets}$. More statistics than $Z(\rightarrow \ell\bar{\ell})+\text{jets}$, but $t\bar{t}$ background. Smaller theoretical uncertainties on Z/W ratio.

All three methods have relative advantages and disadvantages.

$\Rightarrow$ Best to use all three methods to cross-check each other.

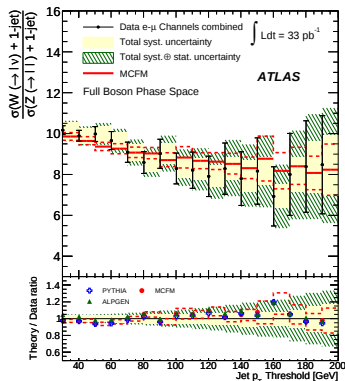
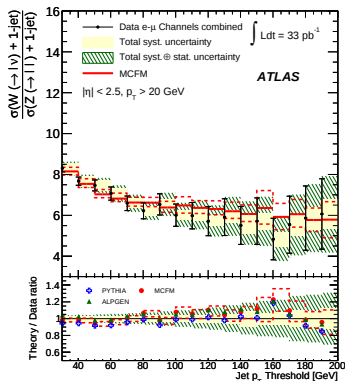
Uncertainties on background estimates [ATLAS, arXiv:1210.4491]

Relative systematic uncertainties for all signal regions (in percent):

Source	SR1	SR2	SR3	SR4
JES/JER/ E_T^{miss}	1.0	2.6	4.9	5.8
MC Z/W modelling	2.9	2.9	2.9	3.0
MC statistical uncertainty	0.5	1.4	3.4	8.9
$1 - f_{\text{EW}}$	1.0	1.0	0.7	0.7
Muon scale and resolution	0.03	0.02	0.08	0.61
Lepton scale factors	0.4	0.5	0.6	0.7
Multijet BG in electron CR	0.1	0.1	0.3	0.6
Di-boson, top, multijet, non-collisions	0.8	0.7	1.1	0.3
Total systematic uncertainty	3.4	4.4	6.8	11.1
Total data statistical uncertainty	0.5	1.7	4.3	11.8

- “MC Z/W modelling” from comparing ALPGEN and SHERPA.

Ratio of W +1-jet to Z +1-jet [ATLAS, arXiv:1108.4908]



- Dedicated ratio measurement validates theory predictions.
- SUSY searches typically use event variables such as H_T , a vector sum of the jets above a certain p_T threshold [CMS, arXiv:1106.4503], numerically close to boson p_T for V +jets.

Goals of our study [S. Malik, G.W., arXiv:1304.2424]

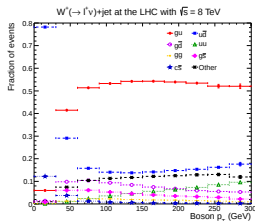
- Examine the behaviour of various cross-section ratios (W^+/W^- , W^+/Z , W^-/Z and $W^\pm/Z$) versus boson p_T .
- Study the theoretical uncertainties on these ratios at large values of the boson p_T in more detail than previously.
- Motivate a dedicated measurement to validate theoretical predictions (and possibly help to reduce uncertainties).
- Investigate if we can learn anything new about PDFs from these ratios measured as a function of the boson p_T .

Codes used for $W^+(\rightarrow \ell^+\nu)$, $W^-(\rightarrow \ell^-\bar{\nu})$ and $Z^0(\rightarrow \ell^+\ell^-)$

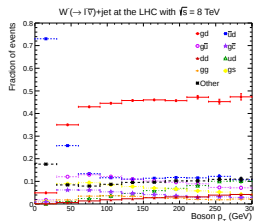
$p_T^{\text{jet}} > 10 \text{ GeV}$, $|\eta^{\text{jet}}| < 5$, anti- k_T jets with $R = 0.5$, no lepton cuts.

- MADGRAPH at LO with $N = \{0, 1, 2, 3, 4\}$ jets matched to PYTHIA (using the MLM prescription) and CTEQ6L1 PDFs.
- MCFM for the V +jet process with MSTW08 NLO PDFs.

