



Perspectives on the Flavor Problem

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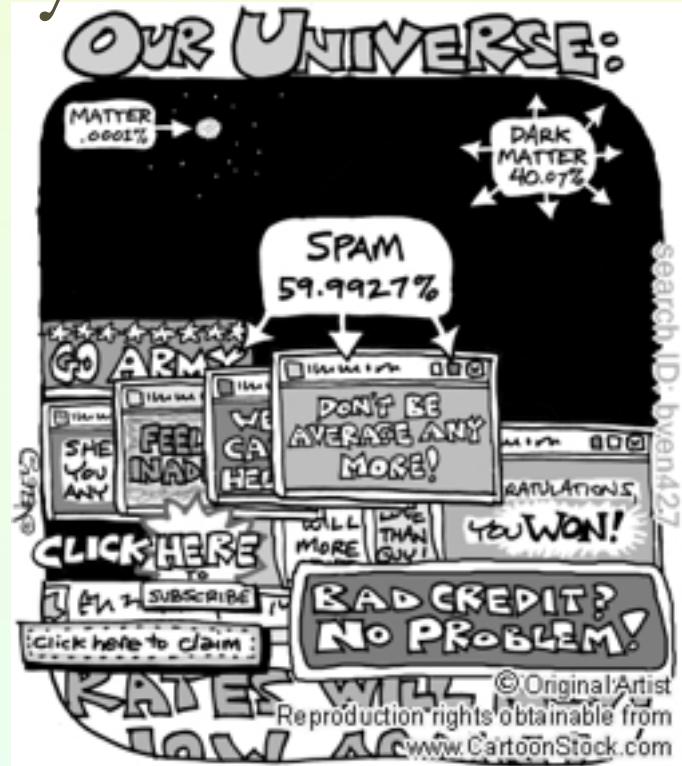
INVISIBLES
Lumley Castle, County Durham UK
2013

Flavor/CP and New Physics

- Outstanding problems in Particle Physics:
 - Dark Energy
 - Dark Matter
 - Hierarchy
 - Baryogenesis

Nature of first three may well be solely gravitational
Baryogenesis requires CPV beyond that in the SM

- The Flavor Problem

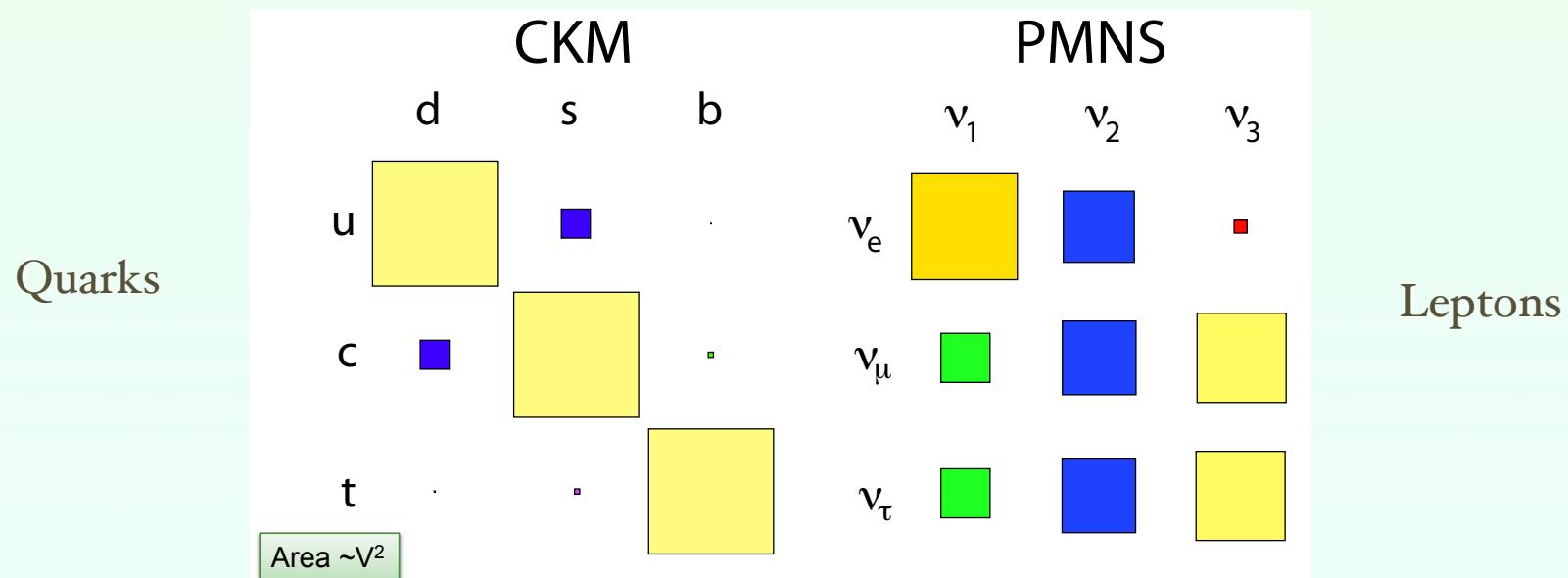


of course, some of us are a bit distracted ...



Perspectives on ... which flavor problem?

- Many questions go under “flavor problem”
I roughly classify them in two camps
- Fundamental or “origin of flavor”
 - Why 3 generations
 - Why the pattern of masses and mixings
- Structural or “coping with flavor”
 - What does flavor physics say about my favorite BSM/NP model



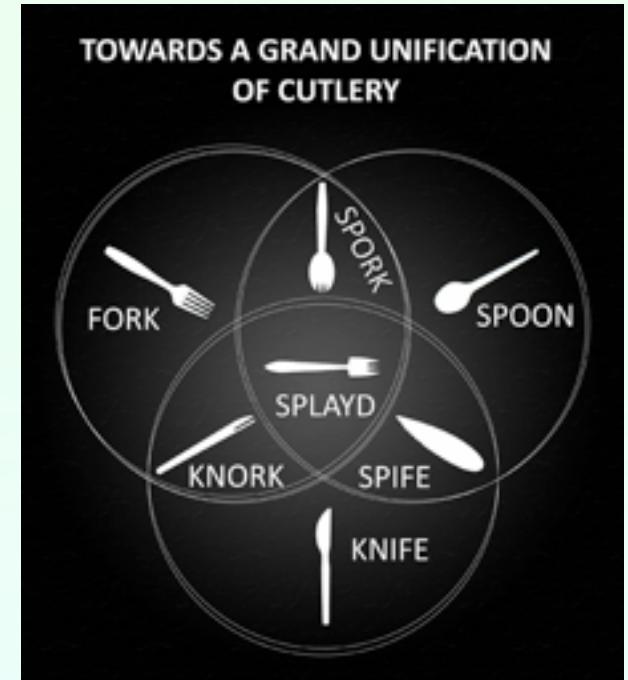
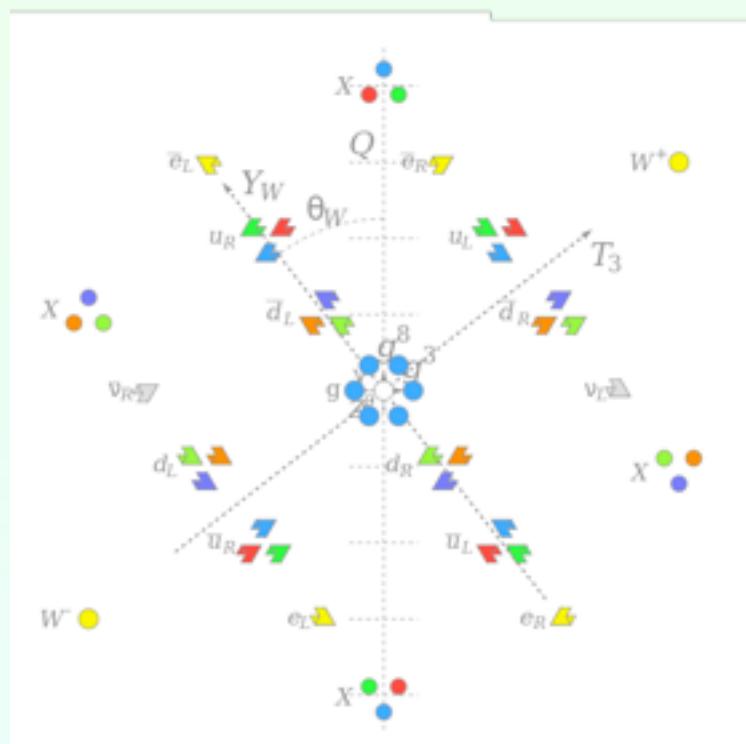
Origin of flavor

- Very few examples of theories that “explain” the number of generations
 - eg, particular compactifications of superstring theory
- Abundance of models (“theories of flavor”) addressing mixing and masses, eg
 - Discrete symmetries (A_4 , S_3 , ...)
 - Abelian, non-ableian
 - Single higgs, multiple higgs
 - w/wo SUSY
 - ...
 - Froggatt-Nielsen
 - w/wo GUT
 - w/wo SUSY
 - ...
 - Warped extra dimensions
 - Localization along extra dims produces exponential mass ratios
 - Wave function overlaps produce mixing
 - Combinations of the above

Quarks vs leptons?

Although not required, it is natural to assume a theory of the origin of flavor will address both, if not combine, the quark-flavor and the lepton-flavor problem:

- Number of generations tied: anomaly cancellation
 - Neat fit of each generation into $SU(5)$ (or $SO(10)$) GUT multiplets



Coping with flavor

- “Flavor physics” often refers only to quark sector
 - Quark mass matrices from EW breaking,
and some masses comparable to EW scale
-Flavor changing processes abound!!
- SM: built in delicate cancellations (GIM)
- Strong constraints on NP/Diagnostic tool (coroner of models)

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Merriam-Webster: “coroner:” a usually elected public officer whose principal duty is to inquire by an inquest into the cause of any death which there is reason to suppose is not due to natural causes

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- Lepton Flavor: not necessarily at EW breaking
 - Majorana neutrinos, large masses decouple (eg, see-saw)
 - Dirac neutrinos: all masses small relative to EW
- Lepton Flavor changing processes .. nowhere near as rich

- BTW, Dirac neutrinos: not such a crazy idea
 - An example I like (Arkani-Hamed & Grossman):
 - Dark side is strong interacting (weak at M_{Pl})
 - Gauge invariant operators in SM of $\text{dim} < 4$

$$H\bar{L}, \quad |H|^2, \quad B_{\mu\nu}$$

- Couple to gauge invariant dark operators, into scalar terms

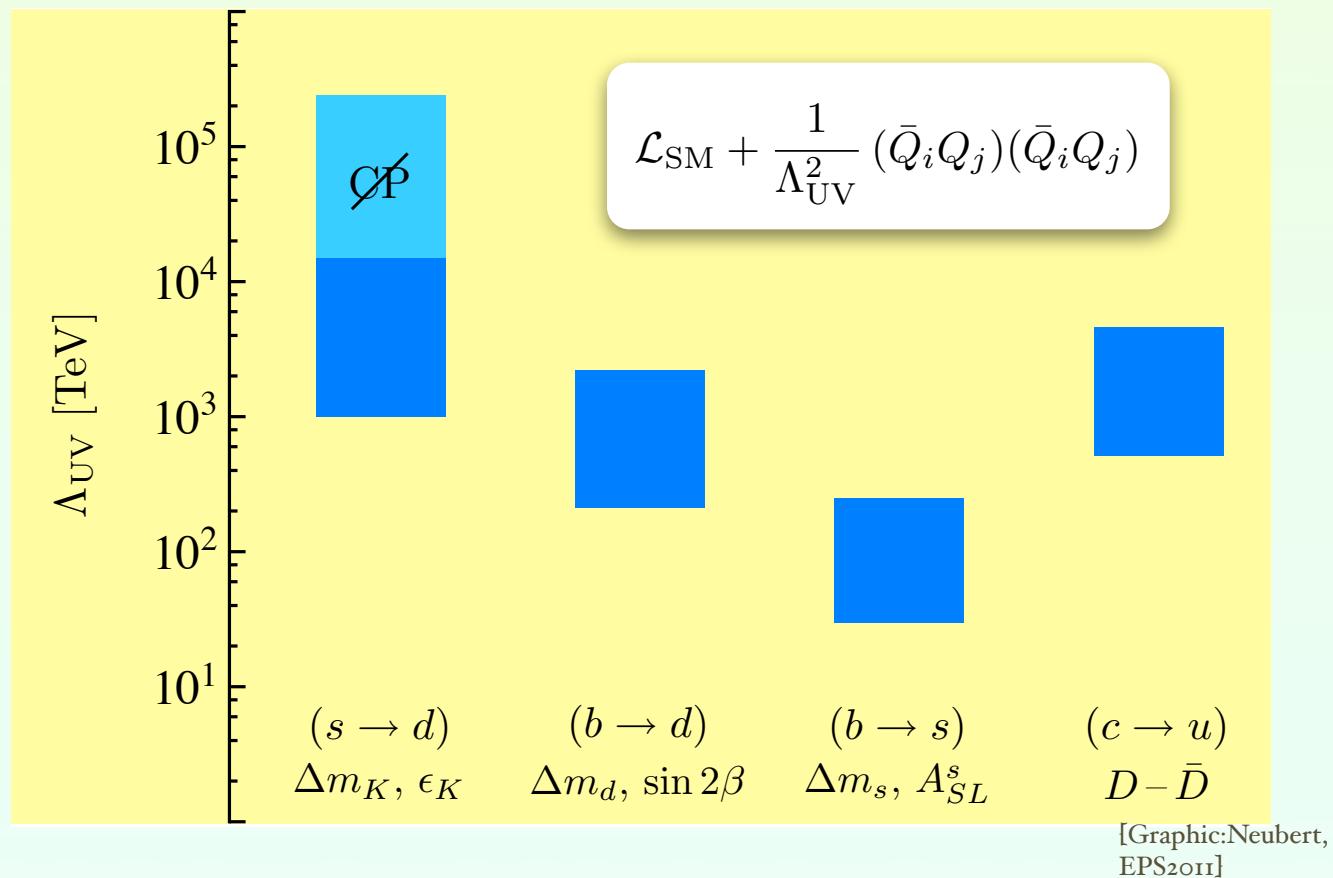
$$H\bar{L}N, \quad |H|^2S, \quad B_{\mu\nu}Y^{\mu\nu}$$

- Operators, like N , become “fundamental” once dark side goes strong at scale Λ . Dimensionless coefficients naturally of order

$$\left(\frac{\Lambda}{M_{Pl}} \right)^n$$

Generic bounds without a flavor symmetry

- Integrate out NP at UV scale
- Produce local operators
- Assume coupling is order 1
(generic, no flavor suppression)



[Graphic:Neubert,
EPS2011]

Alternatively: Specific models

DNA of models (changed from authors' "DNA of flavor physics effects")

| | AC | RVV2 | AKM | δLL | FBMSSM | LHT | RS |
|---|-----|------|-----|-------------------|--------|-----|-----|
| $D^0 - \bar{D}^0$ | ★★★ | ★ | ★ | ★ | ★ | ★★★ | ? |
| ϵ_K | ★ | ★★★ | ★★★ | ★ | ★ | ★★ | ★★★ |
| $S_{\psi\phi}$ | ★★★ | ★★★ | ★★★ | ★ | ★ | ★★★ | ★★★ |
| $S_{\phi K_S}$ | ★★★ | ★★ | ★ | ★★★ | ★★★ | ★ | ? |
| $A_{\text{CP}}(B \rightarrow X_s \gamma)$ | ★ | ★ | ★ | ★★★ | ★★★ | ★ | ? |
| $A_{7,8}(B \rightarrow K^* \mu^+ \mu^-)$ | ★ | ★ | ★ | ★★★ | ★★★ | ★★ | ? |
| $A_9(B \rightarrow K^* \mu^+ \mu^-)$ | ★ | ★ | ★ | ★ | ★ | ★ | ? |
| $B \rightarrow K^{(*)} \nu \bar{\nu}$ | ★ | ★ | ★ | ★ | ★ | ★ | ★ |
| $B_s \rightarrow \mu^+ \mu^-$ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ | ★ | ★ |
| $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ | ★ | ★ | ★ | ★ | ★ | ★★★ | ★★★ |
| $K_L \rightarrow \pi^0 \nu \bar{\nu}$ | ★ | ★ | ★ | ★ | ★ | ★★★ | ★★★ |
| $\mu \rightarrow e \gamma$ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ |
| $\tau \rightarrow \mu \gamma$ | ★★★ | ★★★ | ★ | ★★★ | ★★★ | ★★★ | ★★★ |
| $\mu + N \rightarrow e + N$ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ |
| d_n | ★★★ | ★★★ | ★★★ | ★★ | ★★★ | ★ | ★★★ |
| d_e | ★★★ | ★★★ | ★★ | ★ | ★★★ | ★ | ★★★ |
| $(g-2)_\mu$ | ★★★ | ★★★ | ★★ | ★★★ | ★★★ | ★ | ? |

Table 8: "DNA" of flavour physics effects for the most interesting observables in a selection of SUSY and non-SUSY models. ★★★ signals large effects, ★★ visible but small effects and ★ implies that the given model does not predict sizable effects in that observable.

AC: Agashe-Carone abelian U(1) susy

RVV2: Ross, Velasco-Sevilla, Vives (non-ab, susy)

AKM: Antusch, King, Malinsky (non-ab, susy)

FBMSSM: flavor blind MSSM

δLL : MFV MSSM with LL mass insertions

LHT: Littlest higgs with T-parity

RS: warped extra-dims model with custodial protection

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| $K_L \rightarrow \pi^0 \nu \bar{\nu}$ | ★ | ★ | ★ | ★ | ★ | ★★★ | ★★★ |
| $\mu \rightarrow e \gamma$ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ | ★★★ |
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CPV in interference of mixing/decay

- Decay amplitudes in terms of weak (ϕ_k) and strong (δ_k) phases

$$A_f = \langle f | H | B \rangle = \sum_k A_k e^{i\delta_k} e^{i\phi_k}, \quad \bar{A}_{\bar{f}} = \langle \bar{f} | H | \bar{B} \rangle = \sum_k A_k e^{i\delta_k} e^{-i\phi_k}.$$

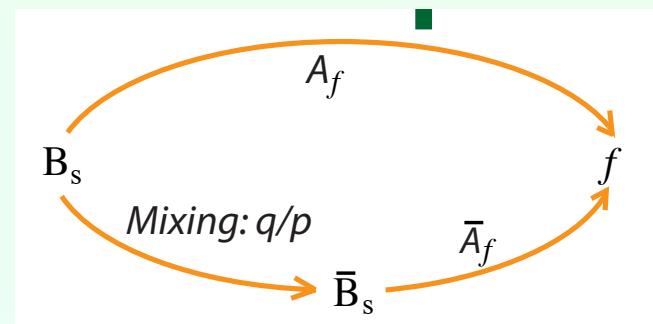
- CPV in decay if non-vanishing

$$|\bar{A}_{\bar{f}}|^2 - |A_f|^2 \propto \sin(\phi_1 - \phi_2) \sin(\delta_1 - \delta_2)$$

- Theory input: strong phases (usually model dependent)

- Instead CPV in interference of mixing.decay can be theo-clean

- If amplitudes with a single weak phase dominate

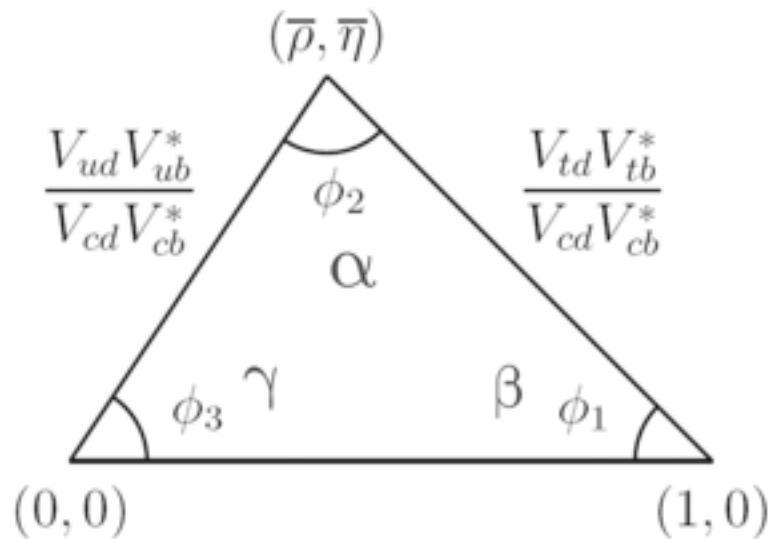


- Simplest if f is a CP eigenstate

$$a(t) = \frac{\Gamma[\bar{B}^0(t) \rightarrow f] - \Gamma[B^0(t) \rightarrow f]}{\Gamma[\bar{B}^0(t) \rightarrow f] + \Gamma[B^0(t) \rightarrow f]}$$

$$= S_f \sin(\Delta m t) - C_f \cos(\Delta m t)$$

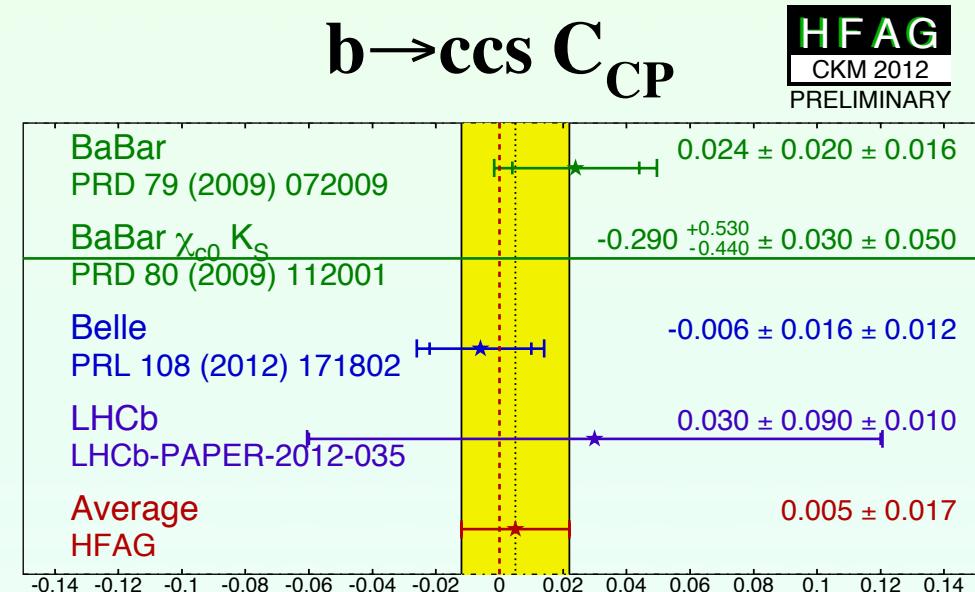
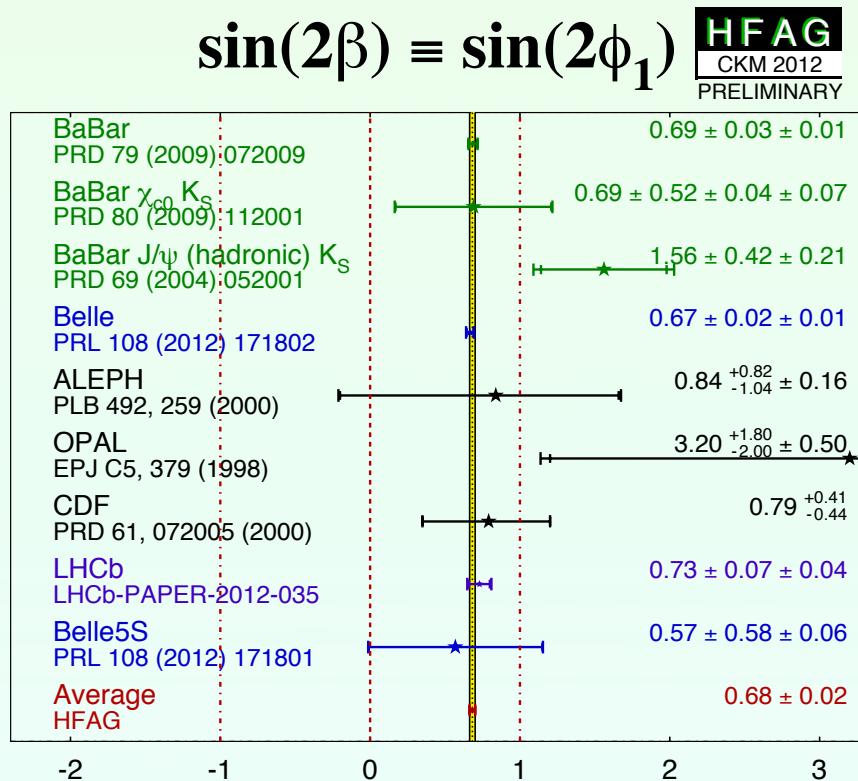
where $S_f = \frac{2 \operatorname{Im} \lambda_f}{1 + |\lambda_f|^2}, \quad C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}, \quad \lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}.$



Gold plated examples: $b \rightarrow c\bar{c}s$

$$B^0 \rightarrow \psi K_{L,S}^0 \quad \lambda_{\psi K_{S,L}^0} = \mp \left(\frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*} \right) \left(\frac{V_{cb} V_{cs}^*}{V_{cb}^* V_{cs}} \right) \left(\frac{V_{cs} V_{cd}^*}{V_{cs}^* V_{cd}} \right) = \mp e^{-2i\beta}$$

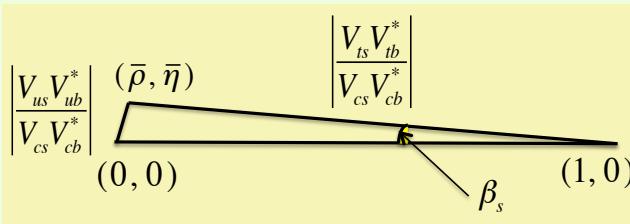
-CP of S, L q/p \bar{A}_f/A_f p/q for K



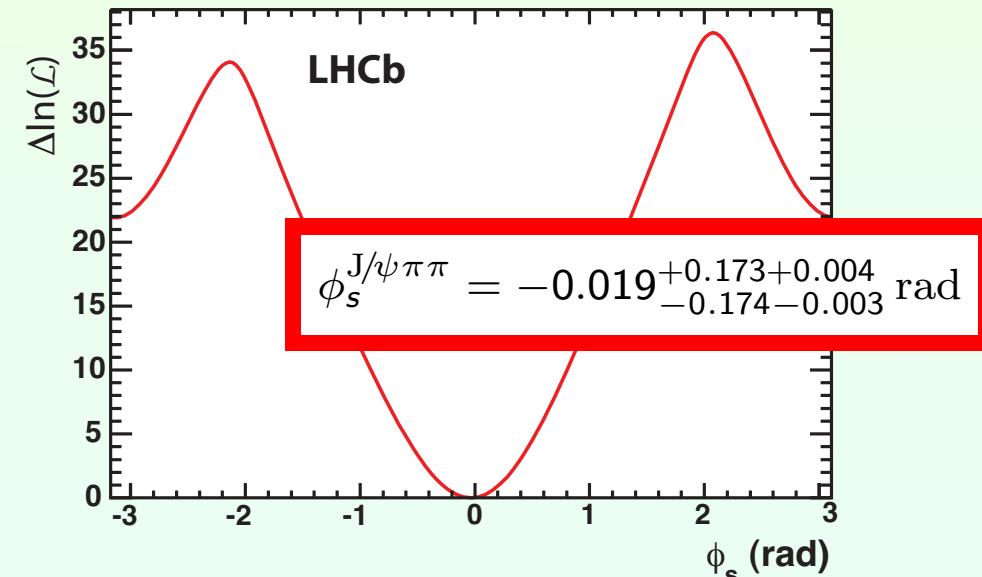
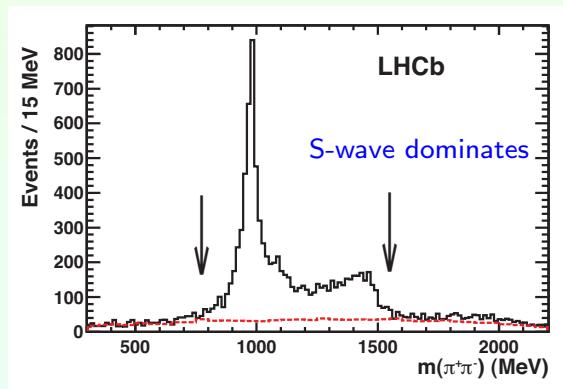
and $B_s \rightarrow \psi\phi, \psi\pi^+\pi^-$

$$\lambda_{\psi\pi^+\pi^-} = - \left(\frac{V_{tb}^* V_{ts}}{V_{tb} V_{ts}^*} \right) \left(\frac{V_{cb} V_{cs}^*}{V_{cb}^* V_{cs}} \right) = -e^{-2i\beta_s}$$

small angle in squashed unitarity triangle
 ≈ 0 in SM



$$\varphi_s^{SM} \equiv -2\beta_s = -2 \arg \left(-\frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*} \right) = -0.04 \text{ rad}$$