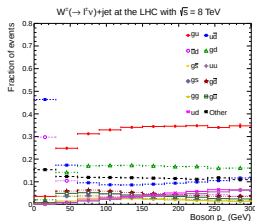
Flavour decomposition using MADGRAPH+PYTHIA



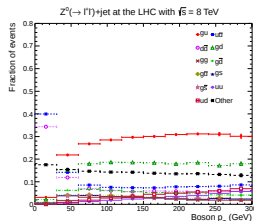
$$W^+ \Rightarrow gu$$



$$W^- \Rightarrow gd$$

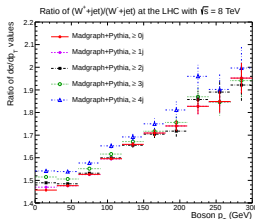


$$W^\pm \Rightarrow gu, gd$$

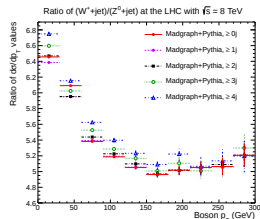


$$Z^0 \Rightarrow gu, gd$$

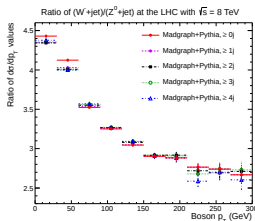
Dependence of cross-section ratios on jet multiplicity



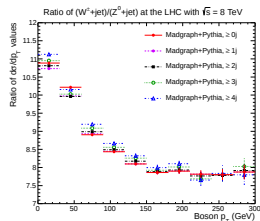
$$W^{+}/W^{-}$$



$$W^{+}/Z^0$$

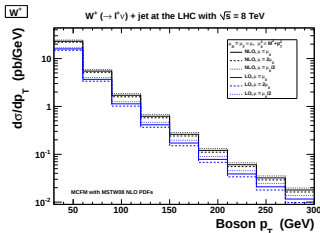
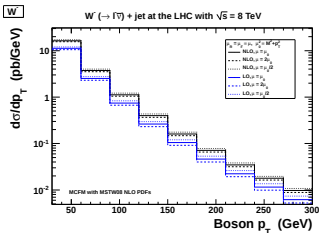
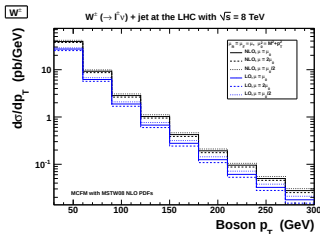
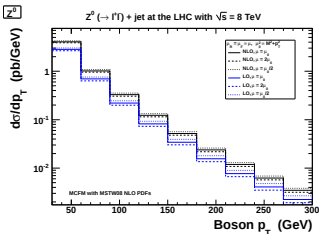


$$W^{-}/Z^0$$

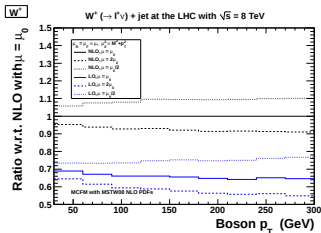
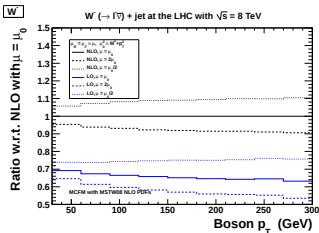
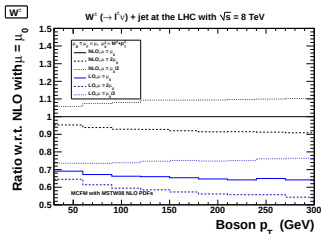
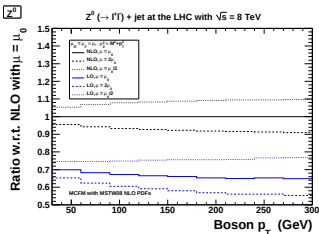


$$W^{\pm}/Z^0$$

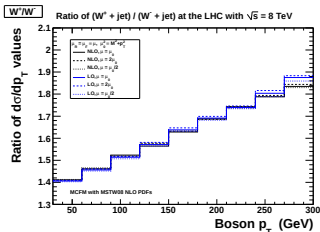
Differential cross sections, $d\sigma/dp_T$, for the V +jet process

 W^+  W^-  $W^{\pm}$  Z^0

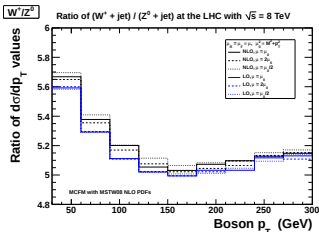
$d\sigma/dp_T$, normalised to the central NLO prediction

W⁺W⁻W[±]Z⁰

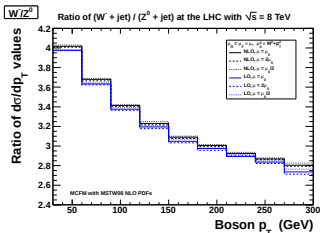
Ratios of boson p_T distributions for the V +jet process



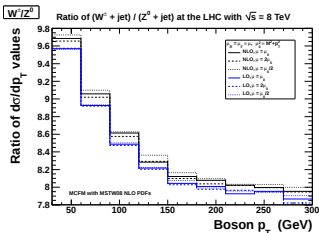
$$W^+ / W^-$$



$$W^+ / Z^0$$

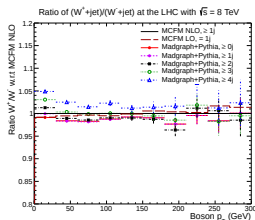


$$W^- / Z^0$$

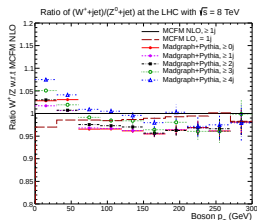


$$W^\pm / Z^0$$

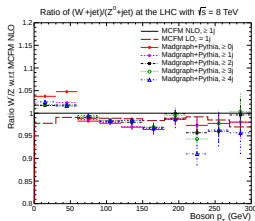
Compare MCFM (CTEQ6L1) and MADGRAPH+PYTHIA



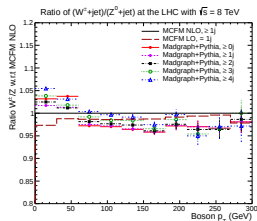
$$W^+ / W^-$$



$$W^+ / Z^0$$

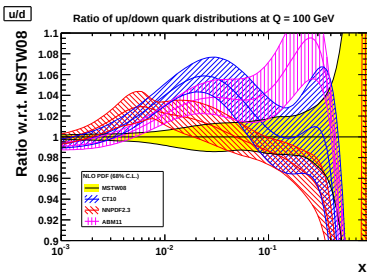
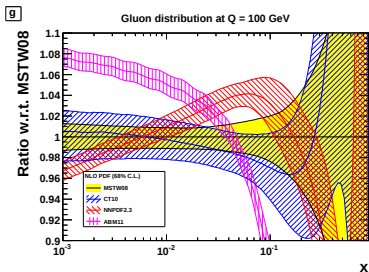


$$W^- / Z^0$$



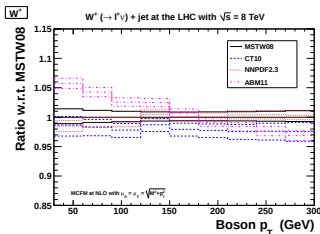
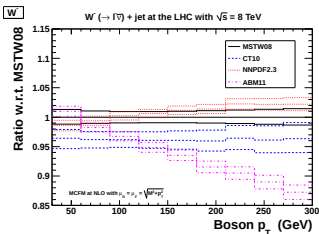
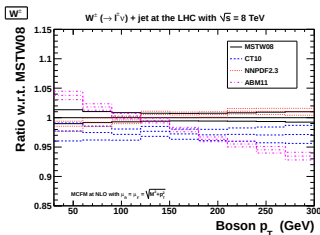
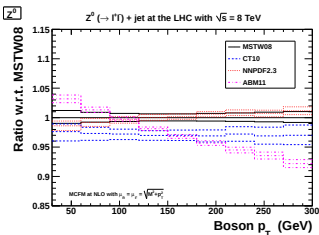
$$W^\pm / Z^0$$

Gluon distribution and u/d ratio versus x

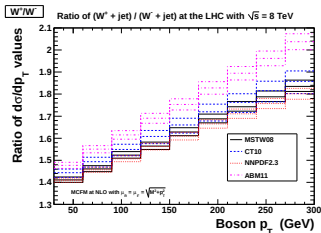


- Consider four NLO PDF sets (**MSTW08**, **CT10**, **NNPDF2.3**, **ABM11**) with $\alpha_S(M_Z^2) = \{0.1202, 0.1180, 0.1190, 0.1180\}$.
- Envelope of predictions using **MSTW08**, **CT10** and **NNPDF2.3** includes implicit $\alpha_S(M_Z^2) \approx 0.119 \pm 0.001$ uncertainty.
- x dependence of gluon $\Rightarrow p_T$ dependence of $d\sigma/dp_T$.
- x dependence of u/d ratio $\Rightarrow p_T$ dependence of W^+/W^- ratio.