$B \rightarrow \psi\phi(K^+K^-)$ requires angular analysis, separate partial waves. Combined analysis:

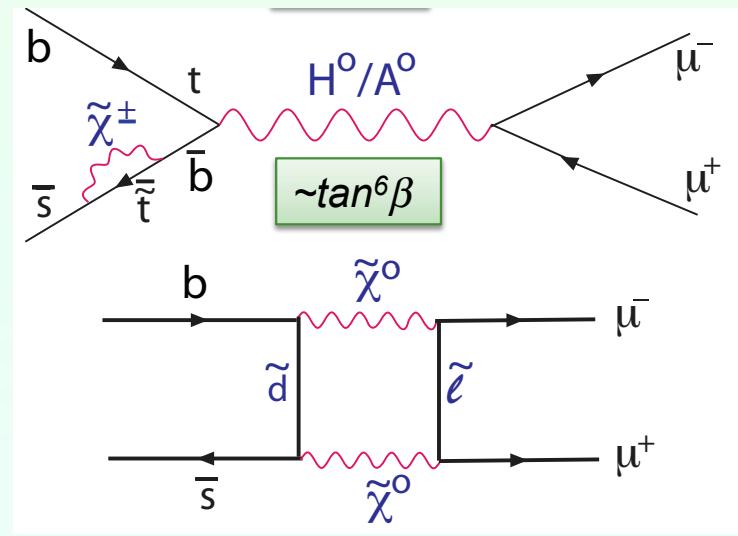
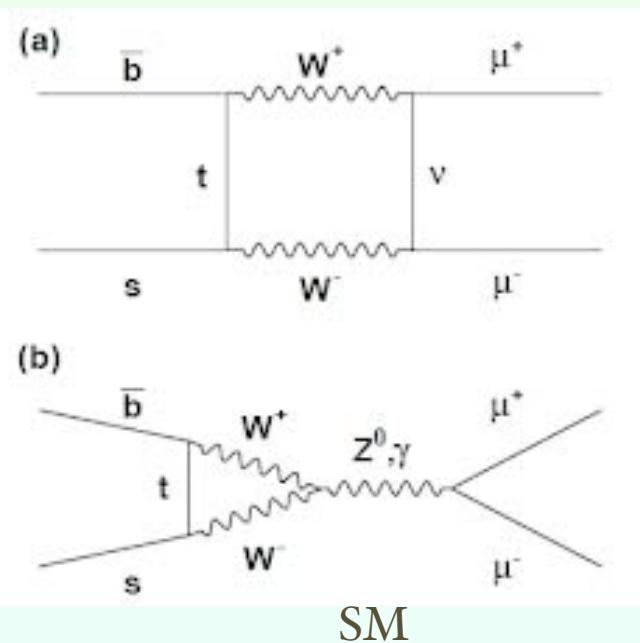
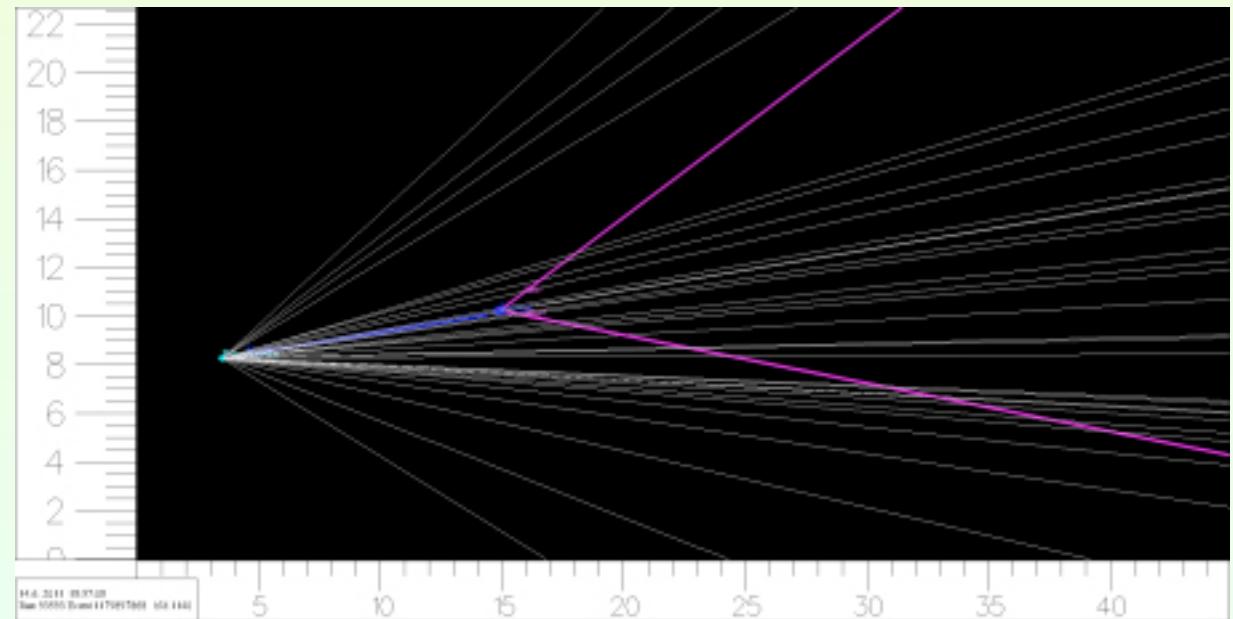
$$\phi_s = -0.002 \pm 0.083 \pm 0.027 \text{ rad}$$

[G Cowan, ICHEP 2012]

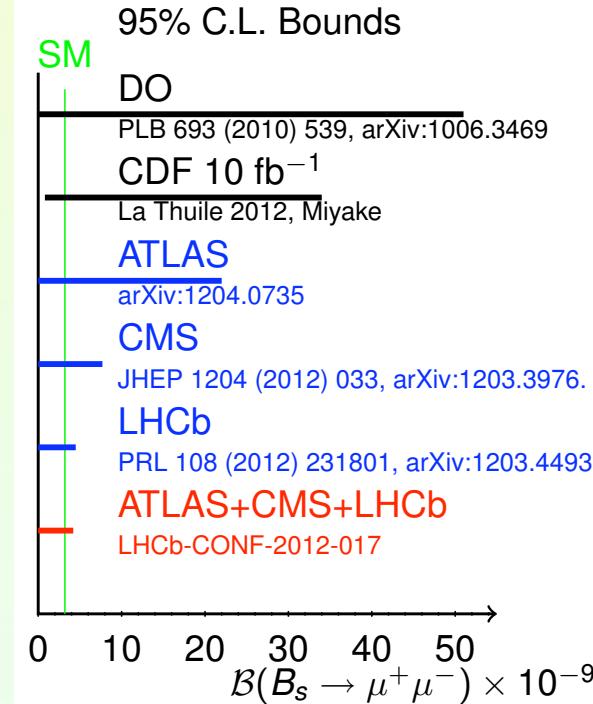
$$\underline{B \rightarrow \mu^+ \mu^-}$$

Reconstructed $B \rightarrow \mu^+ \mu^-$
event from the
LHCb Collaboration
[muon.wordpress.com]

Sensitive to NP:



As of July 2012 (ICHEP)
bounds only



LHCb-CONF-2012-017
Preliminary upper limits
(95% C.L.):

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) < 4.2 \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 8.1 \times 10^{-10}$$

LHCb measurement (Nov 2012)

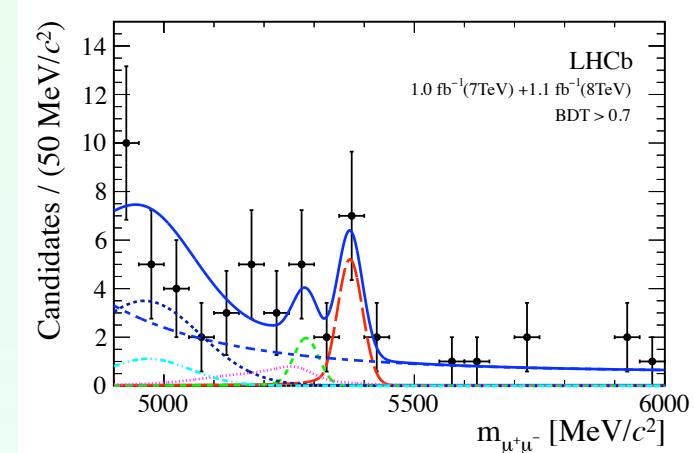
$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.2^{+1.4}_{-1.2}(\text{stat})^{+0.5}_{-0.3}(\text{syst})) \times 10^{-9}$$

recall:

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)^{\text{SM}} = (3.23 \pm 0.27) \times 10^{-9}$$

Also new (best) bound:

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 9.4 \times 10^{-10}$$



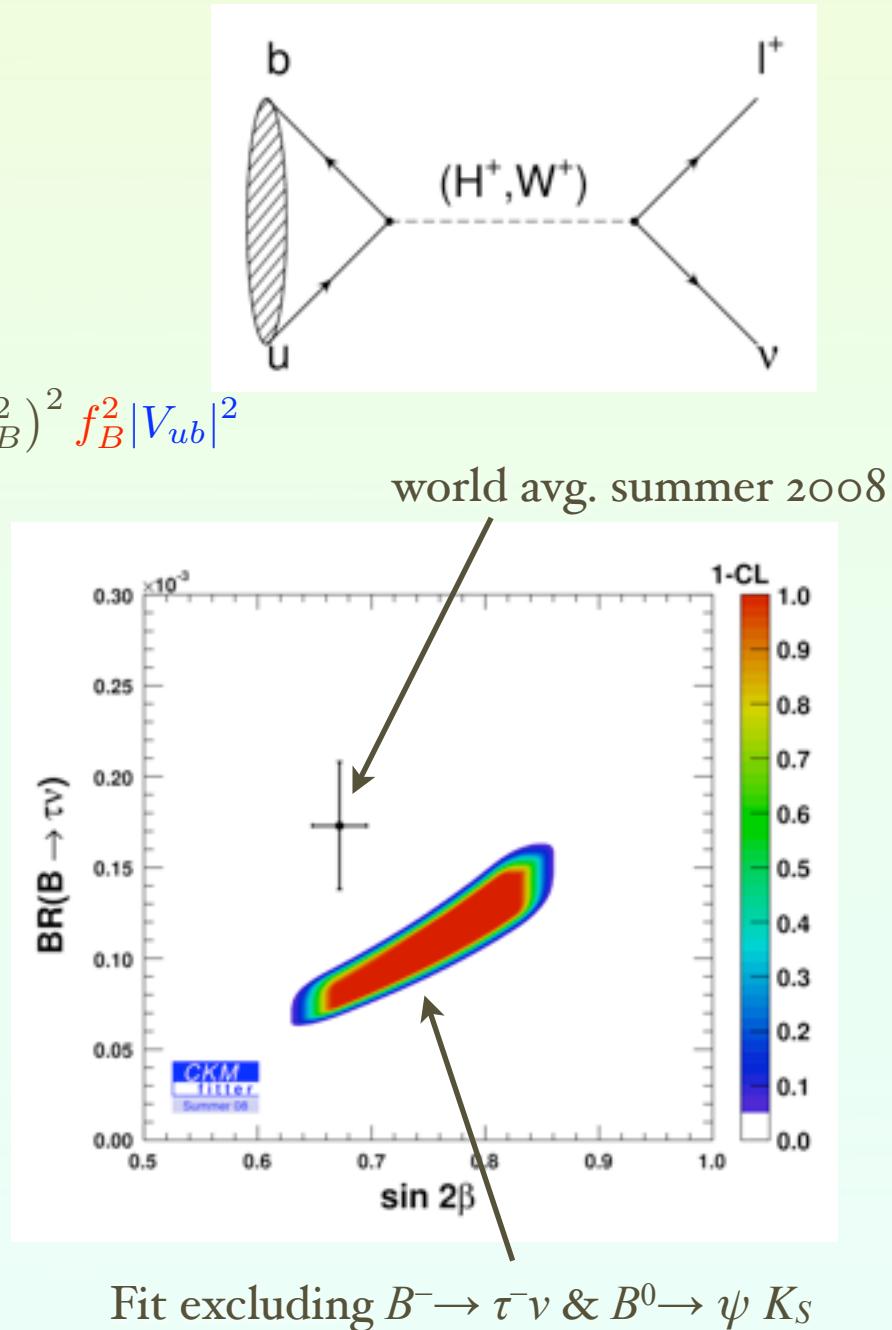
[LHCb, Phys.Rev.Lett. 110 (2013) 021801]

Implications for NP searches

- With few exceptions, no deviations from SM
- Exceptions (some are going away already):
 - $B^- \rightarrow \tau^- \nu$ (*next slide*), $B^- \rightarrow D\tau^- \nu$, $B^- \rightarrow D^*\tau^- \nu$
 - Isospin asymmetry A_I in $B \rightarrow K \mu^+ \mu^-$
 - Flavor specific CP asymmetry a_{s1}
 - FB-asymmetry in top production at Tevatron
 - muon $g - 2$
- Tightening bounds on NP require specialized analysis of specific models
 - (infinitely) many variations of SUSY
 - variations on extra-dimensions
 - techni-color (strongly coupled higgs sector with dilaton)
 -

Is there still a problem with $B^- \rightarrow \tau^- \nu$?

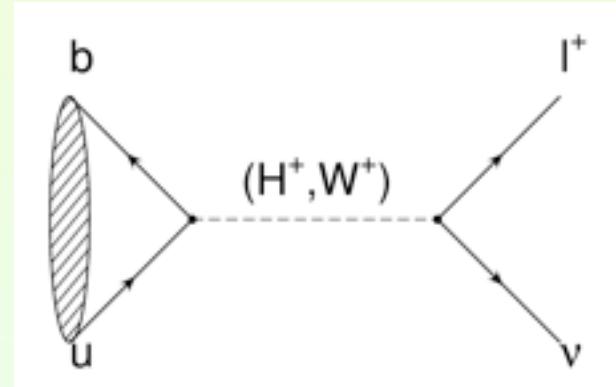
- $B^- \rightarrow \tau^- \nu$ in SM is tree level
- Clean SM prediction, lattice gives f_B
- Modified for τ , less for e, μ , by charged higgs in 2HDM
- 2HDM modifies box diagram too: cannot use SM extraction of $\sin(2\beta)$ from $B^0 \rightarrow \psi K_S$
- But NEW Belle result [\[arXiv:1208.4678\]](https://arxiv.org/abs/1208.4678)



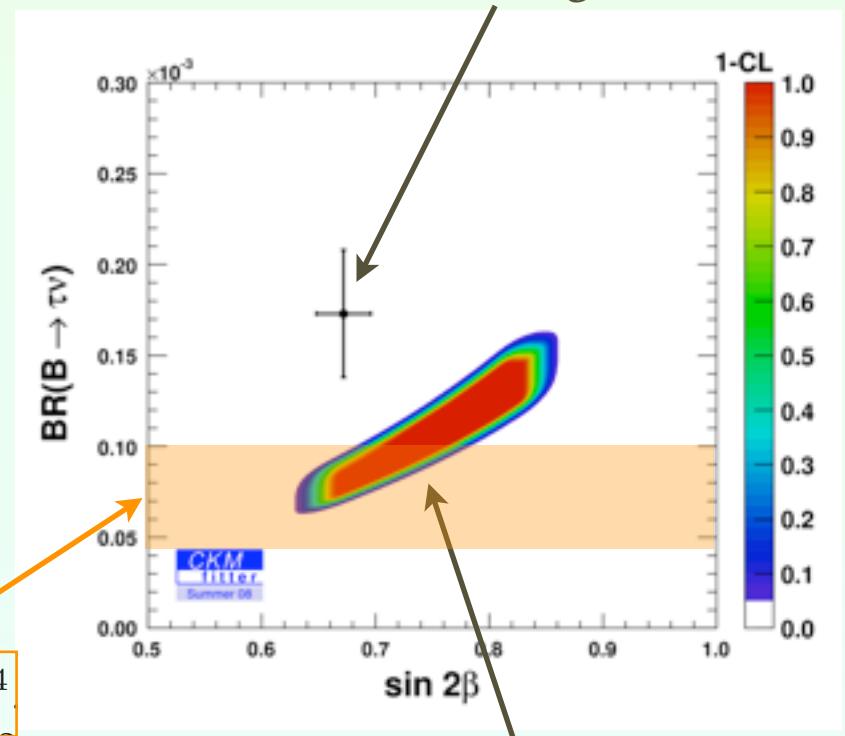
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- But NEW Belle result [\[arXiv:1208.4678\]](https://arxiv.org/abs/1208.4678)

$$\mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}_\tau) = [0.72^{+0.27}_{-0.25}(\text{stat}) \pm 0.11(\text{syst})] \times 10^{-4}$$



world avg. summer 2008

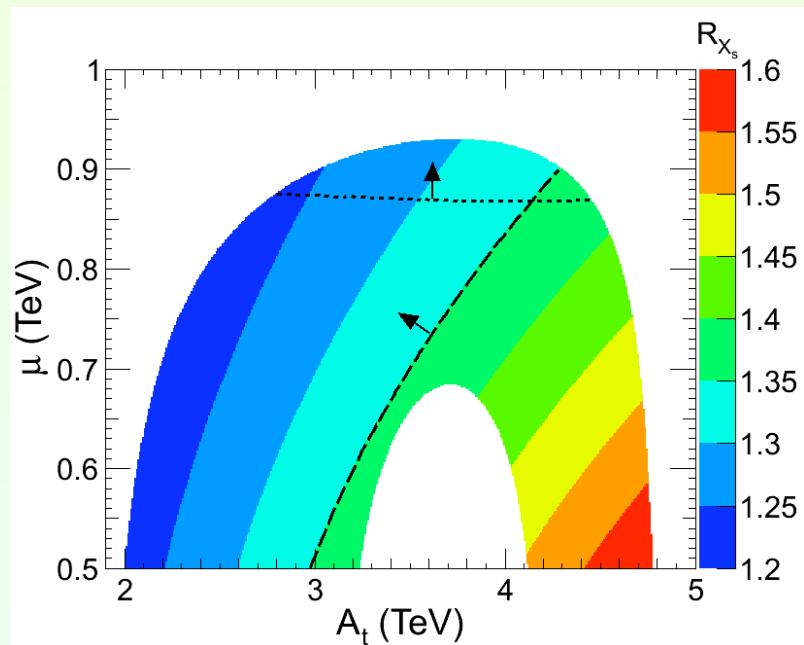
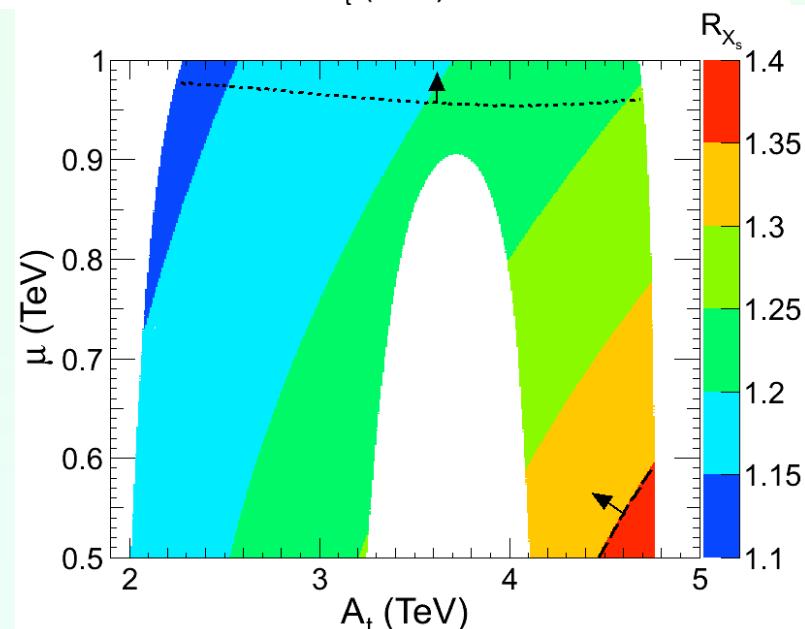


Fit excluding $B^- \rightarrow \tau^- \nu$ & $B^0 \rightarrow \psi K_S$

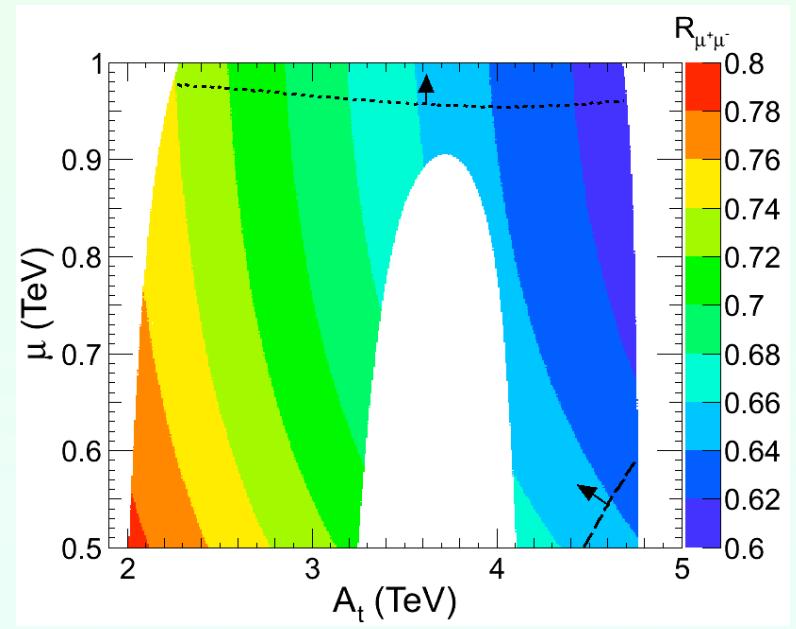
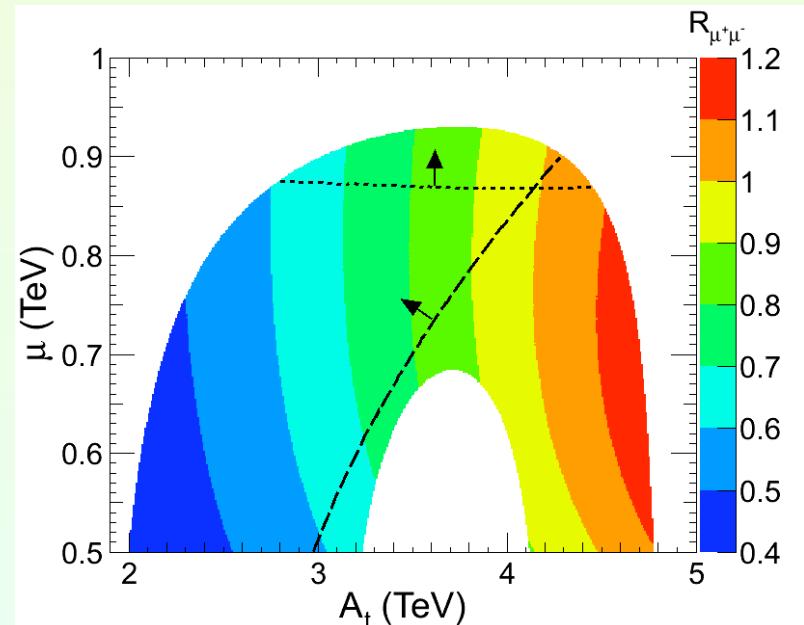
$$\frac{\mathcal{B}(B \rightarrow K^* \gamma)^{\text{EXP}}}{\mathcal{B}(B \rightarrow K^* \gamma)^{\text{SM}}} = 1.13 \pm 0.10$$

 $\tan \beta = 60$

$$R_{X_s} = \frac{\text{BR}(B \rightarrow X_s \gamma)_{\text{MSSM}}}{\text{BR}(B \rightarrow X_s \gamma)_{\text{SM}}}$$

 $\tan \beta = 30$ 

$$R_{\mu^+ \mu^-} = \frac{\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{MSSM}}}{\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}}$$

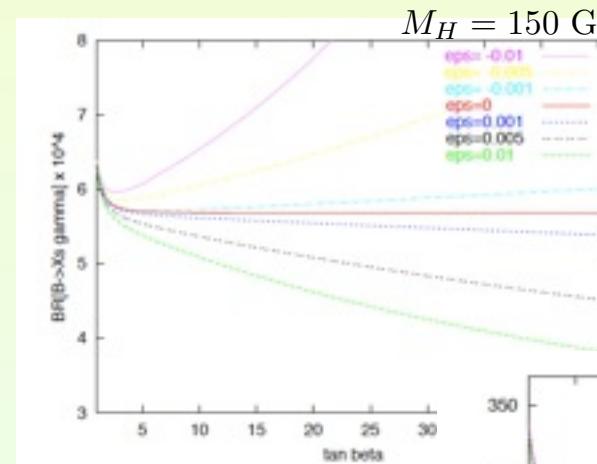


flash back, 4 years ago...

CMSSM (at large $\tan \beta$, possibly)

$\tan \beta \sim 1$ charged Higgs and
chargino

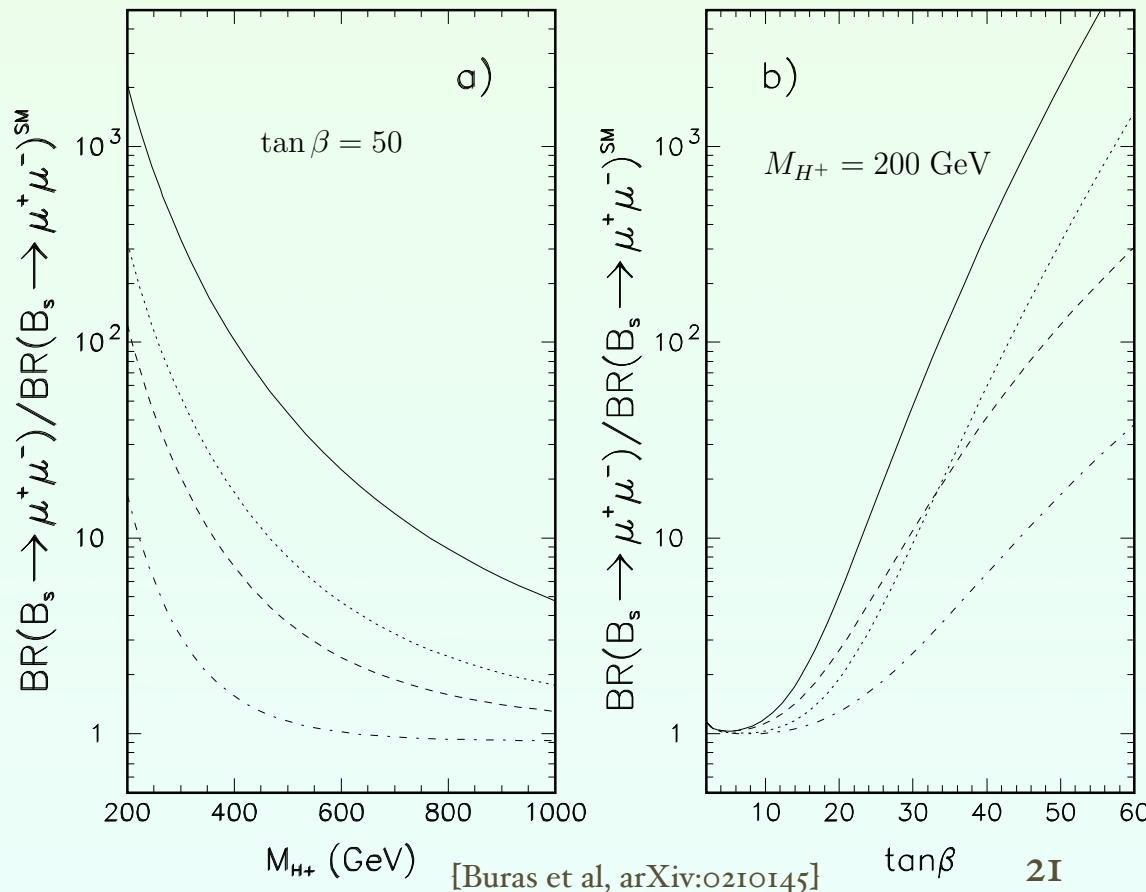
$\tan \beta \gg 1$ exchanges dominant
Higgs exchange dominant



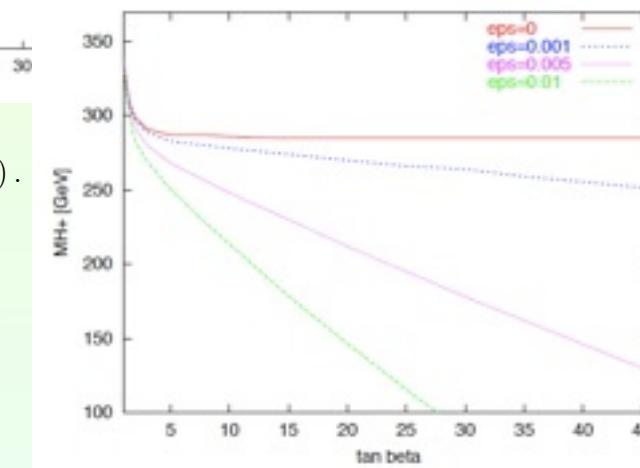
[Degrassi et al, arXiv:0009337]

$$m_b = \sqrt{2} M_W \frac{y_b}{g} \cos \beta (1 + \epsilon_b \tan \beta).$$

five new (beyond SM) parameters



[Buras et al, arXiv:0210145]



solid: $\mu < 0$ $M_{\tilde{t}_1} = 500$ GeV, $M_{\tilde{t}_2} = 850$ GeV

dashed: $\mu > 0$ $M_{\tilde{t}_1} = 500$ GeV, $M_{\tilde{t}_2} = 850$ GeV

dot-dash: $\mu > 0$ $M_{\tilde{t}_1} = 600$ GeV, $M_{\tilde{t}_2} = 750$ GeV

dotted: $\mu < 0$ $M_{\tilde{t}_1} = 600$ GeV, $M_{\tilde{t}_2} = 750$ GeV

CMSSM (at large $\tan \beta$, possibly)

$\tan \beta \sim 1$

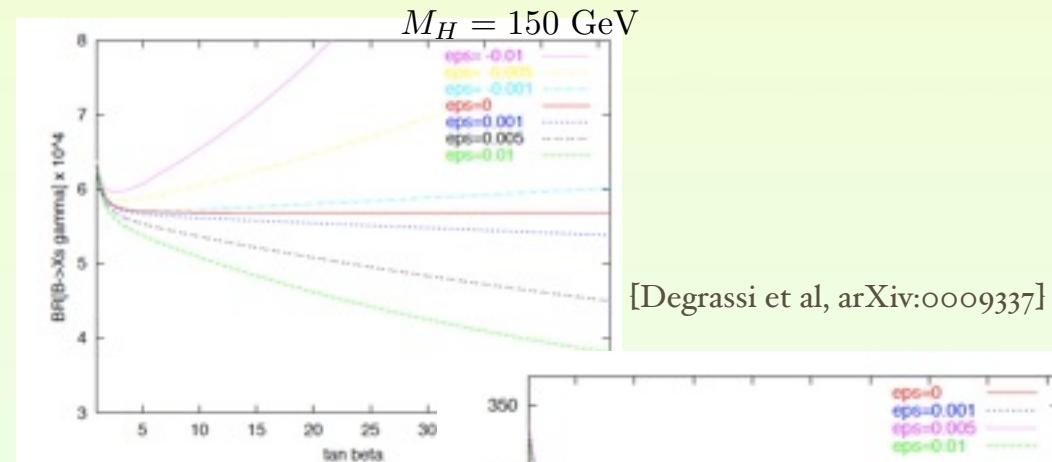
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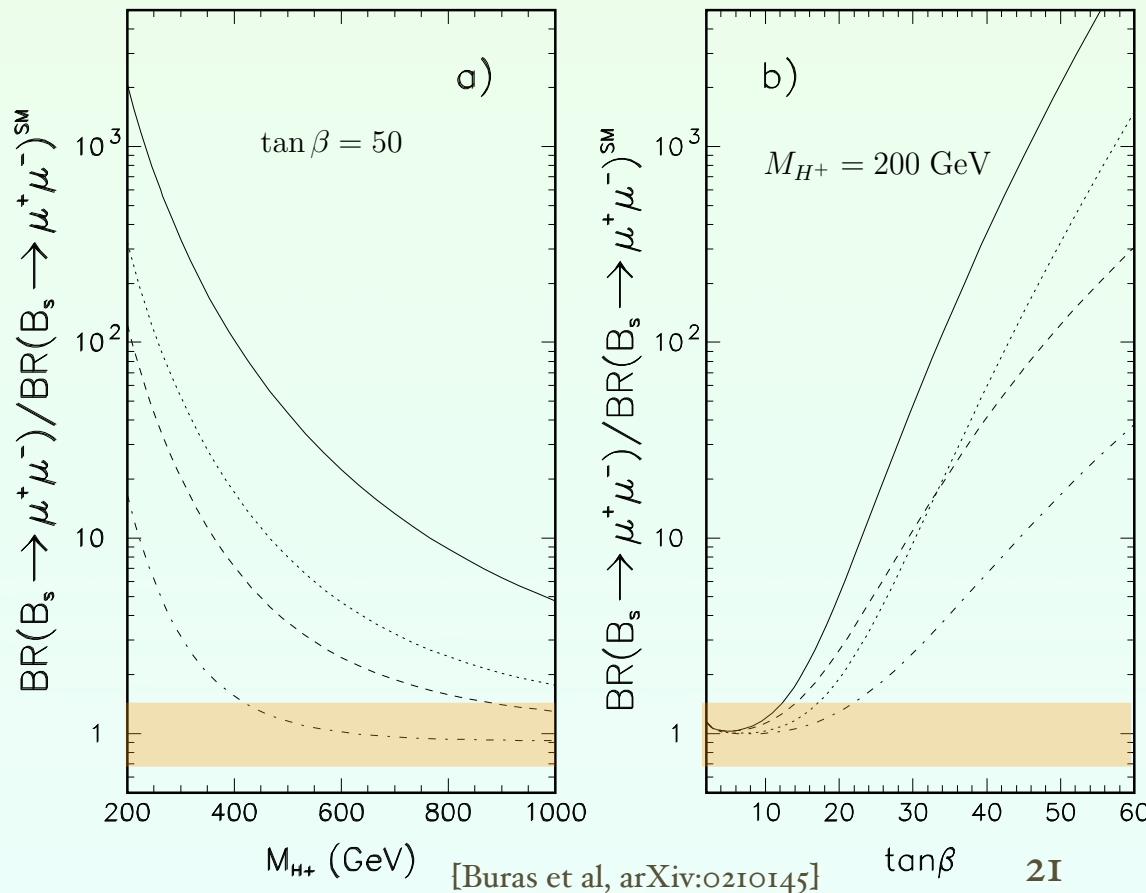
Higgs exchange dominant

$\tan \beta \gg 1$



[Degrassi et al, arXiv:0909.337]

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[Buras et al, arXiv:0910.45]

solid: $\mu < 0$ $M_{\tilde{t}_1} = 500$ GeV, $M_{\tilde{t}_2} = 850$ GeV

dashed: $\mu > 0$ $M_{\tilde{t}_1} = 500$ GeV, $M_{\tilde{t}_2} = 850$ GeV

dot-dash: $\mu > 0$ $M_{\tilde{t}_1} = 600$ GeV, $M_{\tilde{t}_2} = 750$ GeV

dotted: $\mu < 0$ $M_{\tilde{t}_1} = 600$ GeV, $M_{\tilde{t}_2} = 750$ GeV

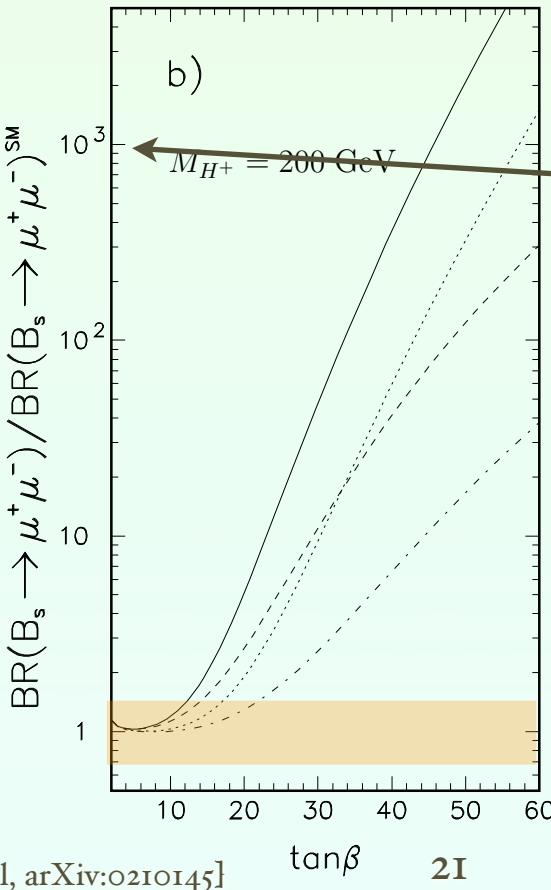
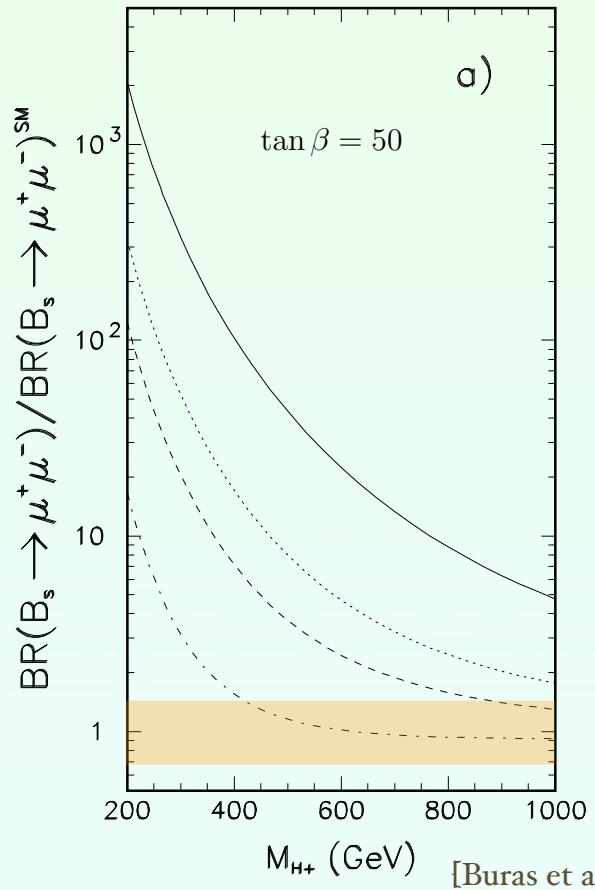
Nov 2012 LHCb

CMSSM (at large $\tan \beta$, possibly)

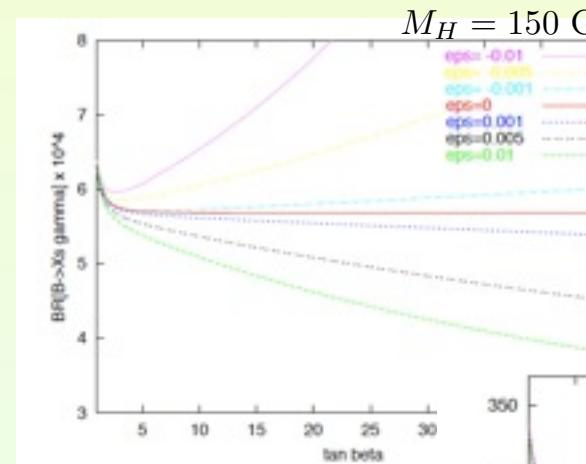
$\tan \beta \sim 1$ charged Higgs and
chargino

$\tan \beta \gg 1$ exchanges dominant
Higgs exchange dominant

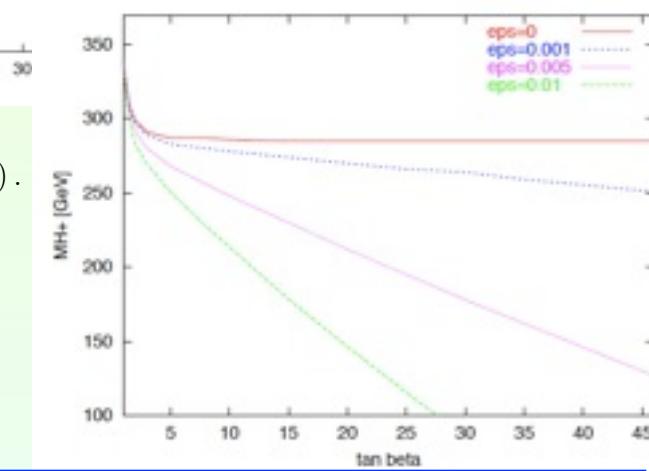
five new (beyond SM) parameters



[Buras et al, arXiv:0210145]



[Degrassi et al, arXiv:0009337]



Scale! Compare with previous slide!!!

solid: $\mu < 0$ $M_{\tilde{t}_1} = 500 \text{ GeV}, M_{\tilde{t}_2} = 850 \text{ GeV}$

dashed: $\mu > 0$ $M_{\tilde{t}_1} = 500 \text{ GeV}, M_{\tilde{t}_2} = 850 \text{ GeV}$

dot-dash: $\mu > 0$ $M_{\tilde{t}_1} = 600 \text{ GeV}, M_{\tilde{t}_2} = 750 \text{ GeV}$

dotted: $\mu < 0$ $M_{\tilde{t}_1} = 600 \text{ GeV}, M_{\tilde{t}_2} = 750 \text{ GeV}$

Nov 2012 LHCb

At this point I am supposed to show you many more plots of the restricted parameter space in versions of low energy SUSY, extra-dimensions, little higgs.....



Instead, get some “perspective”

Minimal Flavor Violation (MFV)

- Let's take a more generic, less mode dependent, approach
- MFV Premise: Unique source of flavor braking
- Quark sector in SM, in absence of masses has large flavor (global) symmetry G_F :

$$U(3)_{Q_L} \otimes U(3)_{U_R} \otimes U(3)_{D_R}$$

- In SM, symmetry is only broken by Yukawa interactions, parametrized by couplings Y_U and Y_D

For the benefit of the experts, who don't seem to get it:

- NP models must have at least this amount of symmetry breaking (“minimal”)
 - They may have more
 - Irrelevant. Here is the story: given new stuff at a given scale Λ , virtual processes will induce corrections to flavor processes (not necessarily perturbatively). Question is: what is the minimum effect in flavor changing processes we have a right to expect?
 - And, yes, it can be avoided by tuning

MFV cont'd

- Recall. Flavor group G_F is

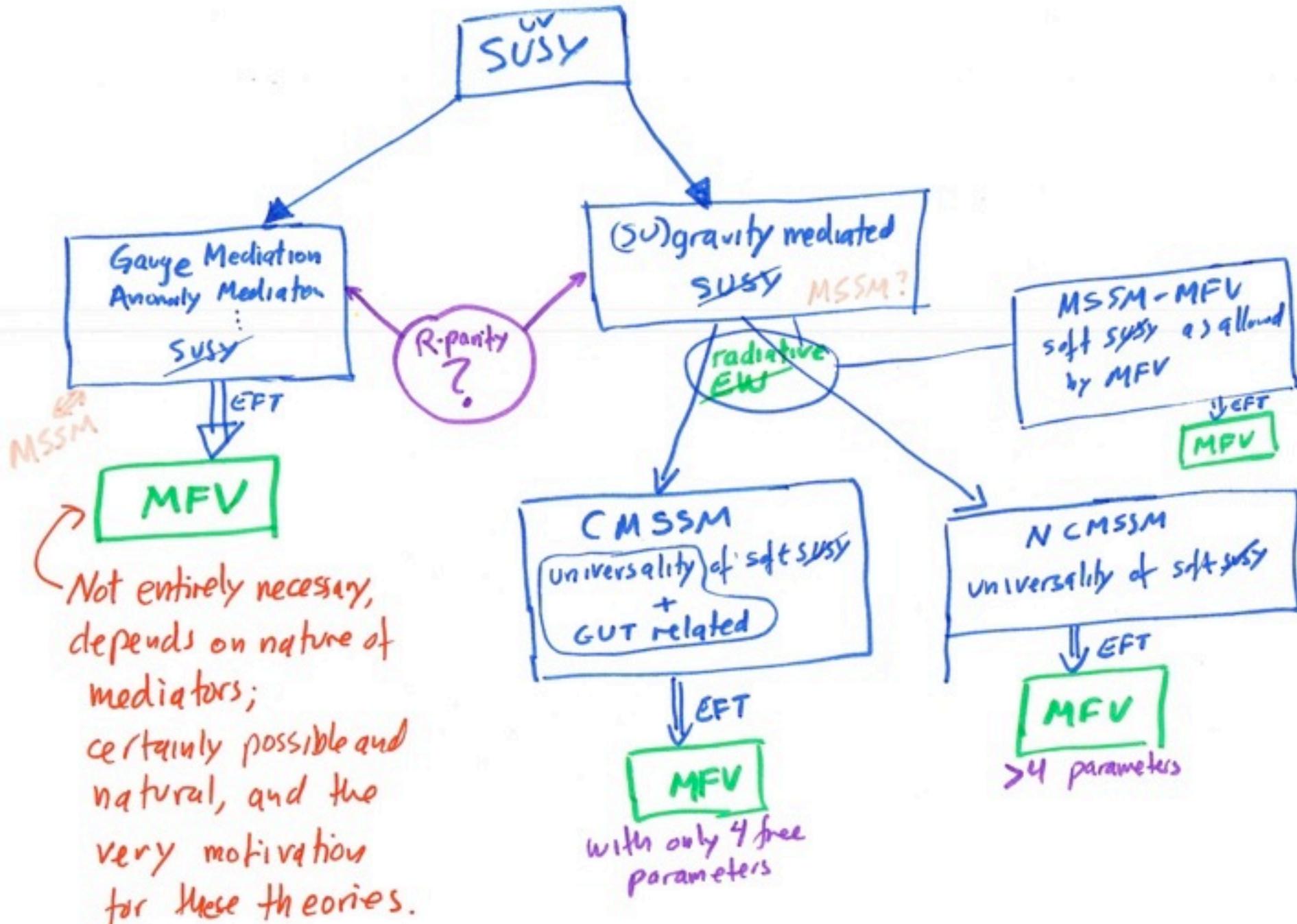
$$U(3)_{Q_L} \otimes U(3)_{U_R} \otimes U(3)_{D_R}$$

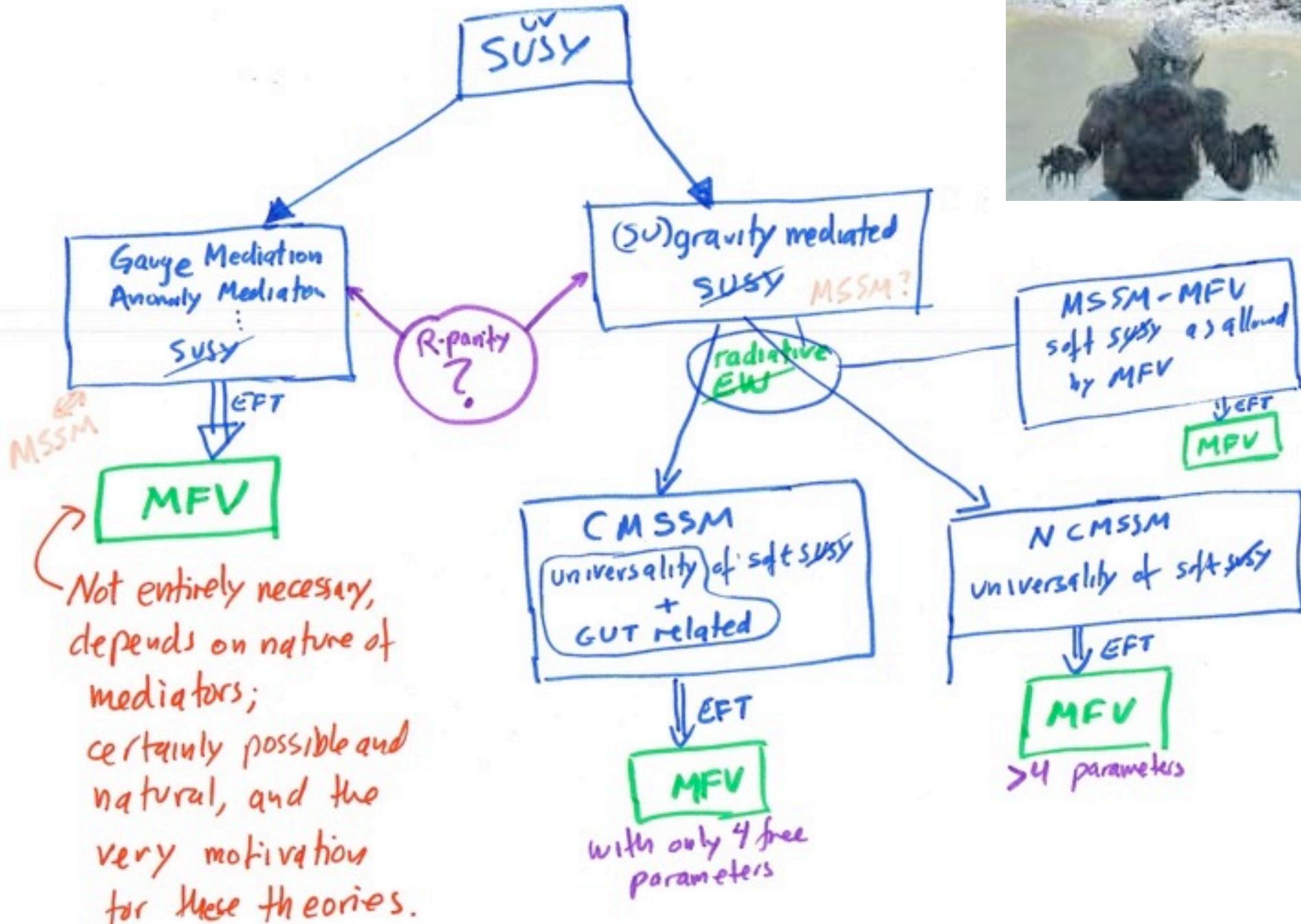
- In SM, symmetry is only broken by Yukawa interactions, parametrized by couplings Y_U and Y_D
- MFV: all breaking of G_F must arise from Y_U and Y_D .
- In practice: Build G_F invariants with Y_U and Y_D as constant fields, a.k.a. “spurions”

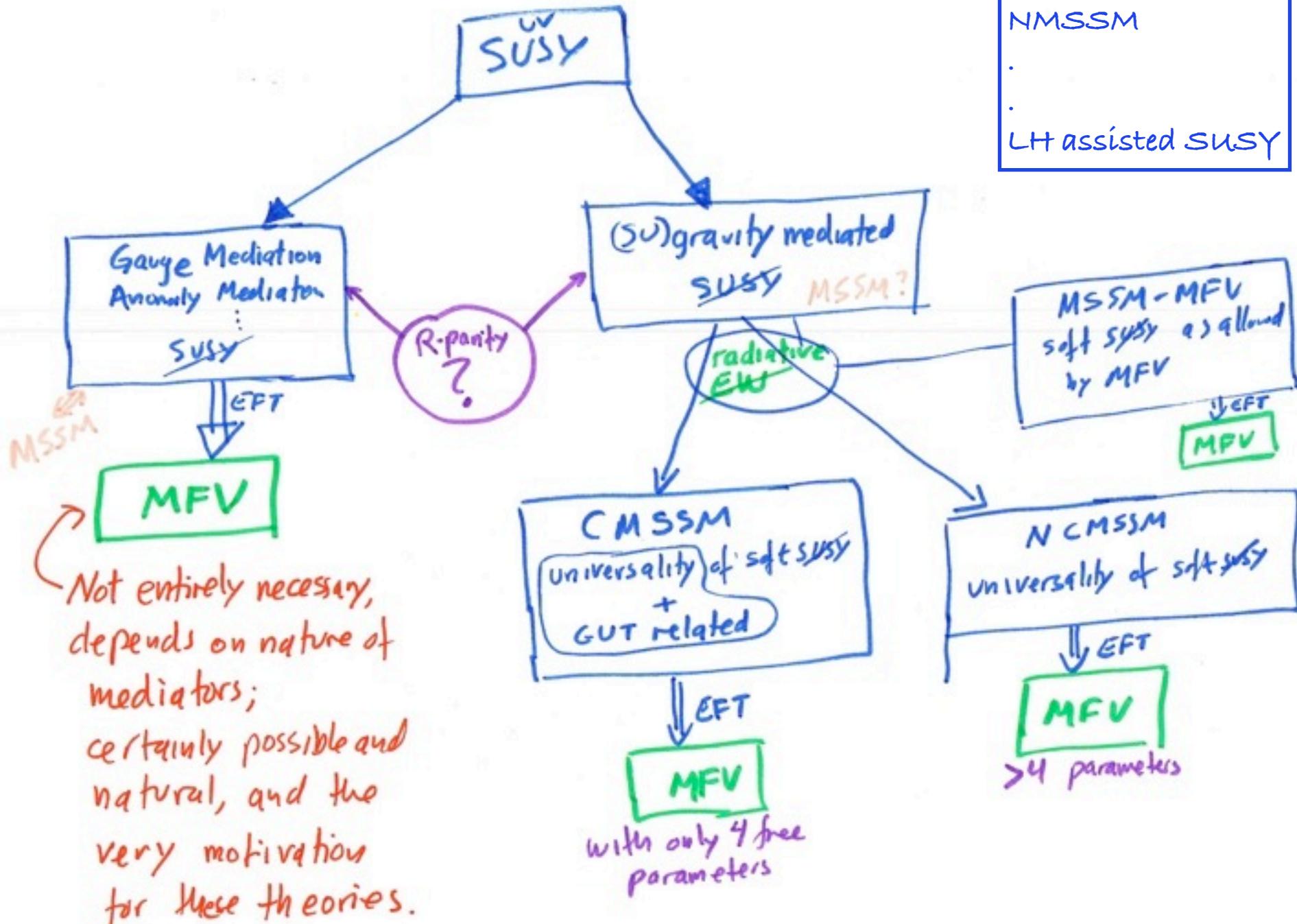
$$Y_u = (\bar{3}, 3, 1),$$

$$Y_d = (\bar{3}, 1, 3).$$

- When going to mass eigenstate basis, all mixing is parametrized by CKM and GIM-like cancellations are automatic
- Result: NP parametrized by high dimension operators: $\Lambda \leq 3\text{--}10 \text{ TeV}$
 - For perturbative NP $\Lambda = 4\pi M$







Digression: can we take spurions seriously?

- Want a model in which spurions are VEVs of scalars
- Want a renormalizable model
- Must gauge G_F (else NGB disaster)
- Desirable (but unnecessary): some chance of LHC physics. But
 - expect $M_V \sim 10^4$ TeV from K^0 physics
 - expect spectrum of vectors roughly like VEVs, i.e., like $Y_{U,D}$
 - so all vectors heavier than 10^4 TeV unless, somehow: inverted hierarchy
- Must: anomaly free
- Desirable: Simplest
- Note: $N = 3$ of generations “explained” (no less than $N_c = 3$ colors explained)
(while spectrum and pattern of mixings still engineered).