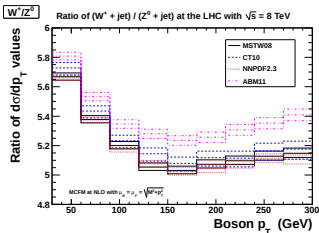
PDF dependence of differential cross sections, $d\sigma/dp_T$


 W^+

 W^-

 $W^\pm$

 Z^0

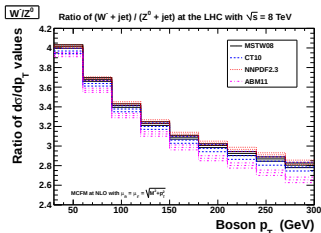
PDF dependence of ratios of boson p_T distributions



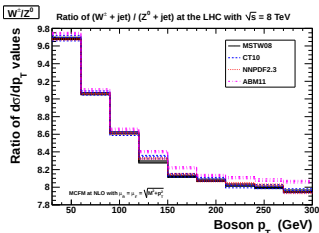
$$W^+/W^-$$



$$W^+/Z^0$$

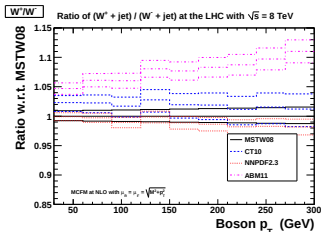


$$W^-/Z^0$$

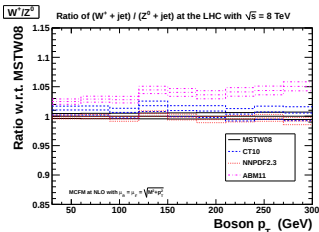


$$W^\pm/Z^0$$

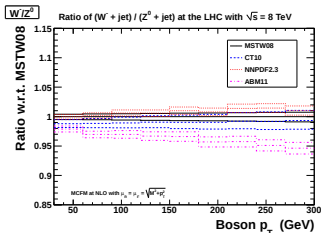
PDF dependence of ratios relative to MSTW08



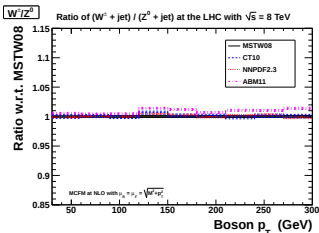
$$W^+ / W^-$$



$$W^+ / Z^0$$

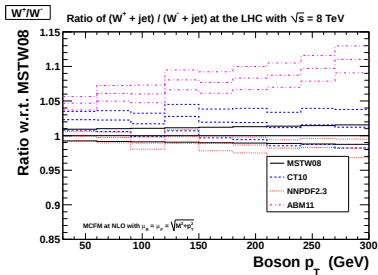


$$W^- / Z^0$$



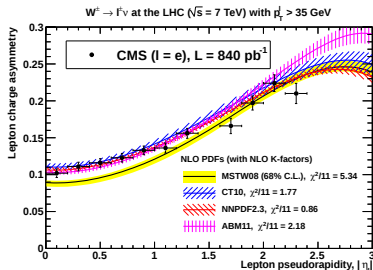
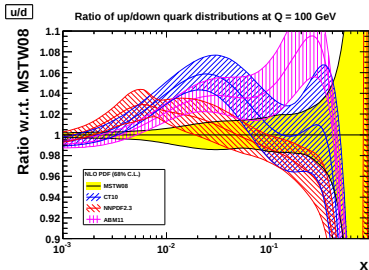
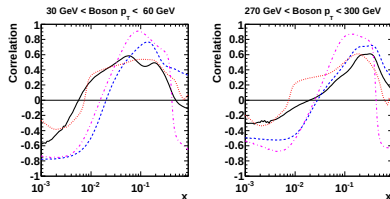
$$W^\pm / Z^0$$

Potential PDF constraints from W^+/W^- versus p_T^W



Correlation between ratio of u/d PDFs at $Q = 100$ GeV and Ratio of $(W^+ + \text{jet}) / (W^- + \text{jet})$ at the LHC with $\sqrt{s} = 8$ TeV using MCFM at NLO with $\mu_r = \mu_f = \sqrt{M^2 + p_T^2}$

Legend: MSTW08, CT10, NNPDF2.3, ABM11

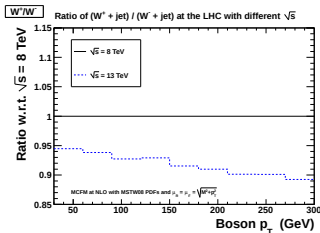


- Measurements versus p_T^W and versus $|\eta_\ell|$ are complementary.

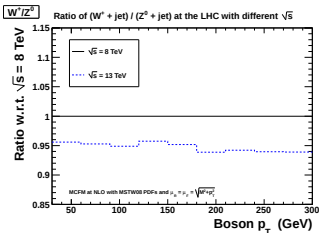
Higher-order electroweak corrections

- Effect of large virtual electroweak Sudakov logarithms of $\hat{s}/M_V^2$ can reach up to a few tens of percent for $d\sigma/dp_T$ at very large boson p_T [Denner *et al.*, arXiv:0906.1656, arXiv:1103.0914].
- Effect cancels in W^+/W^- ratio [Kühn *et al.*, arXiv:0708.0476].
- Decrease in W^+/Z and W^-/Z (and hence $W^\pm/Z$) ratios by 4% at boson $p_T = 1$ TeV and by 7% at $p_T = 2$ TeV at the 14 TeV LHC [Kühn *et al.*, arXiv:0708.0476].
- Smaller electroweak corrections than γ/Z ratio, which increases by 13% at boson $p_T = 1$ TeV and by 22% at $p_T = 2$ TeV at the 14 TeV LHC [Kühn *et al.*, hep-ph/0508253].
- Potential partial cancellation from real emission of soft W and Z bosons for sufficiently inclusive measurements [Baur, hep-ph/0611241; Stirling, Vryonidou, arXiv:1212.6537], but small effect expected for typical experimental cuts.

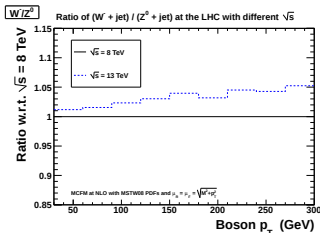
Double ratios at different $\sqrt{s}$ [see Mangano, Rojo, arXiv:1206.3557]



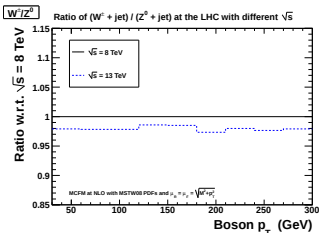
$$W^+ / W^-$$



$$W^+ / Z^0$$



$$W^- / Z^0$$



$$W^\pm / Z^0$$

Summary [S. Malik, G.W., arXiv:1304.2424]

- Theoretical $(W^\pm + \text{jets})/(Z + \text{jets})$ ratio is a key ingredient in data-driven estimates of the $Z(\rightarrow \nu\bar{\nu}) + \text{jets}$ background.
- Presented detailed study of theoretical uncertainties on W^+/W^- , W^+/Z , W^-/Z and $W^\pm/Z$ ratios versus boson p_T .
- Theoretical QCD and EW uncertainties on $W^\pm/Z$ ratio both smaller than for γ/Z ratio: estimate QCD uncertainties to be **less than 5%**. Useful to check using NLO calculations for higher jet multiplicities, preferably with matching to a parton shower.
- $d\sigma/dp_T$ can potentially constrain **gluon**, but large higher-order QCD uncertainties (**need NNLO**) and electroweak corrections.
- W^+/W^- ratio measured as a function of p_T^W has negligible uncertainties from higher-order QCD and EW, and hence can constrain **u/d** ratio in a complementary region of x to the $W(\rightarrow \ell\nu)$ charge asymmetry measured as a function of η_ℓ .