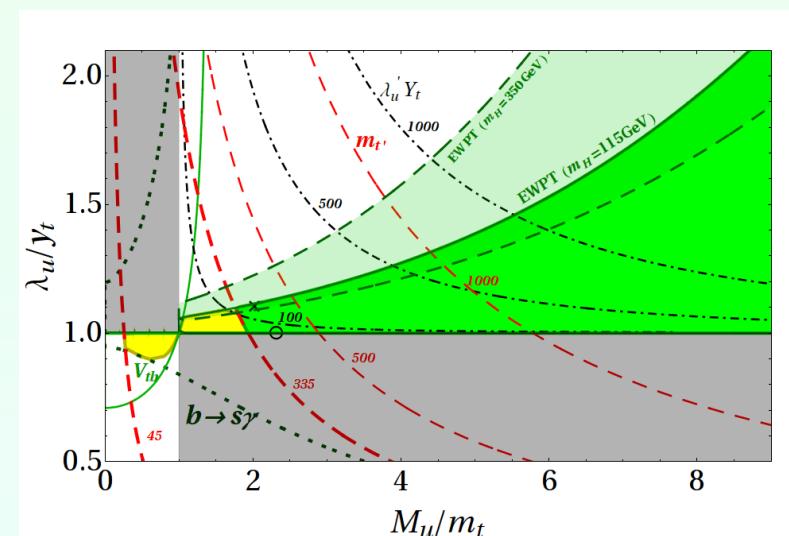
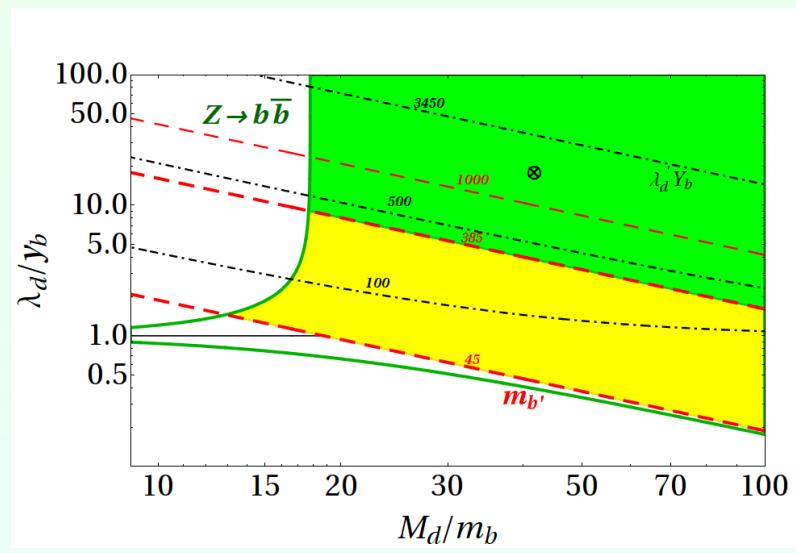
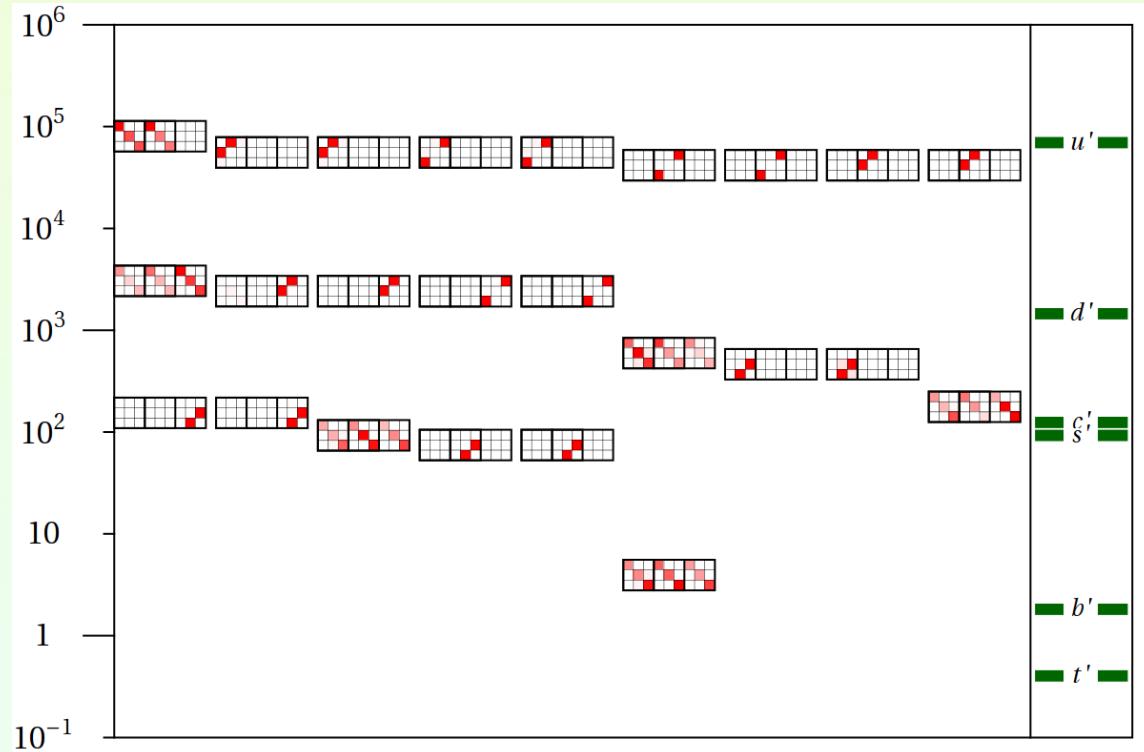
Surprisingly, the simplest renormalizable SM extension with gauged, anomaly free G_F has an inverted hierarchy of vector masses (relative to quark masses)

| | $SU(3)_{Q_L}$ | $SU(3)_{U_R}$ | $SU(3)_{D_R}$ | $SU(3)_c$ | $SU(2)_L$ | $U(1)_Y$ |
|-------------|---------------|---------------|---------------|-----------|-----------|----------|
| Q_L | 3 | 1 | 1 | 3 | 2 | 1/6 |
| U_R | 1 | 3 | 1 | 3 | 1 | 2/3 |
| D_R | 1 | 1 | 3 | 3 | 1 | -1/3 |
| Ψ_{uR} | 3 | 1 | 1 | 3 | 1 | 2/3 |
| Ψ_{dR} | 3 | 1 | 1 | 3 | 1 | -1/3 |
| Ψ_u | 1 | 3 | 1 | 3 | 1 | 2/3 |
| Ψ_d | 1 | 1 | 3 | 3 | 1 | -1/3 |
| Y_u | $\bar{3}$ | 3 | 1 | 1 | 1 | 0 |
| Y_d | $\bar{3}$ | 1 | 3 | 1 | 1 | 0 |
| H | 1 | 1 | 1 | 1 | 2 | 1/2 |

Most general renormalizable lagrangian

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{kin} - V(Y_u, Y_d, H) + \\ & (\lambda_u \bar{Q}_L \tilde{H} \Psi_{uR} + \lambda'_u \bar{\Psi}_u Y_u \Psi_{uR} + M_u \bar{\Psi}_u U_R + \\ & \lambda_d \bar{Q}_L H \Psi_{dR} + \lambda'_d \bar{\Psi}_d Y_d \Psi_{dR} + M_d \bar{\Psi}_d D_R + h.c.) , \end{aligned}$$

Spectrum (arbitrary overall scale, take it as TeV)



but this is INVISIBLES ...

Leptons

- it is easy to accommodate leptons in the gauged- G_F model
- MLFV: MFV for lepton sector
 - Best justified by GUTs, so may as well...
- MFV GUT
 - GUTs connect MFV in quark and lepton sectors
 - New effects (e.g., LFV even for Dirac neutrino)
 - Includes thoroughly studied models
(e.g., SUSY-GUTs)

MFV-GUTs in a nut-shell

three families of
left handed fields:

$$\begin{array}{cccc} \psi_i \sim \bar{\mathbf{5}} & \chi_i \sim \mathbf{10} & N_i \sim \mathbf{1} & i = 1, 2, 3 \\ (d_R^c, L_L) & (Q_L, u_R^c, e_R^c) \end{array}$$

In the absence of masses, symmetric under $SU(3)_{\bar{5}} \times SU(3)_{10} \times SU(3)_1$

Include symmetry breaking (here with one higgs):

$$\lambda_5^{ij} \psi_i^T \chi_j H_5^* + \lambda_{10}^{ij} \chi_i^T \chi_j H_5 \quad \text{gives bad mass relations for light families}$$

$$\lambda_u \propto \lambda_{10}, \lambda_d \propto \lambda_e^T \propto \lambda_5$$

$$\frac{1}{M} (\lambda'_5)^{ij} \psi_i^T \Sigma \chi_j H_{\bar{5}} \quad \Sigma \sim \mathbf{24}; M \text{ large; freedom to fix mass relations}$$

$$\lambda_u \propto \lambda_{10}, \lambda_d \propto (\lambda_5 + \epsilon \lambda'_5), \lambda_e^T \propto (\lambda_5 - \frac{3}{2} \epsilon \lambda'_5), \epsilon = M_{\text{GUT}}/M$$

$$\lambda_1^{ij} N_i^T \psi_j H_5 + M_R^{ij} N_i^T N_j \quad \text{neutrino masses (Dirac+Majorana)}$$

| | | | |
|------------------------------------|-------------------------------------|--|--|
| | $Q_L \rightarrow V_{10} Q_L$ | $\lambda_{10} \rightarrow V_{10}^* \lambda_{10} V_{10}^\dagger$ | <div style="border: 1px solid black; padding: 5px; margin-bottom: 10px;">connect lepton to quark MFV</div> |
| spurion transformation laws: | $u_R \rightarrow V_{10}^* u_R$ | $\lambda_5 \rightarrow V_{\bar{5}}^* \lambda_5 V_{10}^\dagger$ | |
| | $d_R \rightarrow V_{\bar{5}}^* d_R$ | $\lambda'_5 \rightarrow V_{\bar{5}}^* \lambda'_5 V_{10}^\dagger$ | |
| | $L_L \rightarrow V_{\bar{5}} L_L$ | $\lambda_1 \rightarrow V_1^* \lambda_1 V_{\bar{5}}^\dagger$ | |
| | $e_R \rightarrow V_{10}^* e_R$ | $M_R \rightarrow V_1^* M_R V_1^\dagger$ | |

get old mixing structures (to be included in composite operators), like

$$\begin{array}{ll} \text{quarks:} & \bar{Q}_L \lambda_u^\dagger \lambda_u Q_L, \quad \bar{d}_R \lambda_d^\dagger \lambda_u^\dagger \lambda_u Q_L \\ \text{leptons:} & \bar{L}_L \lambda_1^\dagger \lambda_1 L_L, \quad \bar{e}_R \lambda_e^\dagger \lambda_1^\dagger \lambda_1 L_L \end{array}$$

but also get interesting new ones, like

$$\begin{array}{ll} \text{quarks:} & \bar{Q}_L (\lambda_e \lambda_e^\dagger)^T Q_L, \\ & \bar{d}_R \lambda_e^T (\lambda_e \lambda_e^\dagger)^T Q_L, \quad \bar{d}_R (\lambda_e \lambda_1^\dagger \lambda_1)^T Q_L, \\ & \bar{d}_R (\lambda_e^\dagger \lambda_e)^T d_R, \quad \bar{d}_R (\lambda_1^\dagger \lambda_1)^T d_R, \\ \text{leptons:} & \bar{L}_L (\lambda_d \lambda_d^\dagger)^T L_L, \\ & \bar{e}_R (\lambda_d \lambda_d^\dagger \lambda_d)^T L_L, \quad \bar{e}_R \lambda_u \lambda_u^\dagger \lambda_d^T L_L, \\ & \bar{e}_R \lambda_u \lambda_u^\dagger e_R, \quad \bar{e}_R (\lambda_d^\dagger \lambda_d)^T e_R, \end{array}$$

going over to quark-lepton mass basis, introduce two new mixing matrices $C = V_{e_R}^T V_{d_L}$, $G = V_{e_L}^T V_{d_R}$

so get, for example

$$\begin{array}{ll} \bar{e}_R \lambda_u \lambda_u^\dagger e_R & \bar{e}_R [C \Delta^{(q)} C^\dagger]^* e_R \\ \bar{e}_R \lambda_u \lambda_u^\dagger \lambda_d^T L_L & \longrightarrow \bar{e}_R [C \Delta^{(q)} \bar{\lambda}_d G^\dagger]^* e_L \\ \bar{e}_R \lambda_u \lambda_u^\dagger \lambda_e L_L & \bar{e}_R [C \Delta^{(q)} C^\dagger]^* \bar{\lambda}_e e_L \end{array}$$

$$\text{where } \Delta_{ij}^{(q)} \equiv V_{\text{CKM}}^\dagger \bar{\lambda}_u^2 V_{\text{CKM}} = \frac{m_t^2}{v^2} (V_{\text{CKM}})_{3i}^* (V_{\text{CKM}})_{3j} + \mathcal{O}(m_{c,u}^2/m_t^2)$$

quick example (probably out of time by now):

$$\tau \rightarrow \mu\gamma, \quad \tau \rightarrow e\gamma \quad \& \quad \mu \rightarrow e\gamma$$

$$\Delta\mathcal{L}_{\text{eff}} = \frac{v}{\Lambda^2} \bar{e}_R \left[c_1 \lambda_e \lambda_1^\dagger \lambda_1 + c_2 \lambda_u \lambda_u^\dagger \lambda_e + c_3 \lambda_u \lambda_u^\dagger \lambda_d^T \right] \sigma^{\mu\nu} e_L F_{\mu\nu}$$

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just like pure MLFV

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just like pure MLFV

Generalizes Barbieri & Hall ($\lambda'_5 = 0, C = G = 1$)

New mixing structures

Independent of M_ν

Hierarchical

Large: for $\Lambda=10\text{TeV}$

$$\text{Br}(\mu \rightarrow e\gamma) \sim 10^{-12}$$

$$C = V_{e_R}^T V_{d_L}$$

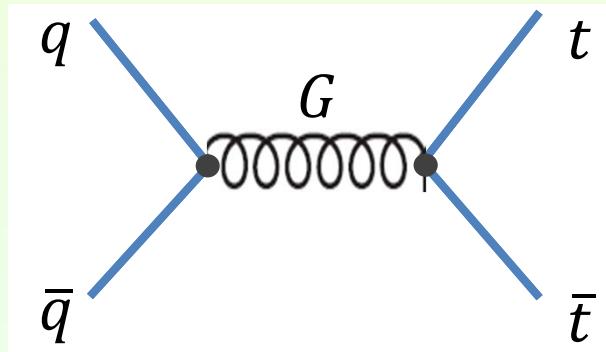
$$G = V_{e_L}^T V_{d_R}$$

$$\left(\frac{m_t^2}{v^2} \right) \times \begin{cases} \lambda^2(m_\tau/v), & (\tau \rightarrow \mu) \\ \lambda^3(m_\tau/v), & (\tau \rightarrow e) \\ \lambda^5(m_\mu/v), & (\mu \rightarrow e) \end{cases}$$

$$(\lambda = 0.22)$$

(is the Cabibbo angle!)

Flavor Physics and FB asymmetry in top production at Tevatron



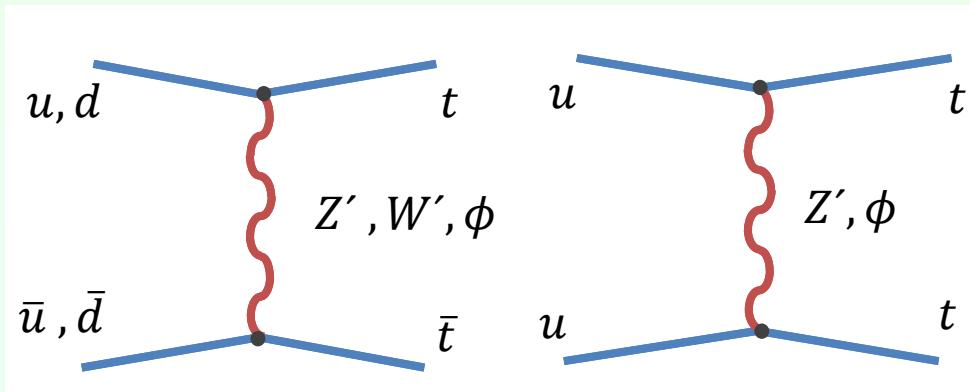
s-channel exchange models

[Marques Tavares, Schmalz / Barcelo, Carmona, Masip, Santiago / Ferrario, Rodrigo / Frampton, Shu, Wang / Djouadi, Richard / Bauer, Goertz, Haisch, Pfoh, Westhoff / Bai, Hewett, Kaplan, Rizzo / Zerwekh / Hewett, Shelton, Spannowsky, Tait, Takeuchi / Haisch, Westhoff / Aguilar-Saavedra, Perez-Victoria, ...]

G is color octet for LO interference with QCD

Need axial coupling; “axigluon.” For positive asymmetry and heavy G need $\text{sign}(g^q g^t) = -1$: vector-axial couplings non-flavor-universal.

Light G : suppressed light- q couplings (from dijets)



t-channel exchange models

[Jung, Murayama, Pierce, Wells / Cheung, Keung, Yuan / Cao, Heng, Wu, Yang / Barger, Keung, Yu / Cao, McKeen, Rosner, Saughnessy, Wagner / Berger, Cao, Chen, Li, Zhang / Bhattacherjee, Biswal, Ghosh / Zhou, Wang, Zhu / Aguilar-Saavedra, Perez-Victoria / Buckley, Hooper, Kopp, Neil / Rajaraman, Surujon, Tait / Duraisamy, Rashed, Datta / Shu, Tait, Wang / Cao, Heng, Wu, Yang / Dorsner, Faifer, Kamenik, Kosnik / Jung, Ko, Lee, Nam, Aguilar-Saavedra, Perez-Victoria / Patel, Sharma / Ligeti, Marques Tavares, Schmalz, ...]

- A large FB asymmetry requires large flavor violating couplings
- Like sign tt, di-jets, single top, very constrained at Tevatron and LHC

All models require non-trivial flavor interactions.

Natural implementation: Minimal Flavor Violating Fields, rich phenomenology [BG, Kagan, Trott, Zupan]

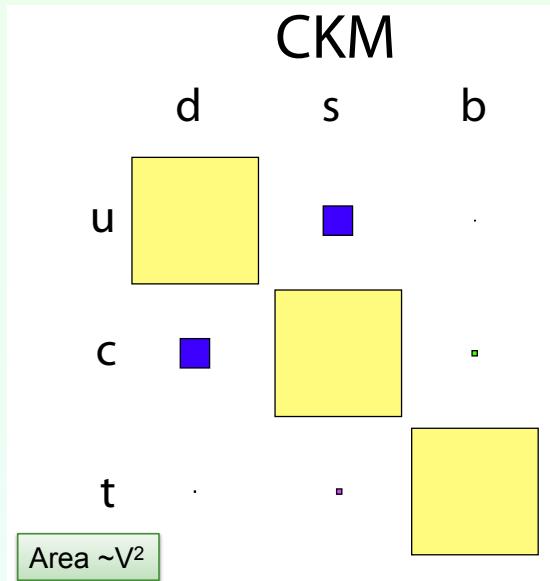
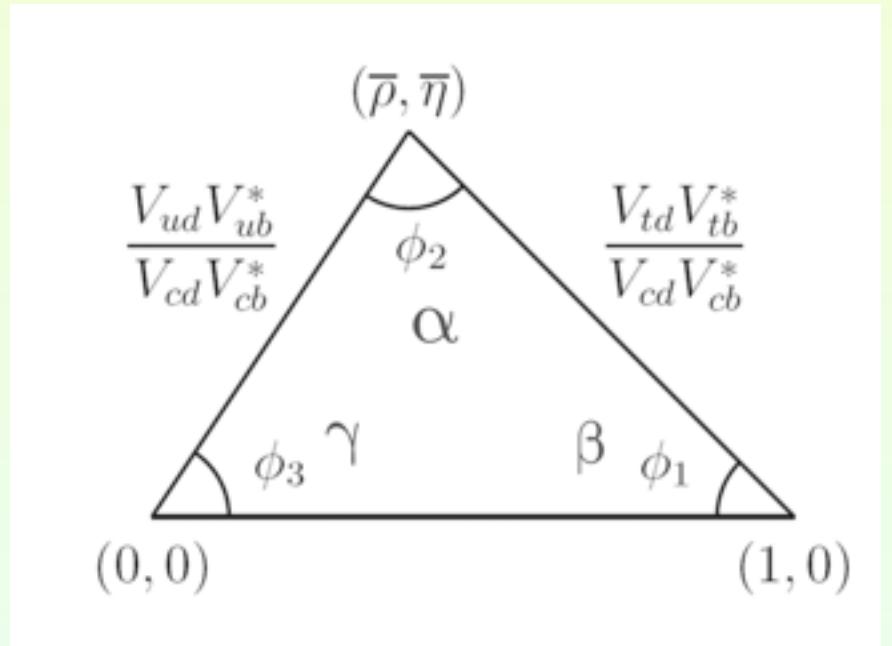
Conclusions

- Flavor physics in quark sector strongly constrains BSM/NP models
- Expect that any complete theory of flavor connects quark and lepton sectors
- In absence of direct evidence for new resonances, generic model independent analysis is valuable
- MFV:
 - Simplest way of relaxing bounds on scale of NP
 - Naturally arising (or to good approximation) in many popular models
 - Extensible to leptons/GUTs
 - Addresses flavor in top-quark-FB-asymmetry
- Gauged flavor models “explain:” number of generations
 - Do not address patterns of masses and mixings
 - MFV? Very nonlinearly
- Plethora of models for patterns of masses and mixings
 - But many only in lepton sector
 - Do not address number of generations (combine with gauged G_F ?)
- Still far from a “theory of flavor”

The End

More slides

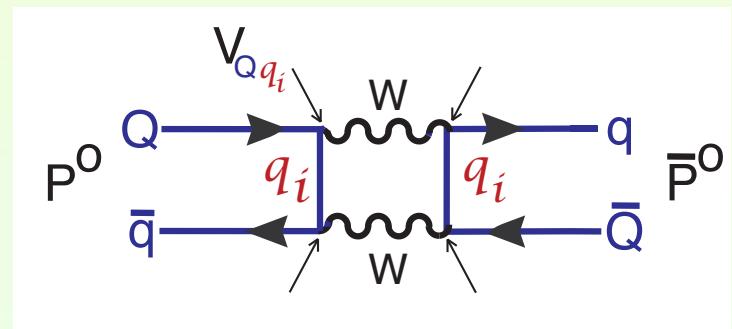
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



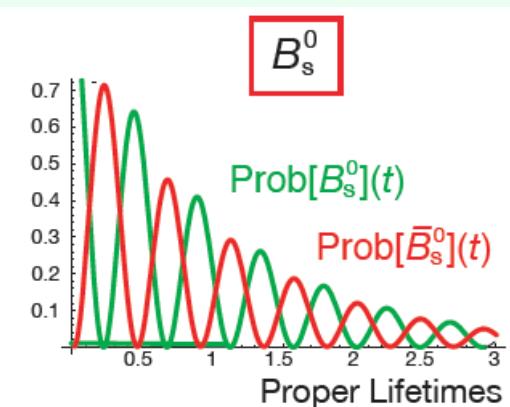
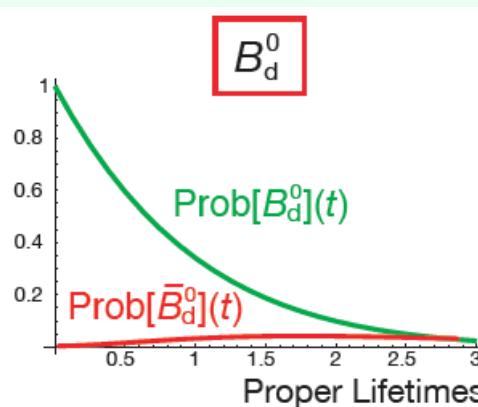
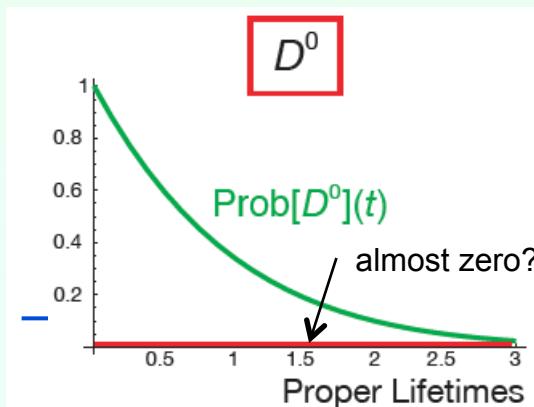
$$= \begin{bmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{bmatrix}.$$

CPV in Mixing

- In SM neutral pseudoscalar P^0 can mix into antiparticle via box diagram
- Mixing rate depends on



- Mass of internal quark larger for heavier quark
- CKM factors V_{ij}
- Largest for B_s since t -quark is not suppressed by CKM



Mixing Theory

Effective two state system:

$$i \frac{d}{dt} \begin{pmatrix} P^0 \\ \bar{P}^0 \end{pmatrix} = H_{\text{eff}} \begin{pmatrix} P^0 \\ \bar{P}^0 \end{pmatrix} \quad H_{\text{eff}} = M - \frac{i}{2}\Gamma \quad M^\dagger = M, \quad \Gamma^\dagger = \Gamma$$

$$\text{CPT: } H_{\text{eff}\,11} = H_{\text{eff}\,22}$$

$$\text{diagonalize: } |P_L\rangle = p|P^0\rangle + q|\bar{P}^0\rangle \quad |P_H\rangle = p|P^0\rangle - q|\bar{P}^0\rangle$$

$$\text{define: } \bar{M} = \frac{M_H + M_L}{2} \quad \Delta M = M_H - M_L \approx 2|M_{12}| \left(1 - \frac{|\Gamma_{12}|^2}{8|M_{12}|^2} \sin^2 \phi_{12} \right)$$

$$\bar{\Gamma} = \frac{\Gamma_H + \Gamma_L}{2} \quad \Delta\Gamma = \Gamma_H - \Gamma_L \approx 2|\Gamma_{12}| \cos \phi_{12} \left(1 + \frac{|\Gamma_{12}|^2}{8|M_{12}|^2} \sin^2 \phi_{12} \right)$$

$$\phi_{12} = \arg(-M_{12}/\Gamma_{12})$$

$$\text{compute, eg: } \left(\frac{q}{p} \right) = \frac{\Delta M + \frac{i}{2}\Delta\Gamma}{2(M_{12} - \frac{i}{2}\Gamma_{12})}$$

Flavor Specific: a_{sl}

- Definition
$$a_{sl} = \frac{\Gamma(\bar{P} \rightarrow f) - \Gamma(P \rightarrow \bar{f})}{\Gamma(\bar{P} \rightarrow f) + \Gamma(P \rightarrow \bar{f})}$$

where $\Gamma(\bar{P} \rightarrow f)(t=0) = 0 = \Gamma(P \rightarrow \bar{f})(t=0)$

- Flavor specific means $\bar{f} \neq f$
 - $B_s \rightarrow D^+ \mu^- \bar{\nu}_\mu$ vs $\bar{B}_s \rightarrow D^- \mu^+ \nu_\mu$
 - Or same sign dileptons: one meson mixes and decays, the other decays without mixing: $\mu^+ \mu^+$ vs $\mu^- \mu^-$
- In SM
$$a_{sl} = \frac{|p/q|^2 - |q/p|^2}{|p/q|^2 + |q/p|^2} \approx \frac{\Delta\Gamma}{\Delta M} \tan \phi_{12}$$

so it is very small in SM,

$$\overrightarrow{B^0} a_{sl}^d = -4.1 \times 10^{-4}, \quad a_{sl}^s = 1.9 \times 10^{-5}$$

40 

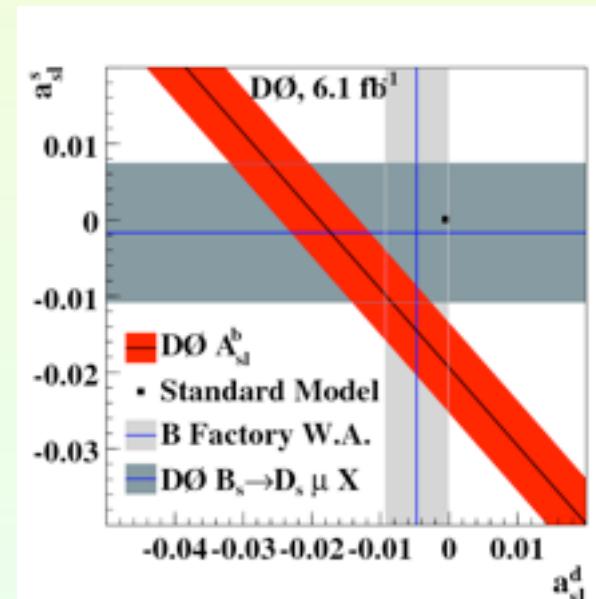
[A. Lenz, Moriond 2012]

a_{sl} : D0, from di-muons

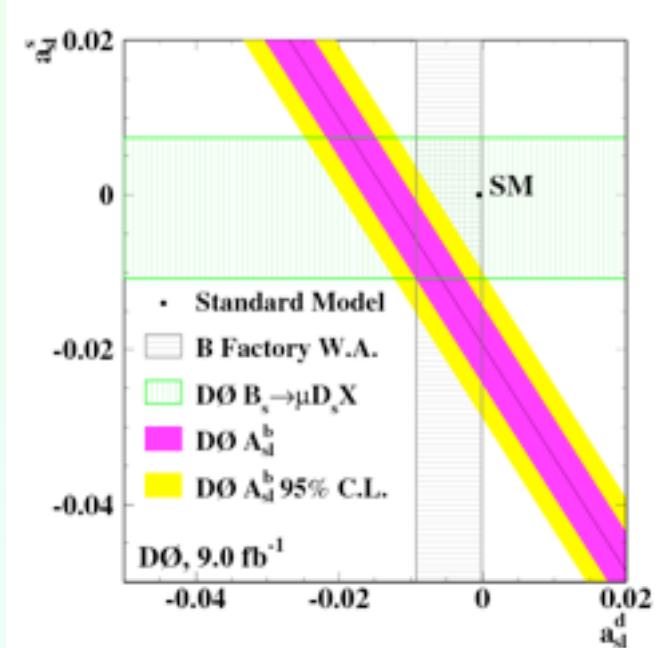
- Dimuons
- $a_{sl}^b = (-0.787 \pm 0.172(\text{stat}) \pm 0.093(\text{syst}))\%$
combined for d and s
- 3.9σ deviation from SM
- Also use IP (impact parameter)
to separate d from s

$$a_{sl}^d = (-0.12 \pm 0.52)\%,$$

$$a_{sl}^s = (-1.81 \pm 1.06)\%.$$



[Phys.Rev. D82 (2010) 032001]



[Phys.Rev. D84 (2011) 052007]

a_{sl} : D0, from semileptonic

[arXiv:1207.1769]

[Phys. Rev. D86, 072009 (2012)]

- New this year (Jul 7, Aug 29)

- $\frac{\Gamma(\bar{B}^0 \rightarrow B^0 \rightarrow \ell^+ D^{(*)-} X) - \Gamma(B^0 \rightarrow \bar{B}^0 \rightarrow \ell^- D^{(*)+} X)}{\Gamma(\bar{B}^0 \rightarrow B^0 \rightarrow \ell^+ D^{(*)-} X) + \Gamma(B^0 \rightarrow \bar{B}^0 \rightarrow \ell^- D^{(*)+} X)},$

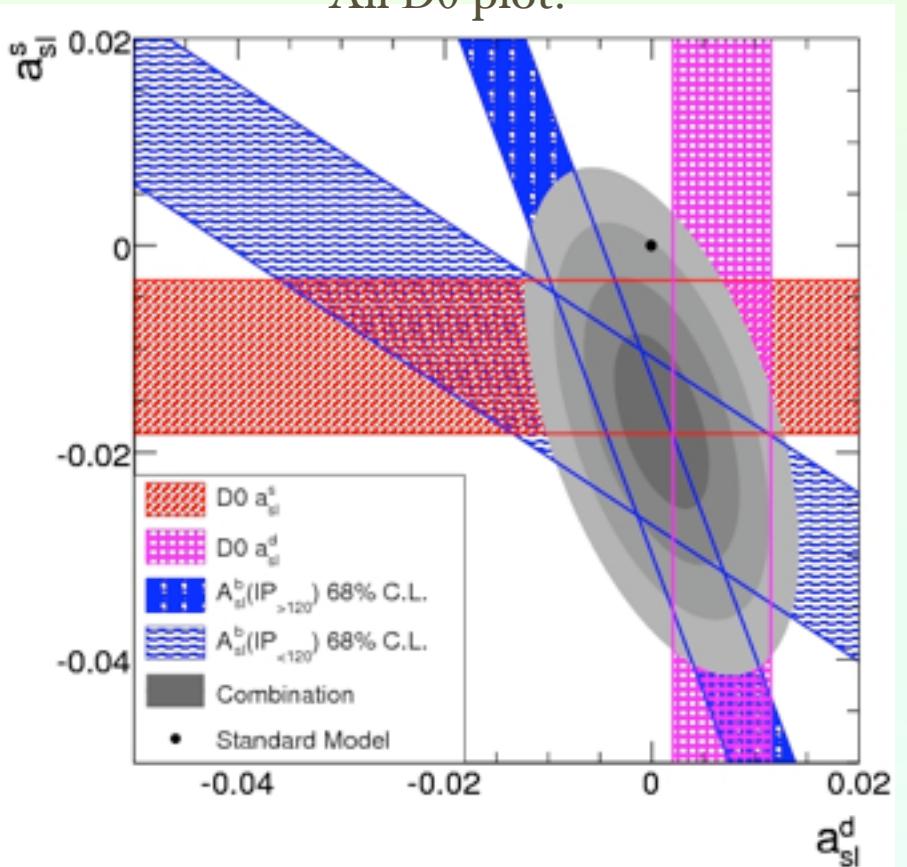
with 2 decay channels:

1. $B^0 \rightarrow \mu^+ \nu D^- X,$
with $D^- \rightarrow K^+ \pi^- \pi^-$
(plus charge conjugate process);
2. $B^0 \rightarrow \mu^+ \nu D^{*-} X,$
with $D^{*-} \rightarrow \bar{D}^0 \pi^-, \bar{D}^0 \rightarrow K^+ \pi^-$
(plus charge conjugate process);

(idem for B_s)

- $a_{sl}^d = [0.68 \pm 0.45 \text{ (stat.)} \pm 0.14 \text{ (syst.)}] \%$

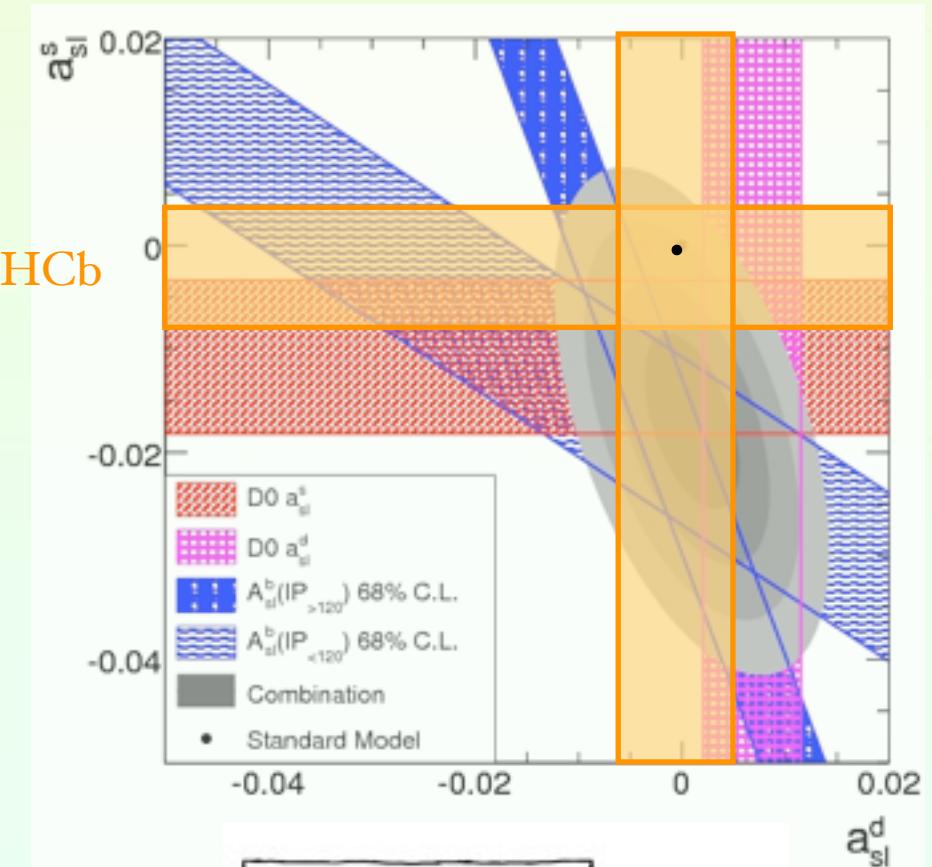
All D0 plot:



$a_{sl}^s = [-1.08 \pm 0.72 \text{ (stat)} \pm 0.17 \text{ (syst)}] \%$

a_{sl} : rest of the world

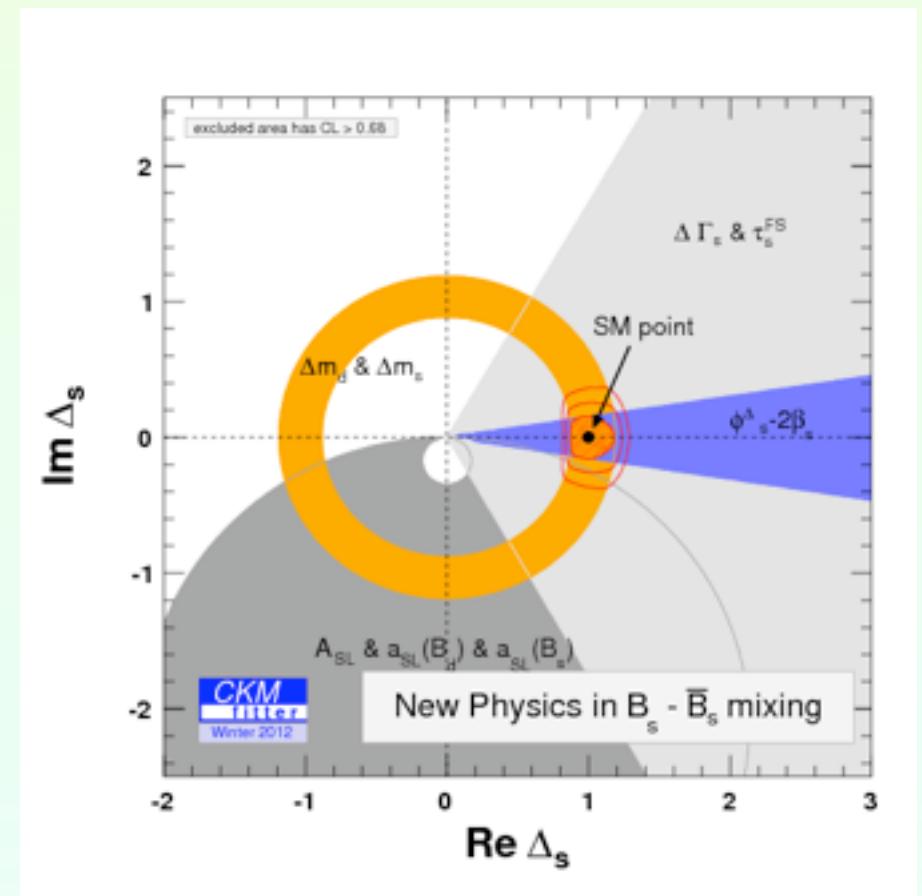
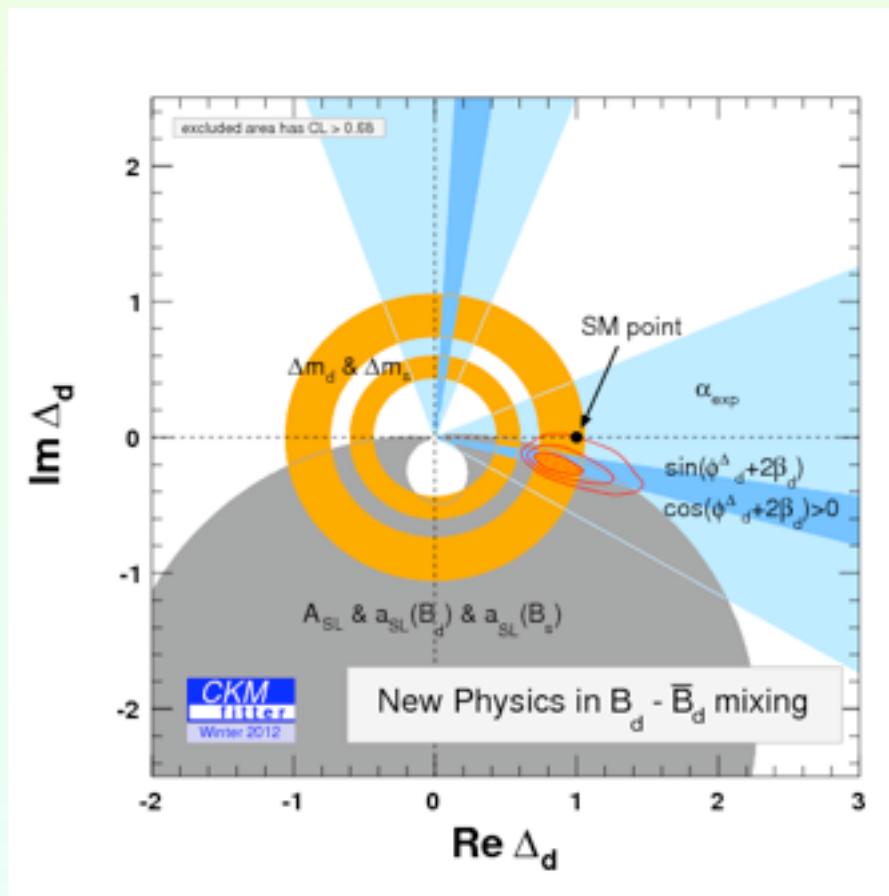
- LHCb [PLB713(2012)186]
 $a_{sl}^s = (-0.24 \pm 0. \pm 0.33)\%$
- B-factories combined
 $a_{sl}^d = (-0.05 \pm 0.56)\%$
- Superimposed on D0 plot, for comparison
- Consistent with SM
- Will have to wait for more (more precise) data (not Tevatron)



a_{sl} :summary

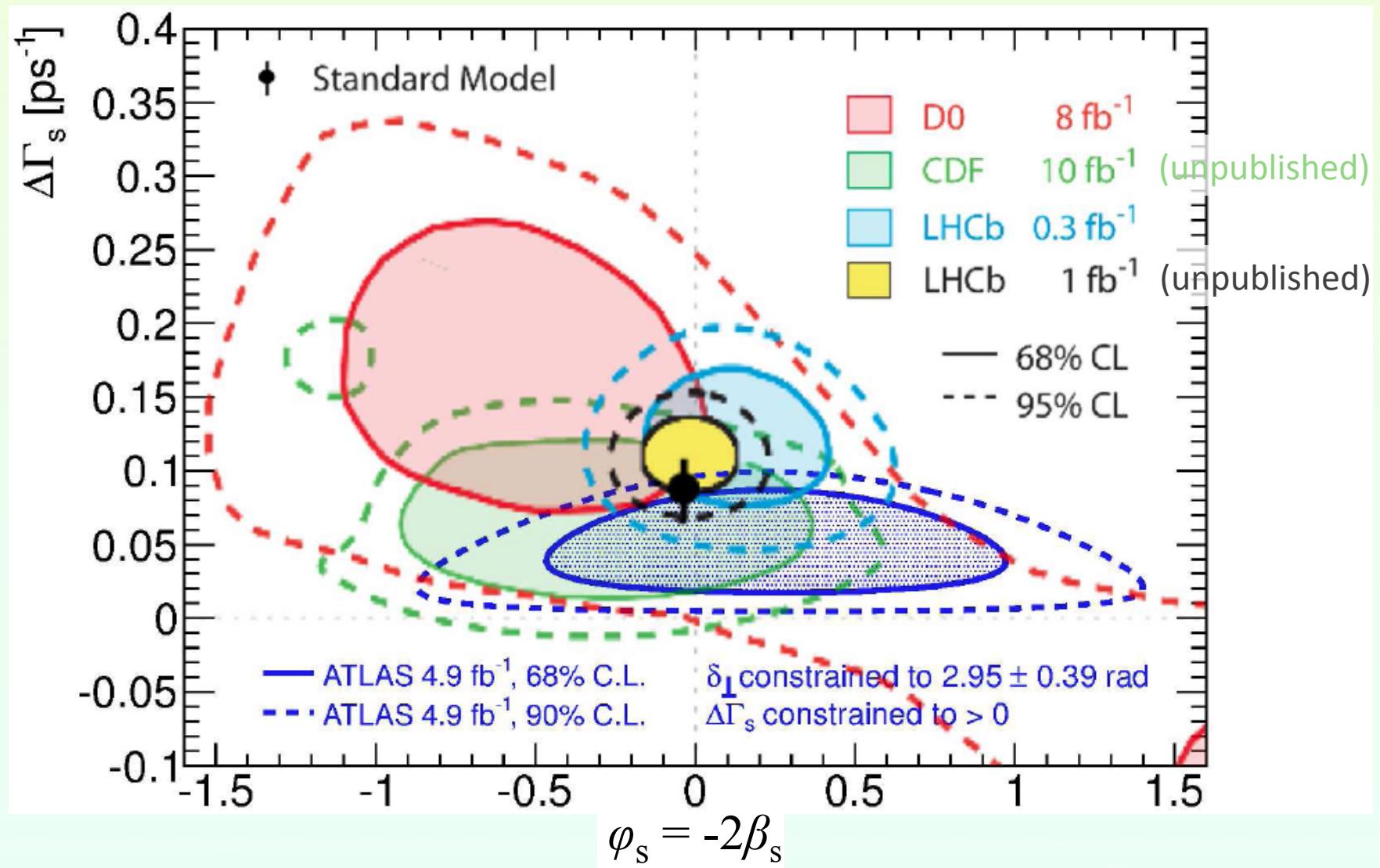
Characterize NP by

$$M_{12}^q = M_{12}^{q,\text{SM}} \Delta_q$$



(does not include new LHCb result)

Combined fit to polarization, widths and angles in $B \rightarrow \psi\phi(K^+K^-)$
gives widths and angles:

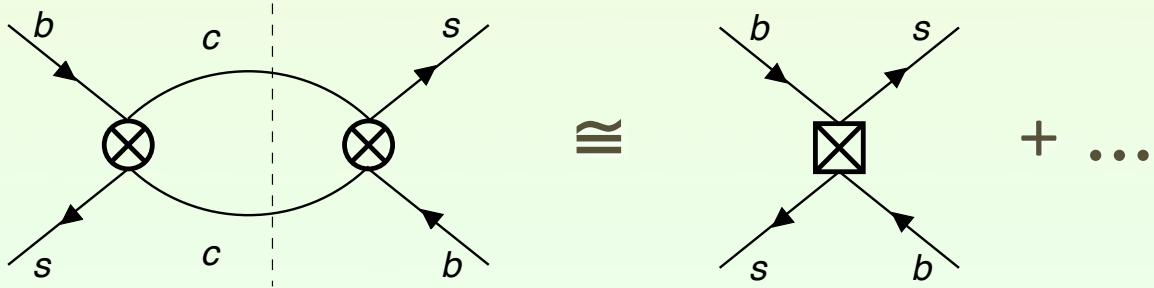


Long Digression

Can we compute Γ (let alone $\Delta\Gamma$)?

- Standard lore: use OPE

- OPE: expansion in $1/m_b$



- Normally:

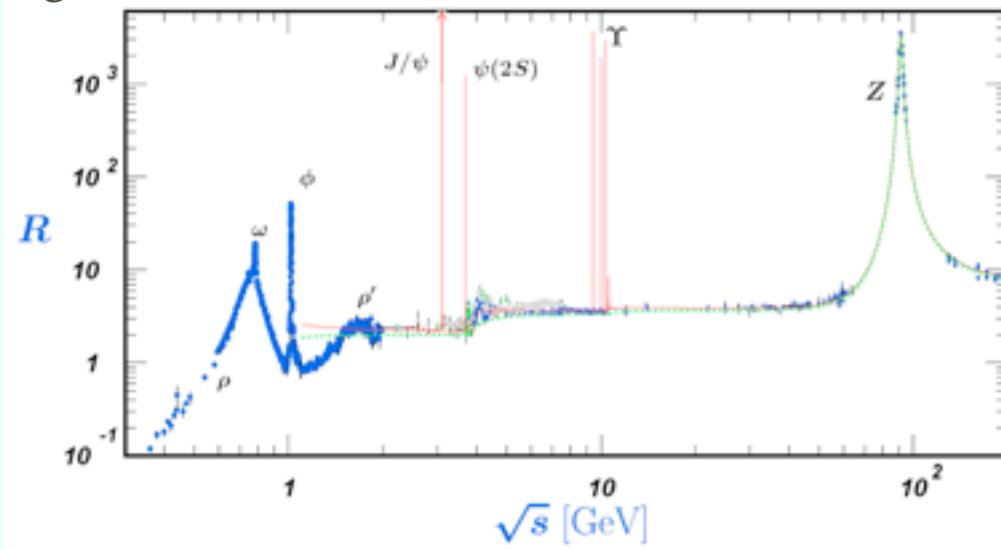
- OPE valid in “deep Euclidean region”
- Use dispersion relation to relate to physical region
- Result in integral over all energies in physical region
- Duality: replace integral over all energies by smearing over domain
- Duality works if smearing over large enough region:
 - Include large number of resonances
 - Smooth regions dominate

[Lenz & Nierste, eg: JHEP 0706 (2007) 072]

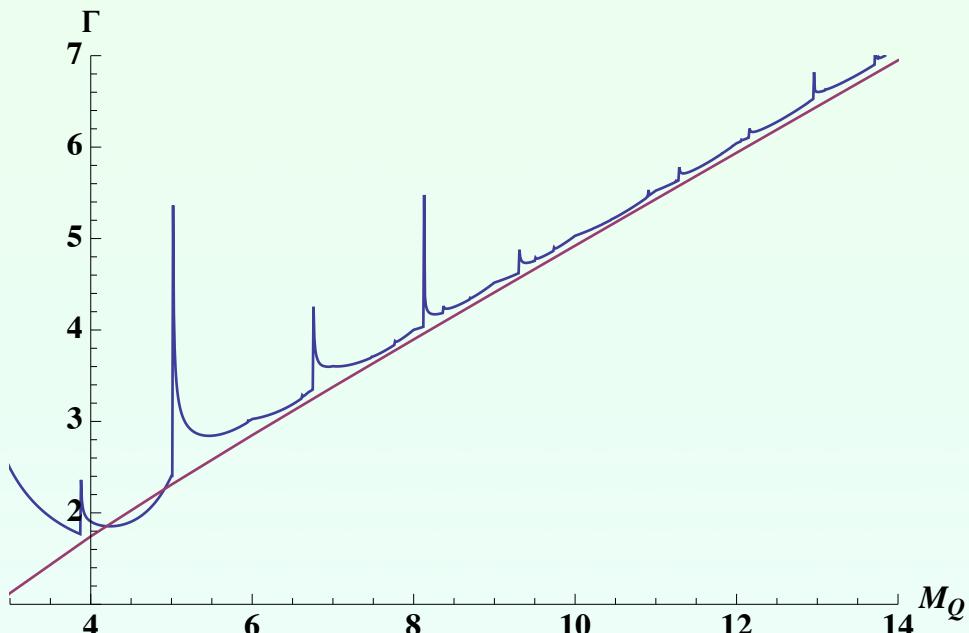
Poggio-Quinn-Weinberg:

$$\bar{\sigma}(s) = \frac{1}{2i} (\Pi(s + i\Delta) - \Pi(s - i\Delta))$$

can use OPE for Π if Δ is large enough



- For B decay we cannot smear (integrate) over quark masses
- Neither can we compute for “deep euclidean” mass
- Maybe duality works if mass is large enough (large number of decay channels)?
- Test the idea by applying it to soluble model:
QCD in 2-dims at large N_c (the ‘t Hooft model)



- Spikes from phase space at thresholds
- Constant difference between “exact” and perturbative: order $(1/M_Q)^0$

$$\Gamma(B) = \Gamma(Q)(1 + 0.14/M_Q)$$

- Smearing will turn the finite difference into one that decreases with $1/M_Q$
- Q: how can this averaging procedure turn a constant difference into one that decreases as $(1/M_Q)^1$?
- Go back to e+e-

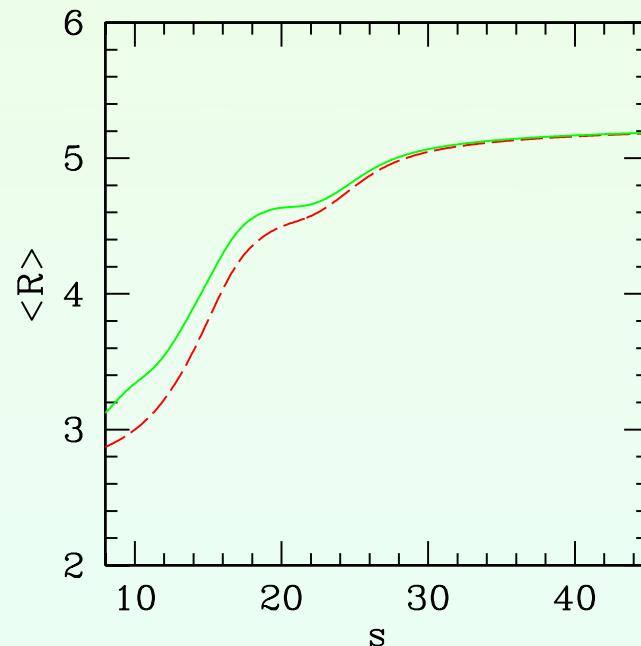
Effect of including narrow resonances in lorentzian smearing:

$$\bar{\sigma}(s) = \frac{\Delta}{\pi} \int_0^\infty ds' \frac{\sigma(s')}{(s' - s)^2 + \Delta^2}$$

red: PQW (exclude resonances)

green: include resonances

NOTE: very slow approach to duality,
effect of resonances significant in resonant region



- Lorentzian smearing

$$\frac{1}{((x - M_Q)^2 + 1)^n}$$

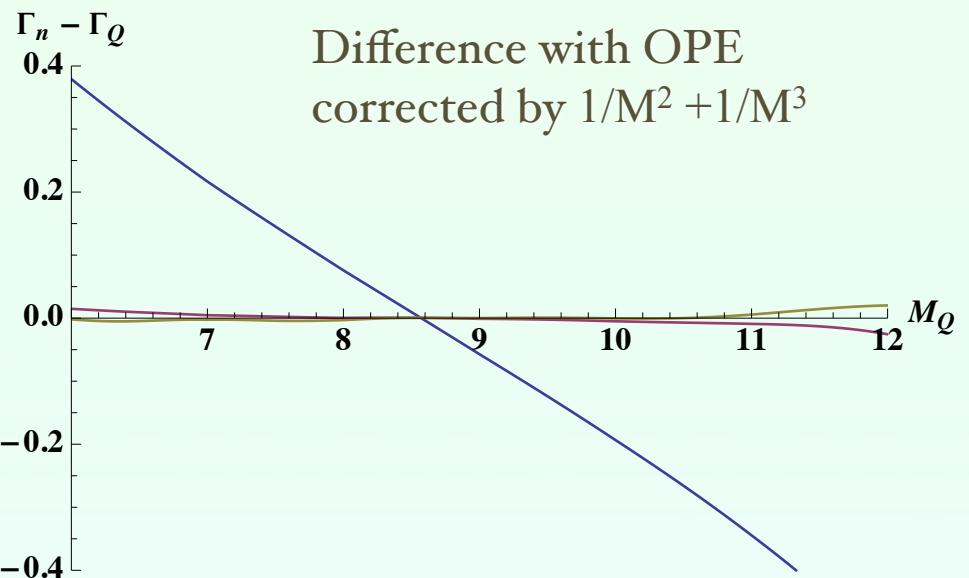
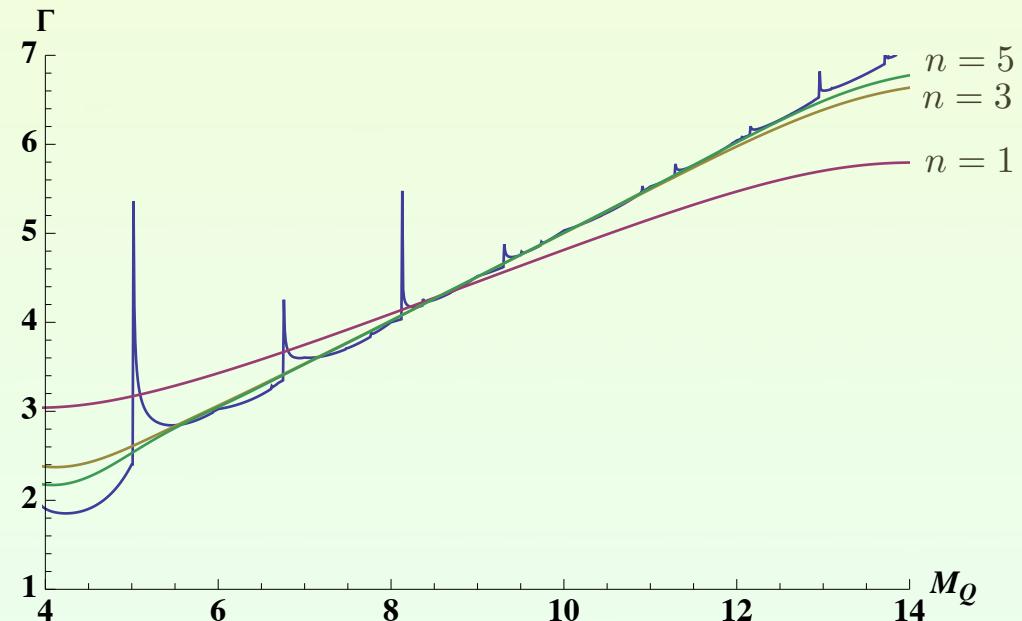
- Justified by OPE provided

$$n \geq 2$$

- Corrections to OPE:

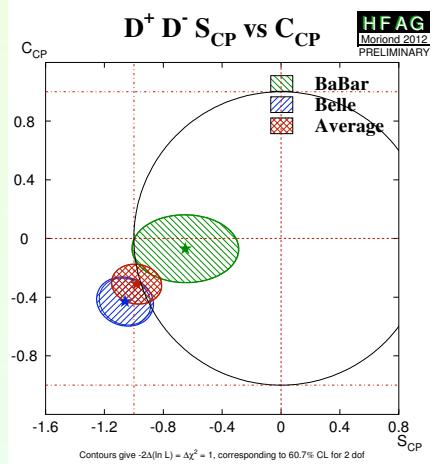
order $\frac{1}{M_Q^2}$

- I conclude:
Cannot trust OPE for width
unless asymptotically heavy quark



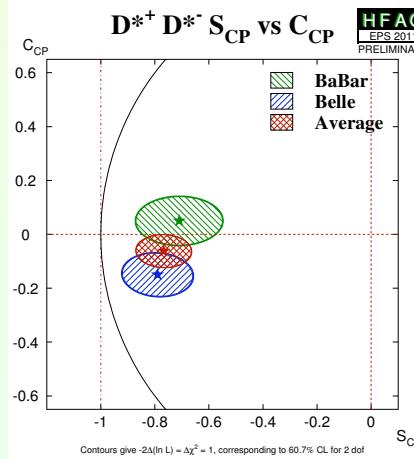
End Long Digression

$b \rightarrow ccd$ modes $B^0 \rightarrow D^+D^-$
 CP-eigenstate
 $\mathcal{S} = \sin 2\phi_1, \mathcal{A} = 0$
 if negligible penguin

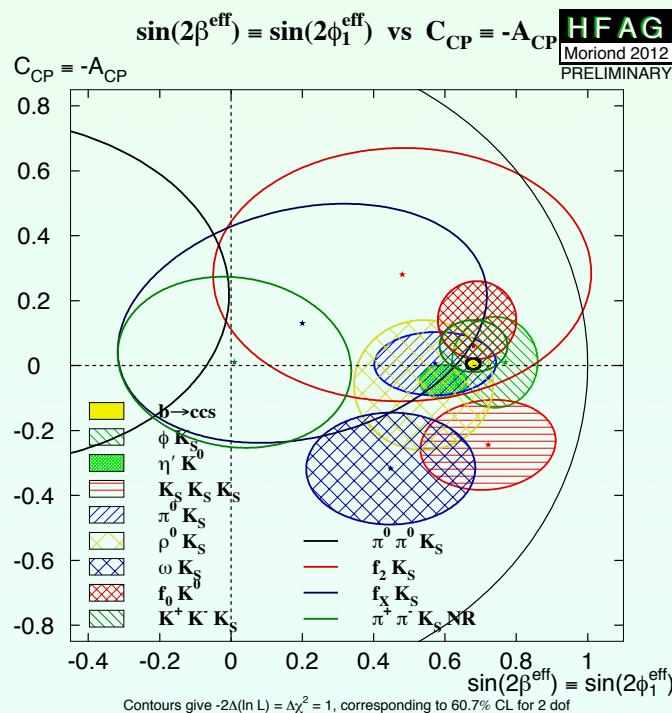


$B^0 \rightarrow D^{*+}D^{*-}$
 mix of CP-odd/even
 \mathcal{S}, \mathcal{A} for each of
 longitudinal / transverse

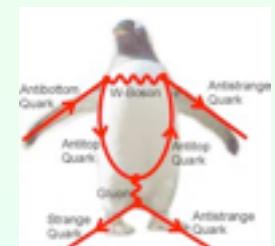
$B^0 \rightarrow D^\pm D^{*\mp}$
 Not a CP-eigenstate
 2 amplitudes × 2 modes
 $\Rightarrow C, \mathcal{S}, \mathcal{A}, \Delta\mathcal{S}, \Delta\mathcal{A}$



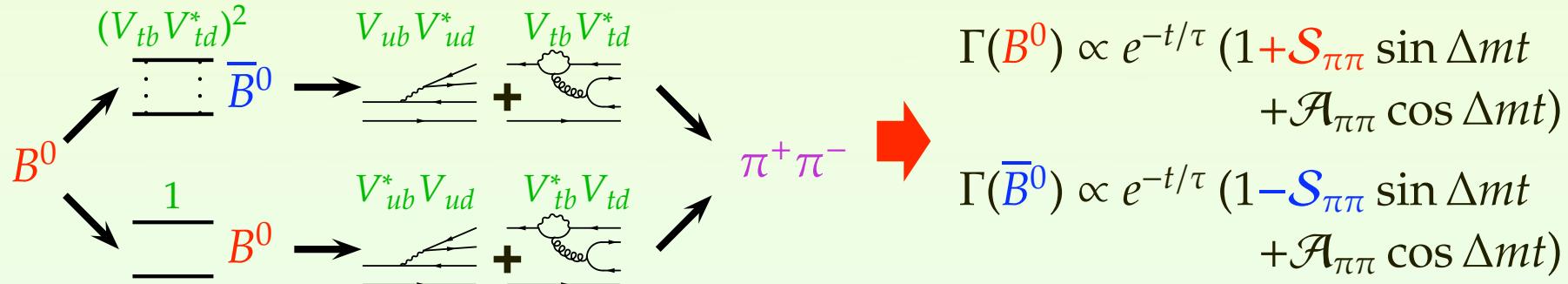
$b \rightarrow s$ penguin modes



- No sign of deviations from standard CKM
- Many of these new: expect improvement in next generation



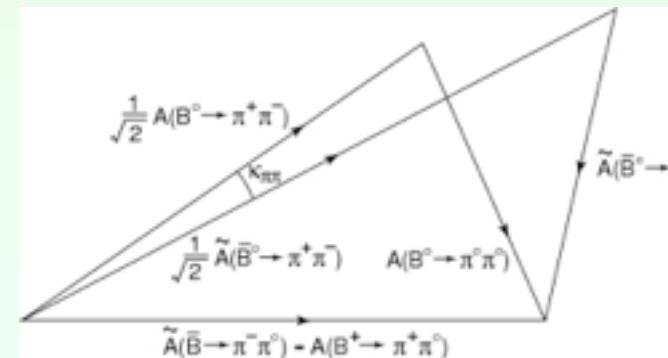
α/ϕ_2 and Penguin Pollution



$$\mathcal{S}_{\pi\pi} = \sqrt{1 - \mathcal{A}_{\pi\pi}^2} \sin 2\phi_2^{\text{eff}}, \text{ where } \phi_2^{\text{eff}} = (\phi_2 + \kappa) \text{ is not } \phi_2$$

[BG Phys.Lett. B229 (1989) 280]

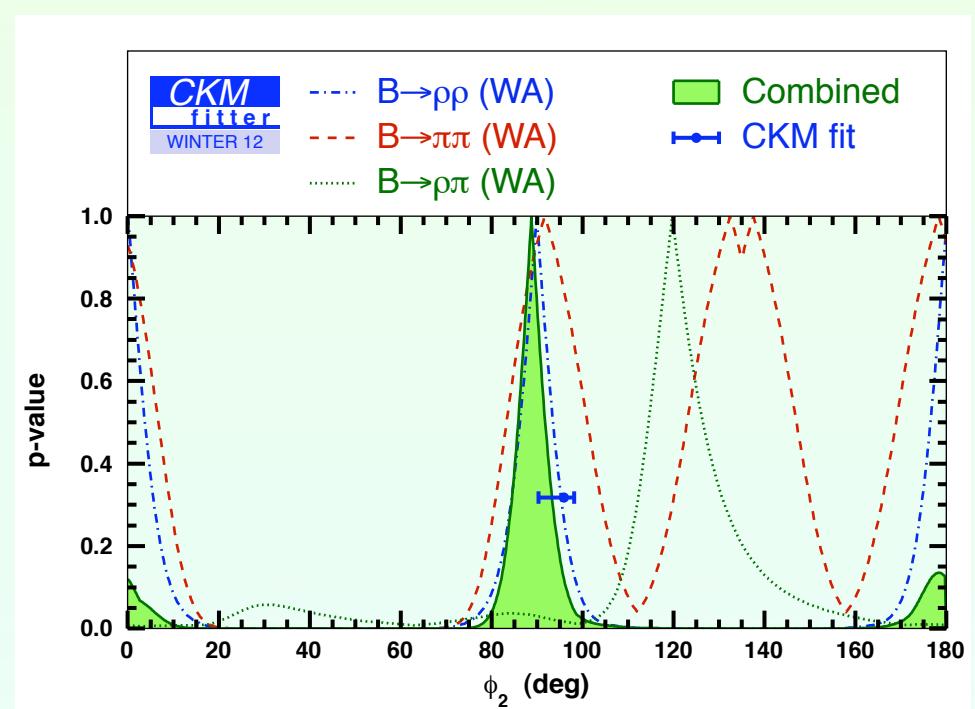
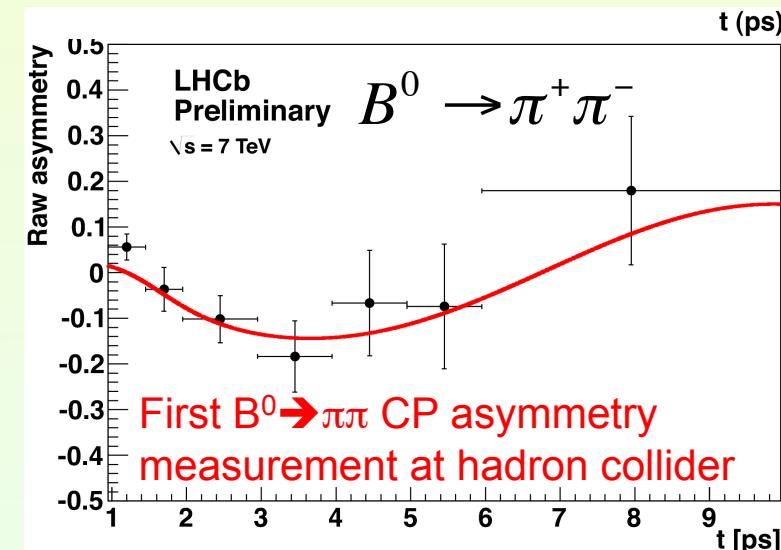
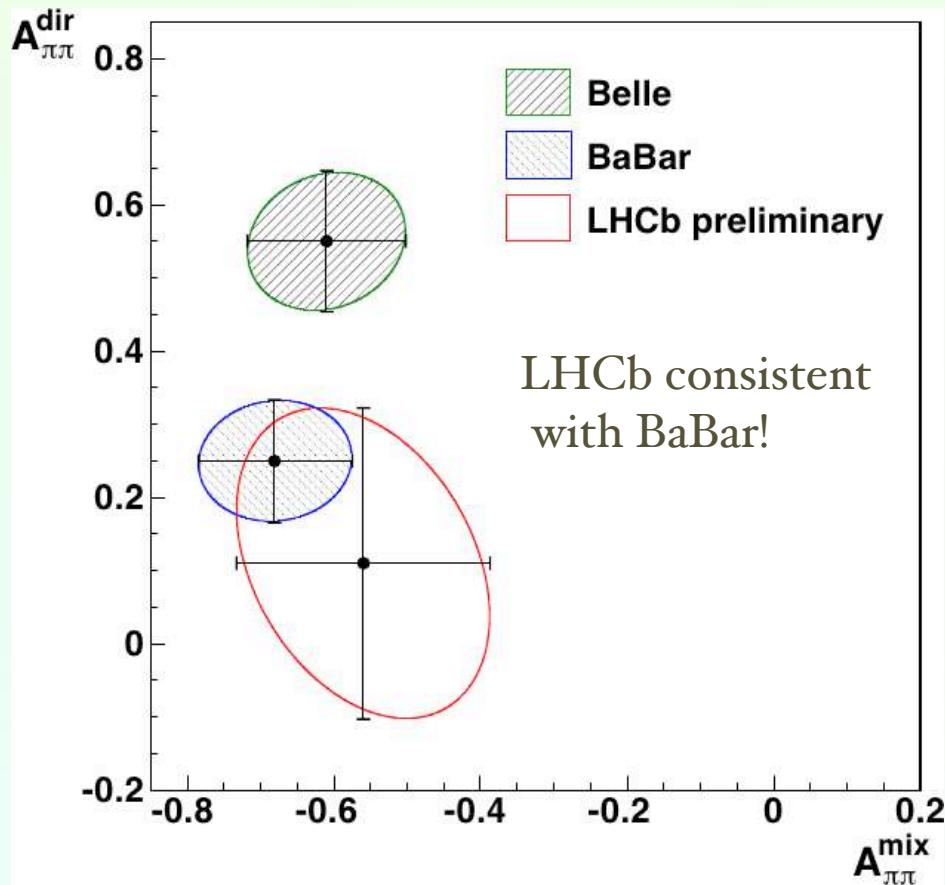
- Isospin analysis [Gronau-London PRL65,3381(1990)]
 - Relations with $B \rightarrow \pi^+\pi^0$ and $B^0 \rightarrow \pi^0\pi^0$ (same for $B \rightarrow \rho\rho$ after resolving polarization)
 - Isospin breaking effects are small
- Time-dependent Dalitz analysis [Snyder-Quinn PRD48,2139(1993)]
 - $B^0 \rightarrow \pi^+\pi^-\pi^0$ contains $\rho^+\pi^-$, $\rho^-\pi^+$, $\rho^0\pi^0$ and cross terms (interference)
 - α/ϕ_2 directly determined, $\rho^\pm\pi^0$ and $\rho^0\pi^\pm$ may improve further (future)



NEW form LHCb
[Paul Soler ICHEP 2012]

$$\mathcal{S}_{\pi\pi} = A_{\pi\pi}^{\text{mix}} = 0.56 \pm 0.17 \pm 0.03$$

$$\mathcal{A}_{\pi\pi} = A_{\pi\pi}^{\text{dir}} = 0.11 \pm 0.21 \pm 0.03$$



$\phi_2 / \alpha = (88.7^{+4.6}_{-4.2})^\circ$
[CKMfitter Moriond2012]

Direct CPV

$D^0 \rightarrow K^+K^-$ and $\pi^+\pi^-$

[BG & Golden, Phys.Lett. B₂₂₂ (1989) 501]

$$A \equiv \frac{\Gamma(D^+ \rightarrow \mathcal{P}\bar{\mathcal{P}}) - \Gamma(D^- \rightarrow \bar{\mathcal{P}}\mathcal{P})}{\Gamma(D^+ \rightarrow \mathcal{P}\bar{\mathcal{P}}) + \Gamma(D^- \rightarrow \bar{\mathcal{P}}\mathcal{P})} = \frac{2 \operatorname{Im}(a^*b) \operatorname{Im}(\Sigma^*\Delta)}{|a|^2 |\Sigma|^2 + |b|^2 |\Delta|^2 + 2 \operatorname{Re}(a^*b) \operatorname{Re}(\Sigma^*\Delta)}$$

where $\mathcal{A}(D \rightarrow \mathcal{P}\bar{\mathcal{P}}) = a\Sigma + b\Delta$

$$\Sigma = \frac{1}{2}(V_{cs}^* V_{us} - V_{cd}^* V_{ud}), \quad \Delta = \frac{1}{2}(V_{cs}^* V_{us} + V_{cd}^* V_{ud})$$

$$|\Sigma| \sim \lambda \gg |\Delta| \sim \lambda^5$$

SU(3) analysis: five invariant amplitudes

$$\begin{aligned} \langle [8]_j^i | [\bar{6}]_{kl} | D_r \rangle &= S \mathcal{T}_{jklr}^i, & \langle [8]_j^i | [15_M]_m^{kl} | D_r \rangle &= E \mathcal{T}_{jmrl}^{ikl}, & \langle [27]_{kl}^i | [15_M]_p^{mn} | D_r \rangle &= T \mathcal{T}_{klpr}^{ijmn}, \\ \langle [8]_j^i | [3]^k | D_r \rangle &= F \mathcal{T}_{jr}^{ik}, & \langle [1] | [3]^i | D_r \rangle &= G \mathcal{T}_r^i, \end{aligned}$$

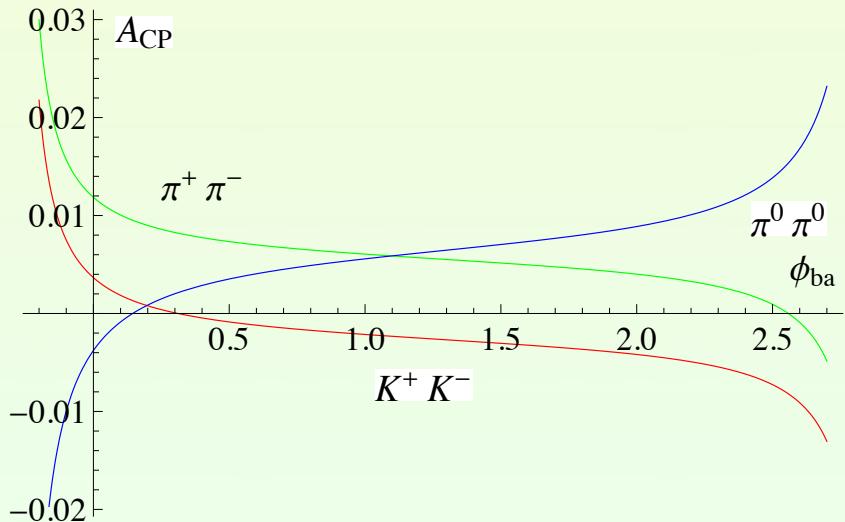
Then

$$\begin{aligned} \mathcal{A}(D^0 \rightarrow K^+K^-) &= (2T+E-S)\Sigma + \frac{1}{2}(3T+2G+F-E)\Delta, \\ \mathcal{A}(D^0 \rightarrow \pi^+\pi^-) &= -(2T+E-S)\Sigma + \frac{1}{2}(3T+2G+F-E)\Delta. \end{aligned}$$

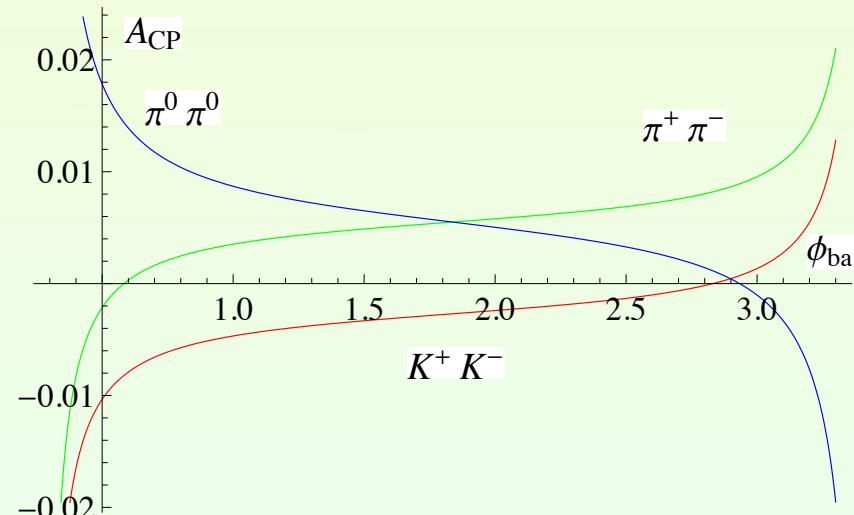
But $\Gamma(D^0 \rightarrow K^+K^-)/\Gamma(D^0 \rightarrow \pi^+\pi^-) \approx 3$ requires both terms of similar size (enhanced G, F)

\Rightarrow Expect sizable direct CPV in these decays! (predicted in 1989)

Of course, expect large SU(3) breaking effects.



This still requires an enhancement of F, G ,
but only of order 10



[Pirtskhalava & Uttayarat, Phys.Lett. B712 (2012) 81-86
Bhattacharya, Gronau & Rosner, PRD85 (2012) 054014
Cheng & Chiang, PRD85 (2012) 034036
Brod, Grossman, Kagan & Zupan, JHEP 1210 (2012) 161]

Or perhaps new physics??

[Rozanov & Vysotsky, arXiv:1111.6949

Altmannshofer, Primulando, Yu & Yu, JHEP 1204 (2012) 049

Cheng, Geng & Wang, PRD85 (2012) 077702

Feldmann, Nandi & Soni, JHEP 1206 (2012) 007

.....]

$$\Delta A_{cp} = A_{cp}(D^0 \rightarrow K^+K^-) - A_{cp}(D^0 \rightarrow \pi^+\pi^-) \text{ [%]}$$

| | | |
|--------------|-------------------------------|-----------|
| LHCb | $-0.82 \pm 0.21 \pm 0.11$ | PRL2012 |
| CDF | $-0.62 \pm 0.21 \pm 0.10$ | charm2012 |
| BaBar | (see below) | PRD2011 |
| Belle | $-0.87 \pm 0.41 \pm 0.06$ | ICHEP2012 |
| WA | $-0.678 \pm 0.147 (>4\sigma)$ | HFAG2012 |

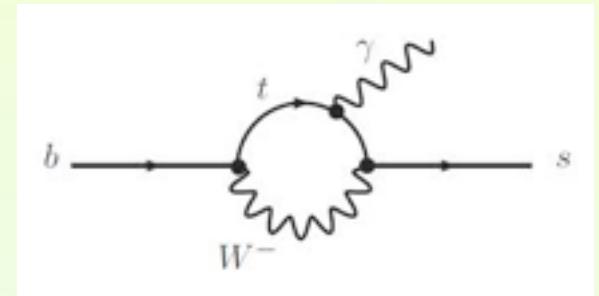
Individual A_{CP} are not significant

| | $A_{cp}(D^0 \rightarrow K^+K^-) \text{ [%]}$ | $A_{cp}(D^0 \rightarrow \pi^+\pi^-) \text{ [%]}$ |
|--------------|--|--|
| CDF | $-0.24 \pm 0.22 \pm 0.09$ | $+0.22 \pm 0.24 \pm 0.11$ |
| BaBar | $0.00 \pm 0.34 \pm 0.13$ | $-0.24 \pm 0.52 \pm 0.22$ |
| Belle | $-0.32 \pm 0.21 \pm 0.09$ | $+0.55 \pm 0.36 \pm 0.09$ |

**Need to search
for A_{CP} in
other modes**

Rare decays

$$B \rightarrow K^* \gamma$$



- Sensitive to NP (no tree level SM, new particles in 1-loop)
- 2HDM type II (SUSY-like) always larger than SM
- Effective theory approach to SM calculation:
 - Matching (NNLO)
 - Running (NNLO)
 - Matrix elements (almost complete NNLO)

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{QCD} \times \text{QED}}(u, d, s, c, b) + \frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \sum_{i=1}^8 C_i(\mu) Q_i$$

$$\begin{aligned}
 Q_{1,2} &= \begin{array}{c} \text{c} \\ \diagup \\ \text{b} \end{array} \text{---} \blacksquare \text{---} \begin{array}{c} \text{c} \\ \diagdown \\ \text{s} \end{array} &= (\bar{s}\Gamma_i c)(\bar{c}\Gamma'_i b), & \text{from } \begin{array}{c} \text{c} \\ \diagup \\ \text{b} \end{array} \text{---} \bullet \text{---} \text{W} \text{---} \bullet \text{---} \begin{array}{c} \text{c} \\ \diagdown \\ \text{s} \end{array}, \\
 Q_{3,4,5,6} &= \begin{array}{c} \text{q} \\ \diagup \\ \text{b} \end{array} \text{---} \blacksquare \text{---} \begin{array}{c} \text{q} \\ \diagdown \\ \text{s} \end{array} &= (\bar{s}\Gamma_i b) \sum_q (\bar{q}\Gamma'_i q), \\
 Q_7 &= \begin{array}{c} \gamma \\ \diagup \\ \text{b} \end{array} \text{---} \blacksquare \text{---} \begin{array}{c} \gamma \\ \diagdown \\ \text{s} \end{array} &= \frac{em_b}{16\pi^2} \bar{s}_L \sigma^{\mu\nu} b_R F_{\mu\nu}, \\
 Q_8 &= \begin{array}{c} g \\ \diagup \\ \text{b} \end{array} \text{---} \blacksquare \text{---} \begin{array}{c} g \\ \diagdown \\ \text{s} \end{array} &= \frac{gm_b}{16\pi^2} \bar{s}_L \sigma^{\mu\nu} T^a b_R G_{\mu\nu}^a,
 \end{aligned}$$

$$|C_i(m_b)| \sim 1$$

$$|C_i(m_b)| < 0.07$$

Known to NNLO

$$C_7(m_b) \simeq -0.3$$

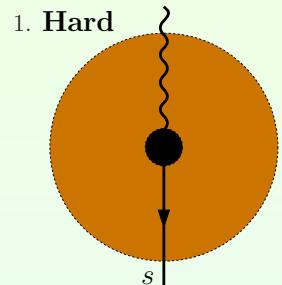
$$C_8(m_b) \simeq -0.15$$

Relative size of various long distance contributions (“matrix elements”) have been studied

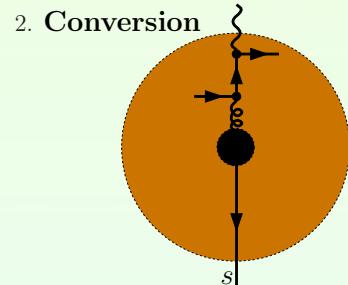
Energetic photon production in charmless decays of the \bar{B} -meson

$$(E_\gamma \gtrsim \frac{m_b}{3} \simeq 1.6 \text{ GeV})$$

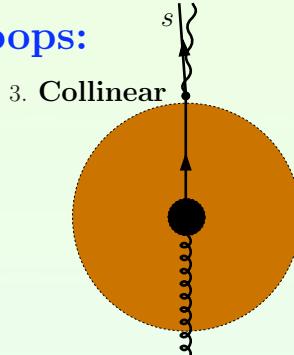
A. Without long-distance charm loops:



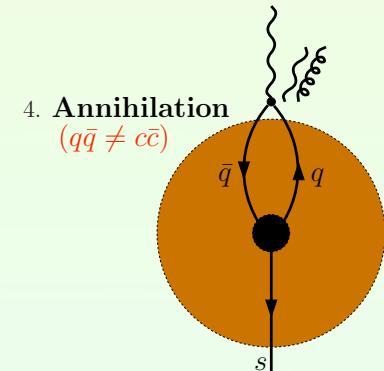
Dominant, well-controlled.



$\mathcal{O}(\alpha_s \Lambda/m_b)$, $(-1.5 \pm 1.5)\%$.
[Lee, Neubert, Paz, 2006]

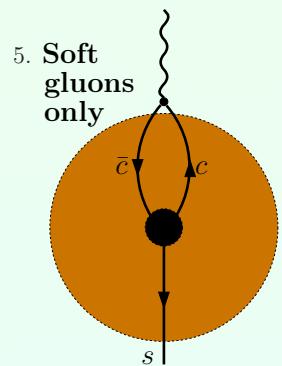


Pert. < 1%, nonp. $\sim -0.2\%$.
[Kapustin,Ligeti,Politzer, 1995]

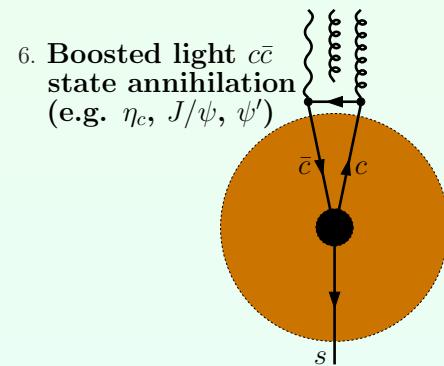


Exp. $\pi^0, \eta, \eta', \omega$ subtracted.
Perturbatively $\sim 0.1\%$.

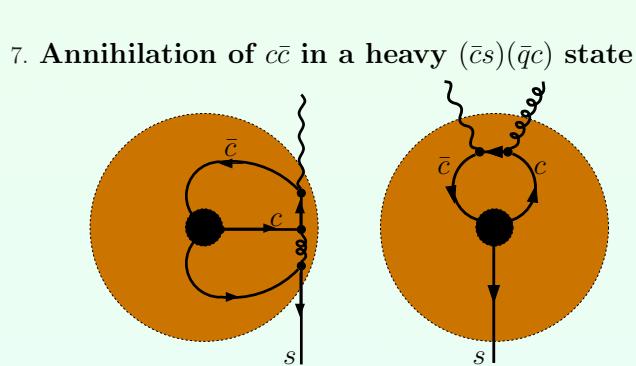
B. With long-distance charm loops:



$\mathcal{O}(\Lambda^2/m_c^2)$, $\sim +3.1\%$.
[Voloshin, 1996], [...],
[Buchalla, Isidori, Rey, 1997]



Exp. J/ψ subtracted ($< 1\%$).
Perturbatively (including hard): $\sim +3.6\%$.
 $\phi_{ij}^{(1)}(\delta), \phi_{ij}^{(2)\beta_0}(\delta), i, j = 1, 2$



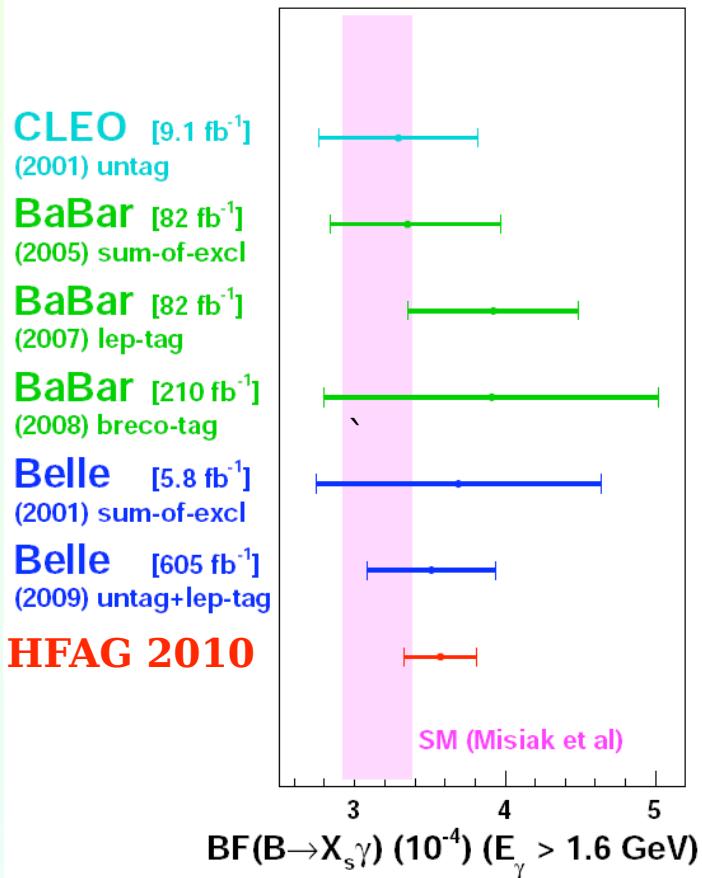
$\mathcal{O}(\alpha_s(\Lambda/M)^2)$
 $M \sim 2m_c, 2E_\gamma, m_b$.
e.g. $\mathcal{B}[B^- \rightarrow D_{sJ}(2457)^- D^*(2007)^0] \simeq 1.2\%$,
 $\mathcal{B}[B^0 \rightarrow D^*(2010)^+ \bar{D}^*(2007)^0 K^-] \simeq 1.2\%$.

[lifted from Misiak]

HFAG 2010: $B(B \rightarrow X_s \gamma) = (3.55 \pm 0.26) \times 10^{-4}$ (for $E_\gamma > 1.6$ GeV)

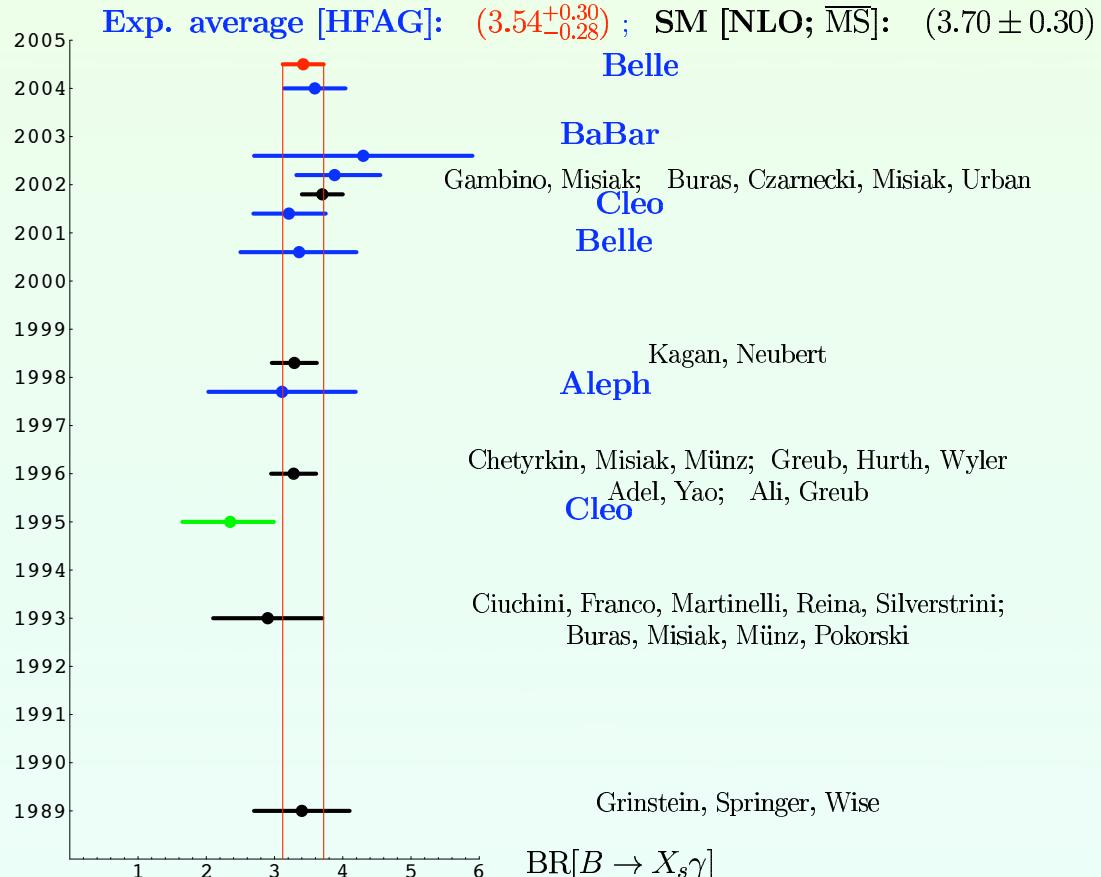
vs

SM: $B(B \rightarrow X_s \gamma) = (3.15 \pm 0.23) \times 10^{-4}$ (for $E_\gamma > 1.6$ GeV)

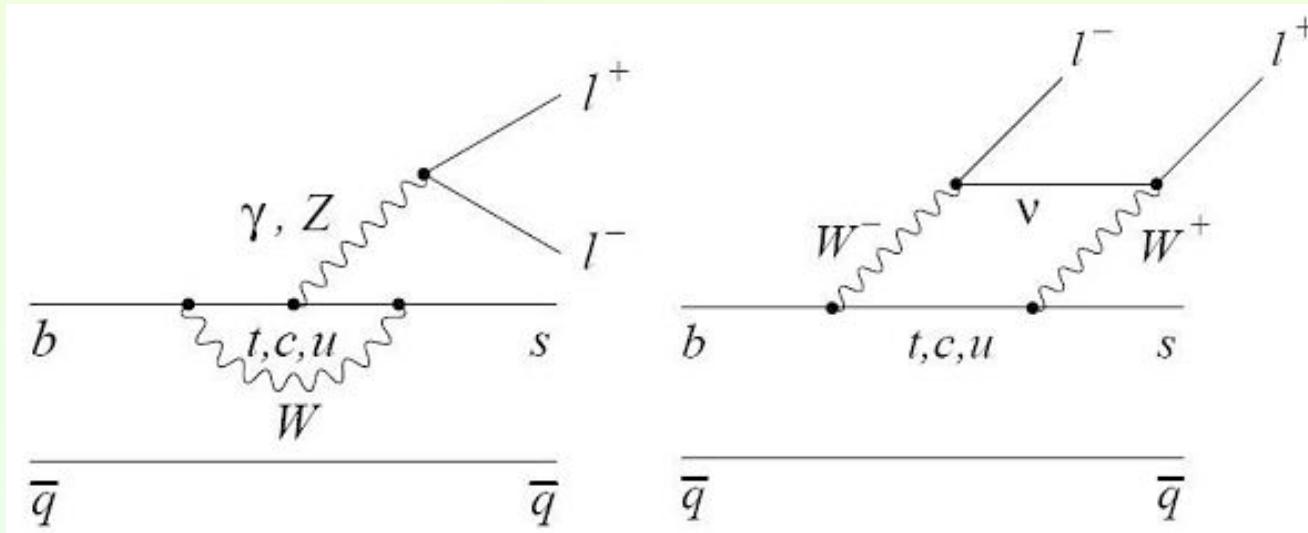


A Brief History of Time

BR[$\bar{B} \rightarrow X_s \gamma$] (units: 10^{-4}) Measurements & the SM calculations



$$B \rightarrow K^{(*)} l^+ l^-$$



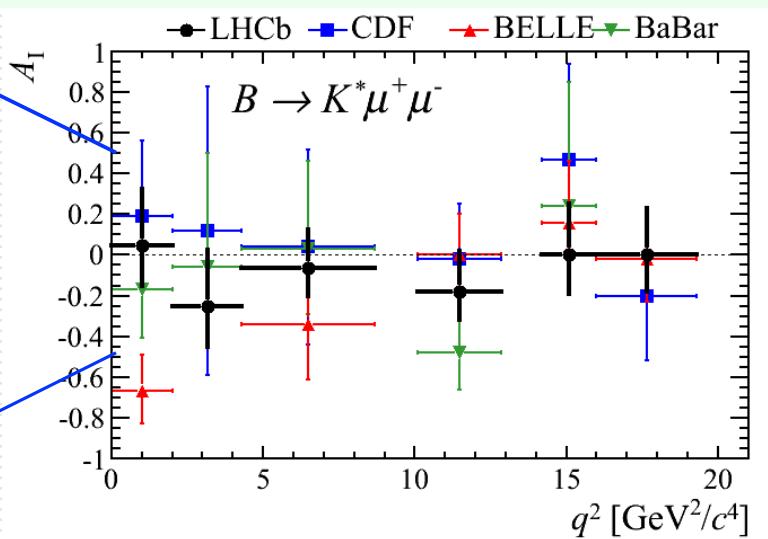
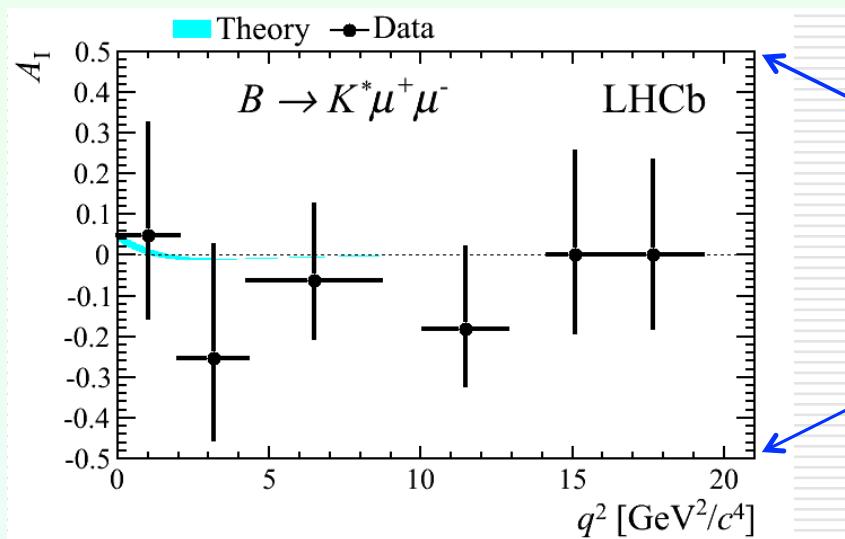
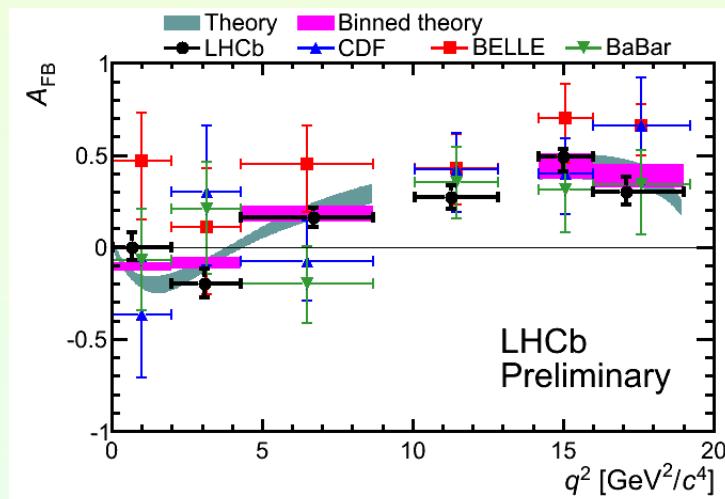
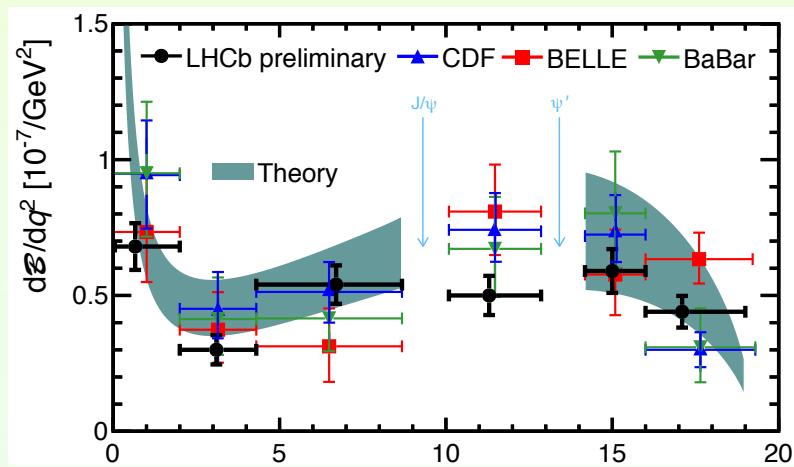
- Sensitive to NP (no tree level SM, new particles in 1-loop)
- Many variables can be studied, e.g., forward-backward asymmetry A_{FB} or Isospin asymmetry:

$$A_I = \frac{\mathcal{B}(B^0 \rightarrow K^{(*)0} \mu^+ \mu^-) - \frac{\tau_0}{\tau_+} \mathcal{B}(B^\pm \rightarrow K^{(*)\pm} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{(*)0} \mu^+ \mu^-) + \frac{\tau_0}{\tau_+} \mathcal{B}(B^\pm \rightarrow K^{(*)\pm} \mu^+ \mu^-)}$$

- Charmonium resonance region must be excluded ($B \rightarrow K^{(*)}\psi \rightarrow K^{(*)}l^+ l^-$)
 - Small $q^2 = (p_+ + p_-)^2$, large recoil energy for $K^{(*)}$, use SCET
 - Large q^2 , use HQET
 - SM: fairly clean prediction of location of zero in A_{FB} , negligible A_I

$B \rightarrow K^* l^+ l^-$

[Gallas, ICHEP 2012]

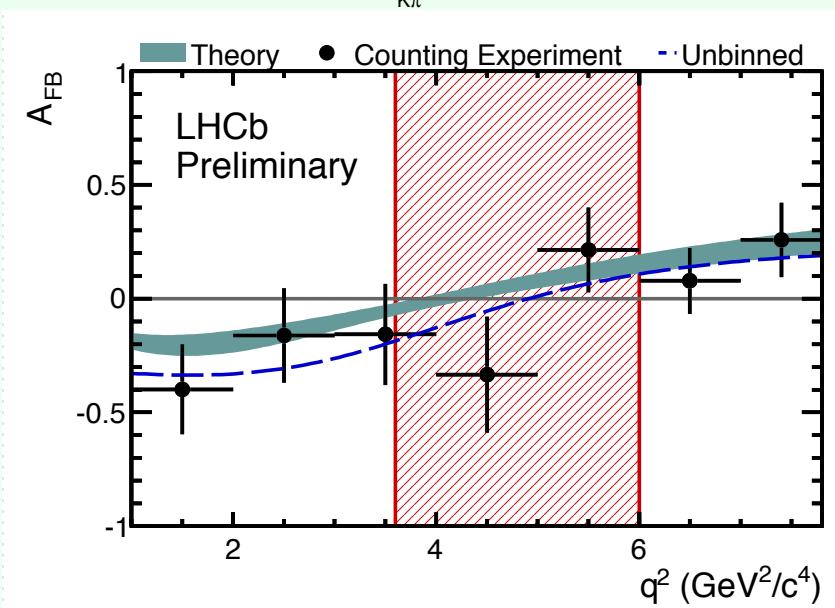
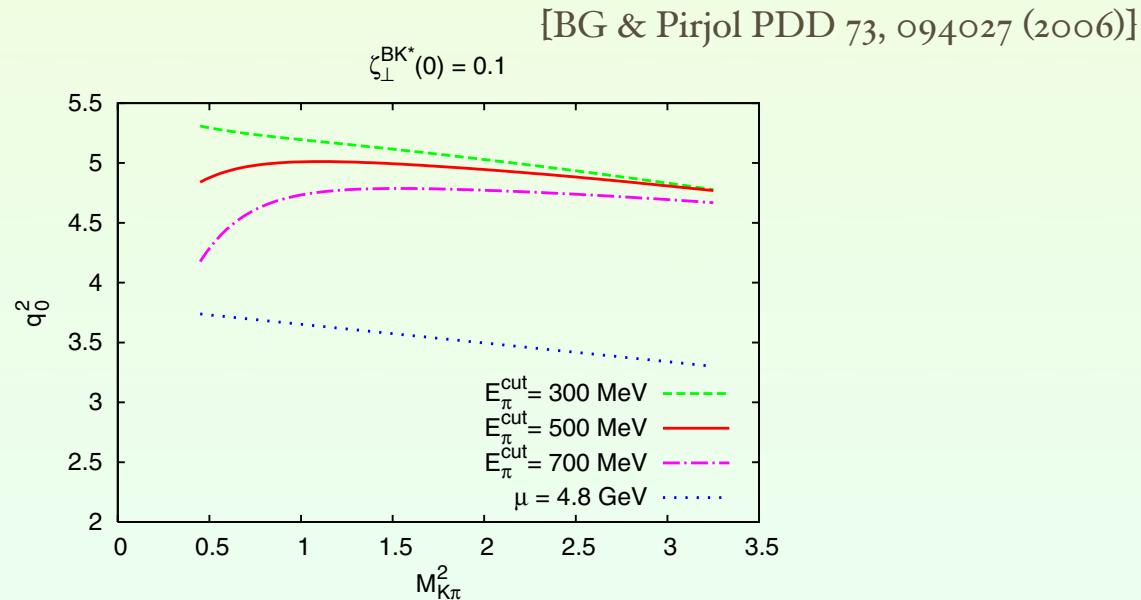
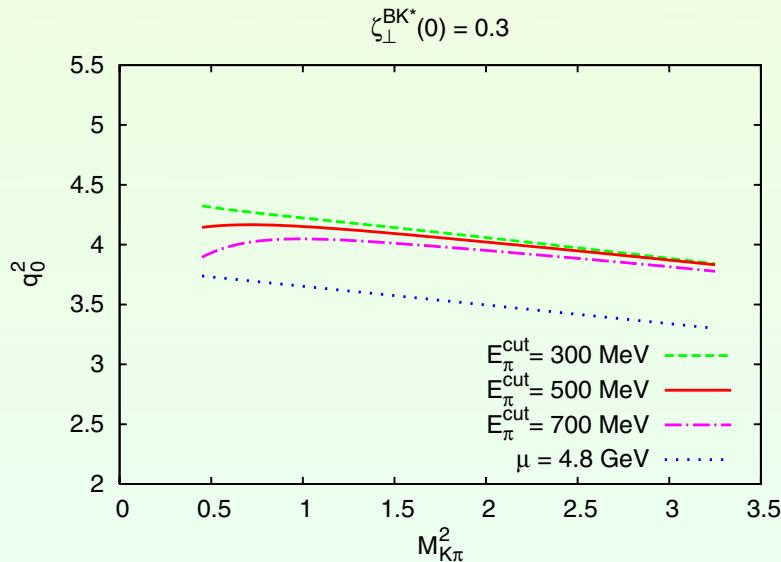


No hint of NP here!

A_{FB} zero

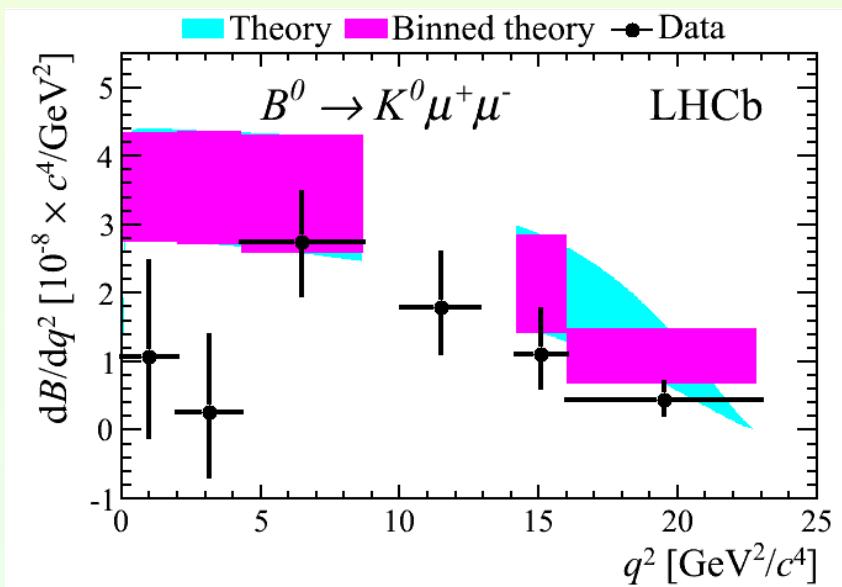
[Burdman]

Theory, including non-resonant $K\pi$, to order Λ/m_b , with maximum π energy cut



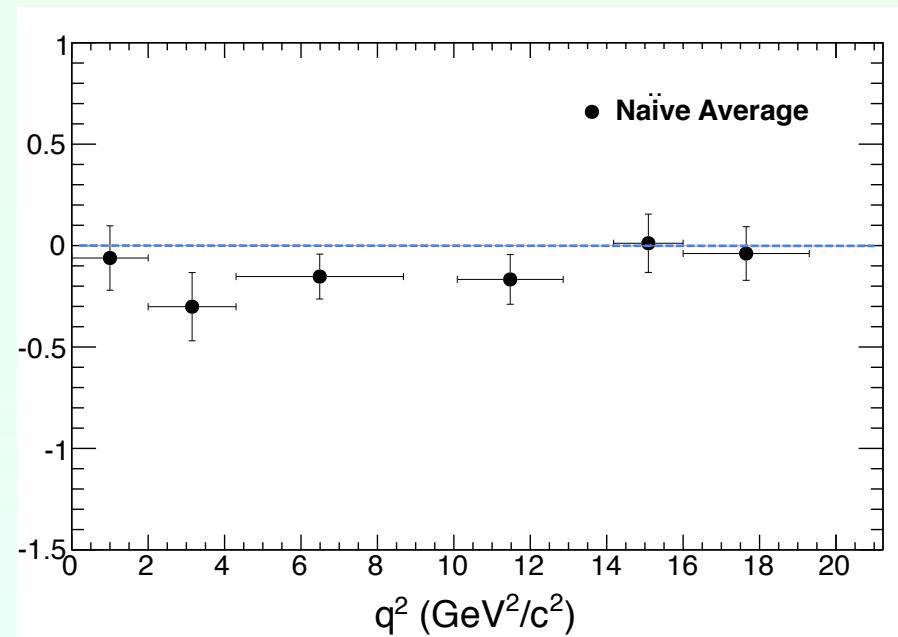
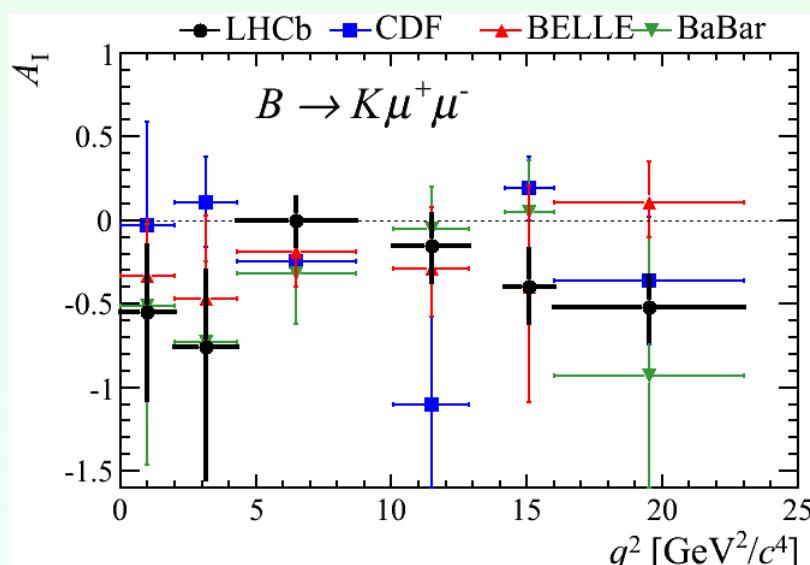
The world's first measurement of q_0^2 ,
at $q_0^2 = 4.9^{+1.1}_{-1.3} \text{ GeV}^2/\text{c}^4$ [Preliminary]

$$B \rightarrow Kl^+l^-$$



Discrepant with SM predictions:

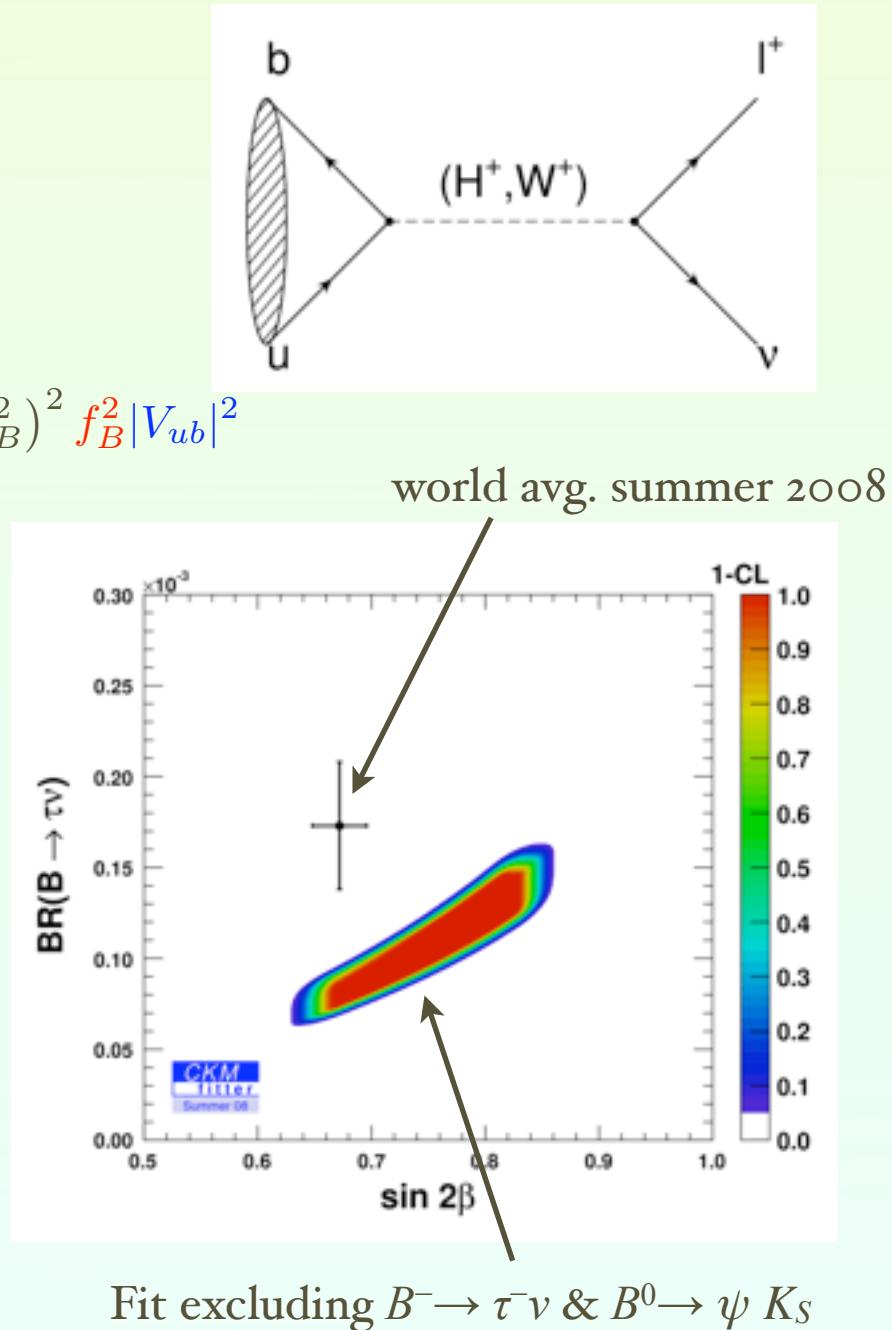
- Low rate at low q^2
- A_1 negative throughout
 - LHCb alone: 4.2σ from zero
 - Why in K , but not in K^* ?
 - NP models?



τ

Is there still a problem with $B^- \rightarrow \tau^- \nu$?

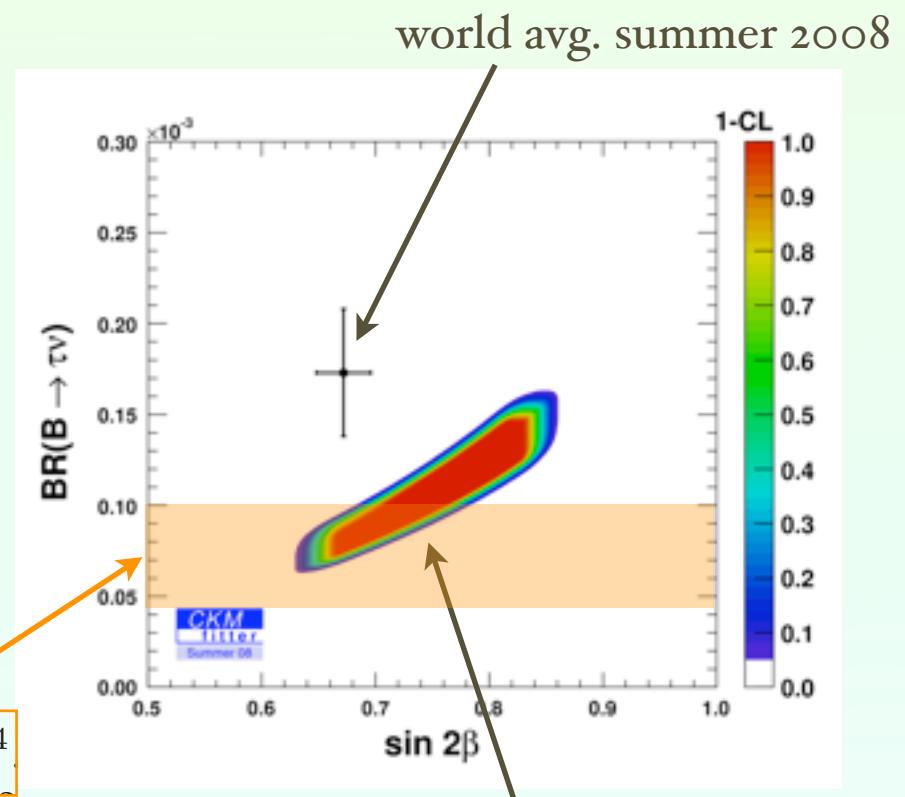
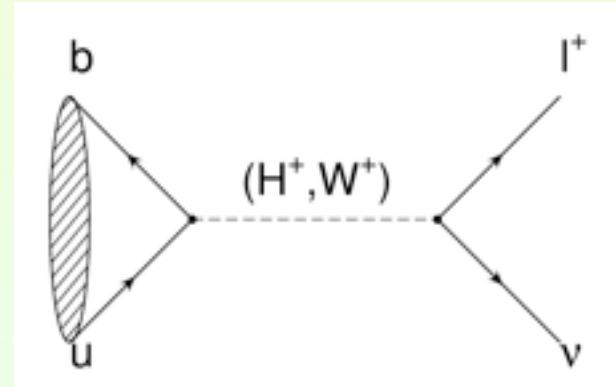
- $B^- \rightarrow \tau^- \nu$ in SM is tree level
- Clean SM prediction, lattice gives f_B
- Modified for τ , less for e, μ , by charged higgs in 2HDM
- 2HDM modifies box diagram too: cannot use SM extraction of $\sin(2\beta)$ from $B^0 \rightarrow \psi K_S$
- But NEW Belle result [\[arXiv:1208.4678\]](#)



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- But NEW Belle result [arXiv:1208.4678]

$$\mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}_\tau) = [0.72^{+0.27}_{-0.25}(\text{stat}) \pm 0.11(\text{syst})] \times 10^{-4}$$



Fit excluding $B^- \rightarrow \tau^- \nu$ & $B^0 \rightarrow \psi K_S$

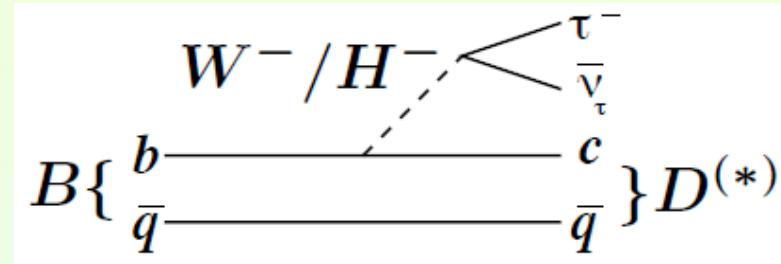
$$B^- \rightarrow D\tau^-\nu \quad \text{and} \quad B^- \rightarrow D^*\tau^-\nu$$

- Like $B^- \rightarrow \tau^-\nu$, tree level
- Like $B^- \rightarrow \tau^-\nu$, enhanced relative to SM

- Sensitive to more form factors, e.g.,

- 2HDM: tree level

- Define R



$$\langle D(p_D) | \bar{c} \gamma^\mu b | \bar{B}(p_B) \rangle = F_V(q^2) \left[p_B^\mu + p_D^\mu - m_B^2 \frac{1-r^2}{q^2} q^\mu \right] \\ + F_S(q^2) m_B^2 \frac{1-r^2}{q^2} q^\mu,$$

$$\langle D(p_D) | \bar{c} b | \bar{B}(p_B) \rangle = \frac{m_B^2 (1-r^2)}{\overline{m}_b - \overline{m}_c} F_S(q^2) \quad r = m_D/m_B$$

$$R(D) = \frac{Br(\bar{B} \rightarrow D\tau\nu)}{Br(\bar{B} \rightarrow D\ell\nu)}$$

$$R(D^*) = \frac{Br(\bar{B} \rightarrow D^*\tau\nu)}{Br(\bar{B} \rightarrow D^*\ell\nu)}$$

| | SM Theory | BaBar value | Diff. |
|--------------------|-------------------|-----------------------------|--------------|
| R(D) | 0.297 ± 0.017 | $0.440 \pm 0.058 \pm 0.042$ | $+2.0\sigma$ |
| R(D [*]) | 0.252 ± 0.003 | $0.332 \pm 0.024 \pm 0.018$ | $+2.7\sigma$ |

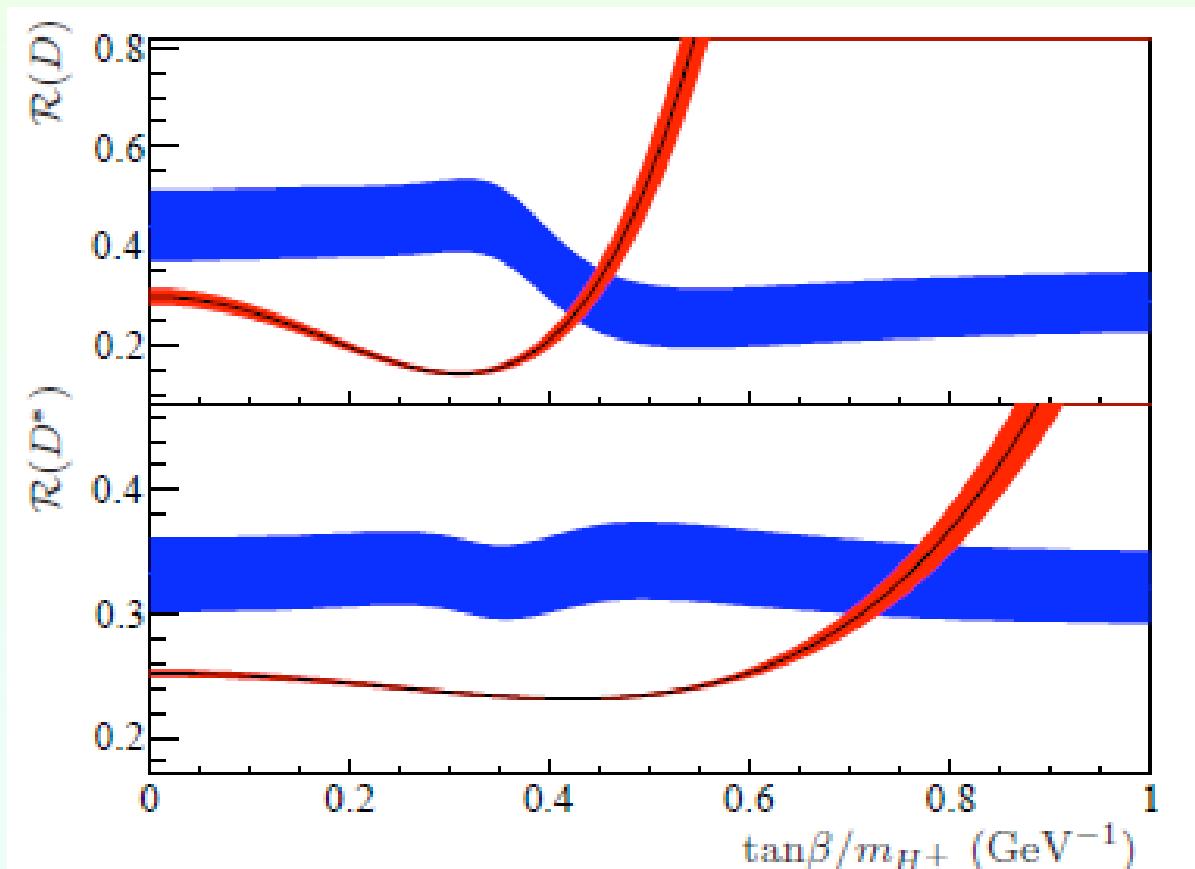
3.4σ deviation (above)
SM in aggregate

Combination of measurements also inconsistent with 2HDM

$$\text{SM}(D^*) \quad \frac{d\Gamma_\tau}{dq^2} = \frac{G_F^2 |V_{cb}|^2 |\mathbf{P}| q^2}{96\pi^3 m_B^2} \left(1 - \frac{m_\tau^2}{q^2}\right)^2 \left[(|H_{++}|^2 + |H_{--}|^2 + |H_{00}|^2) \left(1 + \frac{m_\tau^2}{2q^2}\right) + \frac{3}{2} \frac{m_\tau^2}{q^2} |H_{0t}|^2 \right]$$

$$H_t^{\text{2HDM}} = H_t^{\text{SM}} \times \left(1 - \frac{\tan^2 \beta}{m_{H^\pm}^2} \frac{q^2}{1 \mp m_c/m_b}\right)$$

- for $D\tau\nu$
+ for $D^*\tau\nu$



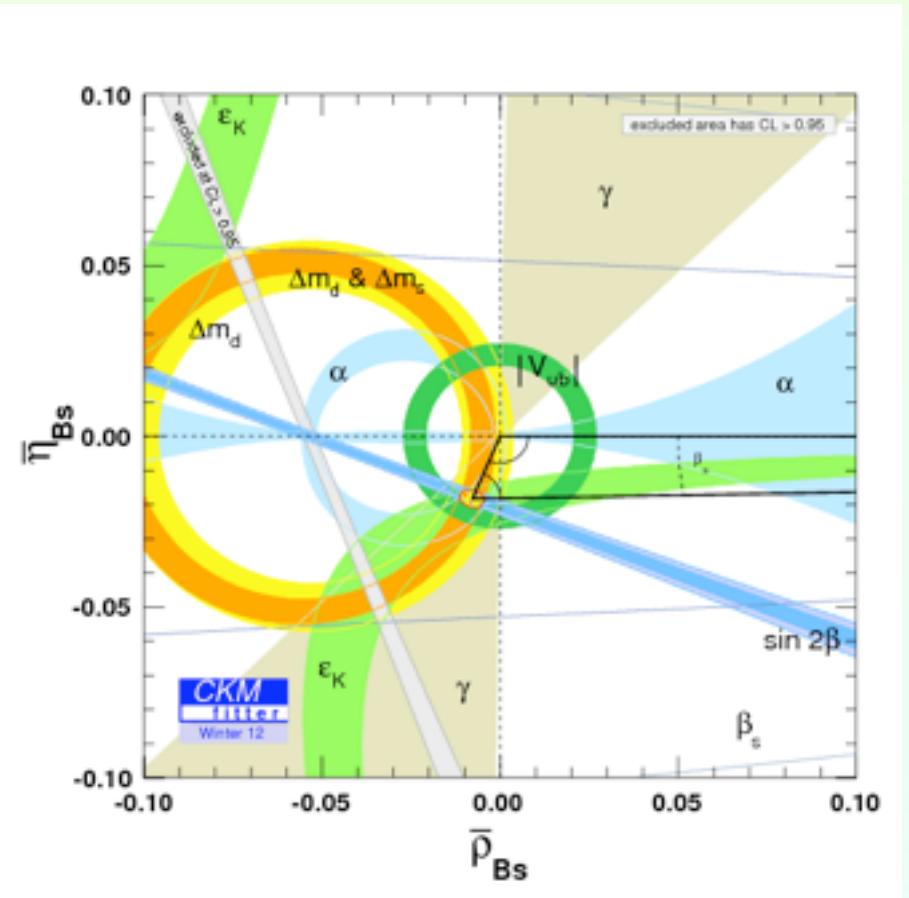
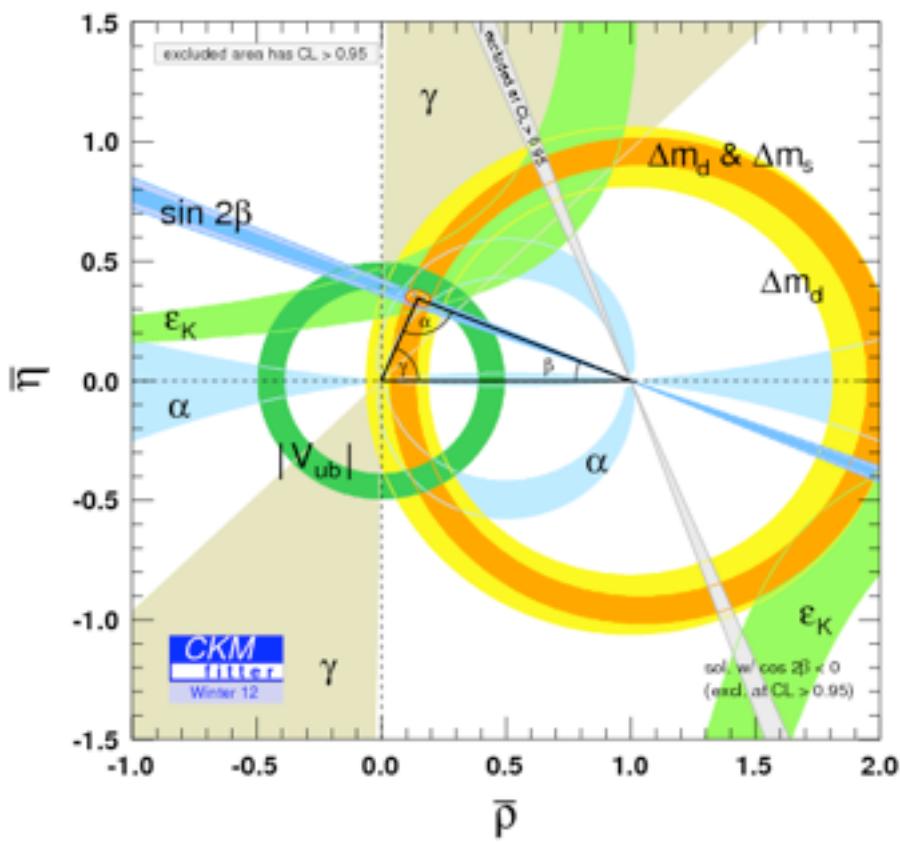
Taking into account the effect of $\tan \beta/m_H$ on efficiency

$$R(D) \rightarrow \tan \beta/m_H = 0.44 \pm 0.02$$

$$R(D^*) \rightarrow \tan \beta/m_H = 0.75 \pm 0.04$$

Mutually exclusive with
 $CL > 99.8\%$

NP?



Don't forget: General MSSM lives in a straightjacket because of flavor

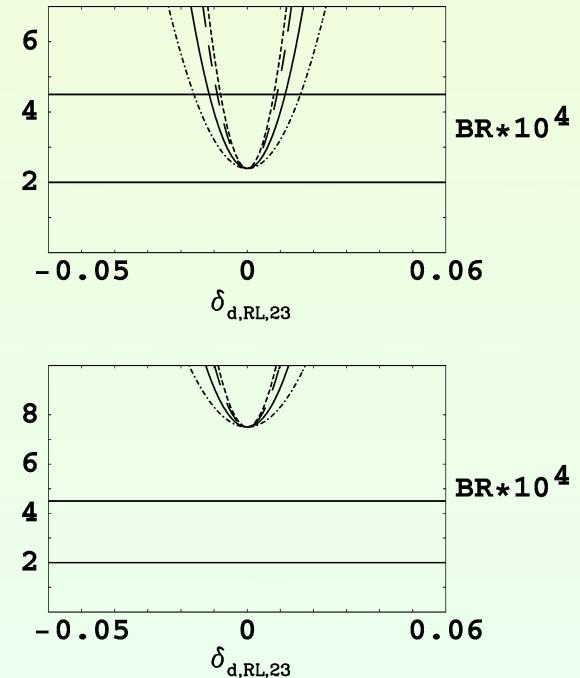
General MSSM

Ruled out unless squarks almost degenerate

Assume small

$$\delta = \frac{\Delta m^2}{\bar{m}^2}$$

and bound

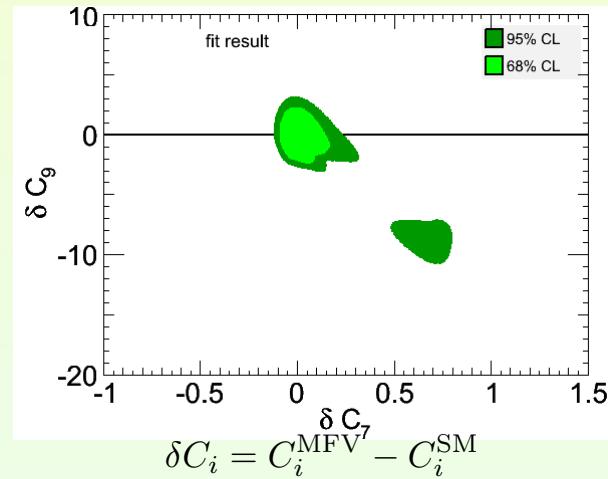


Besmer et al, NPB609:359,2001

**Must introduce (ad-hoc) CMSSM, or NUHM1,
or better justified gauge mediation variants**

(NUMH_I=”non-universal higgs masses”-1 version of MSSM)

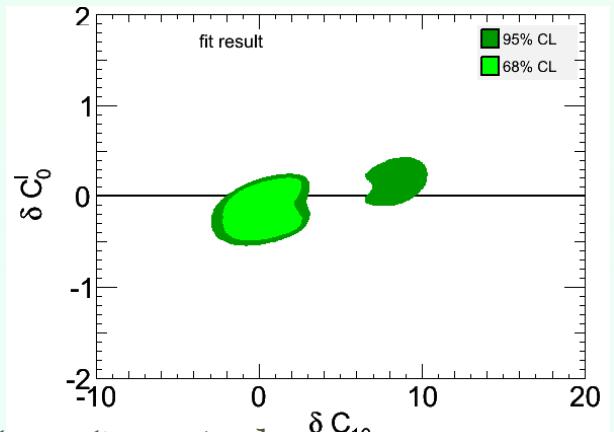
- What remains as acceptable NP:
 - Decoupling: Make all new particles ever heavier
 - Flavor Blind: Make all flavor couplings small (MFV)
- Fabulous for hiding non-existent particles and interactions!



$$\mathcal{H}_{\text{eff}}^{b \rightarrow s} = -\frac{4G_F}{\sqrt{2}} \sum_{i=3}^{10} [(V_{us}^* V_{ub} + V_{cs}^* V_{cb}) C_i^c + V_{ts}^* V_{tb} C_i^t] P_i + V_{ts}^* V_{tb} C_0^\ell P_0^\ell + \text{h.c.}$$

- I propose we should be doing something else:
 - We do have deviations from SM
 - Should focus on models that address anomalies
 - Tricky: which anomalies do you focus on?
 - $>3\sigma$
 - At least two experiments
 - (No guaranteed persistence, witness $B \rightarrow \tau\nu$)
 - Example: top-quark FB asymmetry at Tevatron

$$\begin{aligned} P_7 &= \frac{e}{16\pi^2} m_b (\bar{s}_L \sigma^{\mu\nu} b_R) F_{\mu\nu}, \\ P_8 &= \frac{g_s}{16\pi^2} m_b (\bar{s}_L \sigma^{\mu\nu} T^a b_R) G_{\mu\nu}^a, \\ P_9 &= \frac{e^2}{16\pi^2} (\bar{s}_L \gamma_\mu b_L) \sum_\ell (\bar{\ell} \gamma^\mu \ell), \\ P_{10} &= \frac{e^2}{16\pi^2} (\bar{s}_L \gamma_\mu b_L) \sum_\ell (\bar{\ell} \gamma^\mu \gamma_5 \ell), \\ P_0^\ell &= \frac{e^2}{16\pi^2} (\bar{s}_L b_R) (\bar{\ell}_R \ell_L). \end{aligned}$$



SM Theory ($B_s \rightarrow \mu^+ \mu^-$)

Reliably compute CP-averaged decay rates in the flavor eigenstate basis

$$\langle \Gamma(B_s(t) \rightarrow f) \rangle|_{t=0} = \Gamma(B_s^0 \rightarrow f) + \Gamma(\bar{B}_s^0 \rightarrow f)$$

$$\text{Br}(B_s) = (3.23 \pm 0.27) \times 10^{-9}$$

$$\text{Br}(B_d) = (1.07 \pm 0.27) \times 10^{-10}$$

[Buras et al, Eur.Phys.J. C72 (2012) 2172]

Digression

NEW: De Bruyn et al: This is not what is measured!

[De Bruyn et al, PRD86 (2012) 014027]

Cannot neglect life-time difference:

$$y_s \equiv \frac{\Delta\Gamma_s}{2\Gamma_s} \equiv \frac{\Gamma_L^{(s)} - \Gamma_H^{(s)}}{2\Gamma_s} = 0.088 \pm 0.014$$

Decay rate is sum of two different exponentials

$$\langle \Gamma(B_s(t) \rightarrow f) \rangle \equiv \Gamma(B_s^0(t) \rightarrow f) + \Gamma(\bar{B}_s^0(t) \rightarrow f) = R_H^f e^{-\Gamma_H^{(s)} t} + R_L^f e^{-\Gamma_L^{(s)} t},$$

Experiment measures total number produced:

$$\text{BR}(B_s \rightarrow f)_{\text{exp}} \equiv \frac{1}{2} \int_0^\infty \langle \Gamma(B_s(t) \rightarrow f) \rangle dt$$

They obtain:

$$\boxed{\text{BR}(B_s \rightarrow f)_{\text{theo}} = \left[\frac{1 - y_s^2}{1 + \mathcal{A}_{\Delta\Gamma}^f y_s} \right] \text{BR}(B_s \rightarrow f)_{\text{exp}}}$$

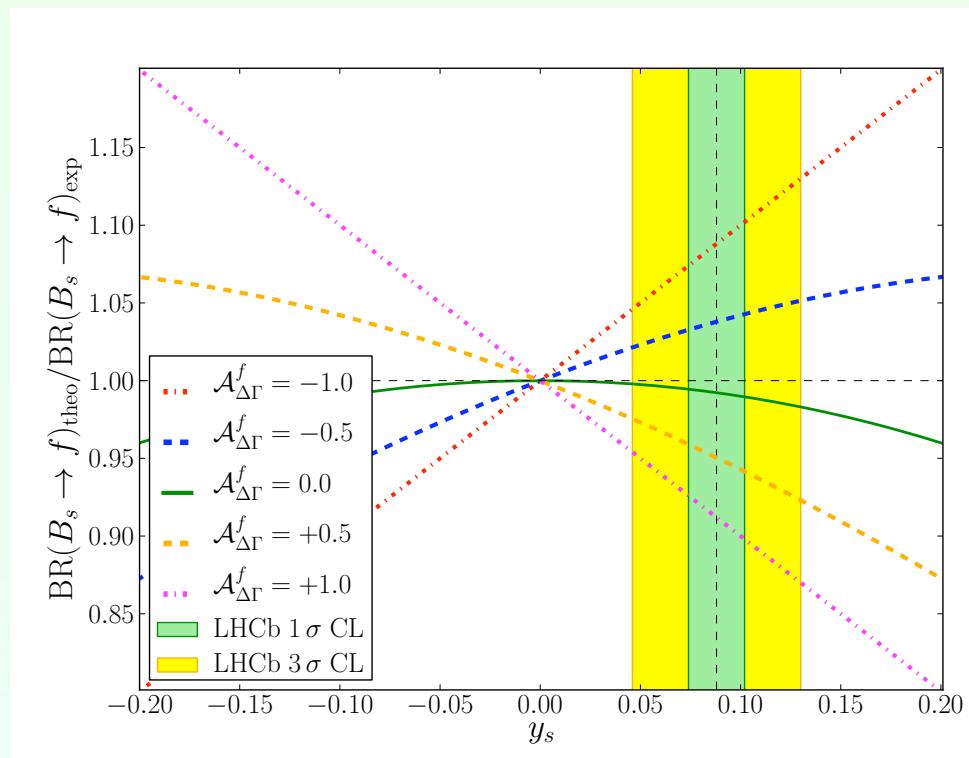
where

$$\mathcal{A}_{\Delta\Gamma}^f \equiv \frac{R_H^f - R_L^f}{R_H^f + R_L^f}$$

This applies to any final state f (not just $\mu^+\mu^-$)

| $B_s \rightarrow f$ | $\text{BR}(B_s \rightarrow f)_{\text{exp}}$ (measured) | $\mathcal{A}_{\Delta\Gamma}^f(\text{SM})$ | $\frac{\text{BR}(B_s \rightarrow f)_{\text{theo}}}{\text{BR}(B_s \rightarrow f)_{\text{exp}}}$ From Eq. (8) | $\frac{\text{BR}(B_s \rightarrow f)_{\text{theo}}}{\text{BR}(B_s \rightarrow f)_{\text{exp}}}$ From Eq. (10) |
|---------------------|---|---|--|---|
| $J/\psi f_0(980)$ | $(1.29^{+0.40}_{-0.28}) \times 10^{-4}$ [18] | 0.9984 ± 0.0021 [14] | 0.912 ± 0.014 | 0.890 ± 0.082 [6] |
| $J/\psi K_S$ | $(3.5 \pm 0.8) \times 10^{-5}$ [7] | 0.84 ± 0.17 [15] | 0.924 ± 0.018 | N/A |
| $D_s^- \pi^+$ | $(3.01 \pm 0.34) \times 10^{-3}$ [9] | 0 (exact) | 0.992 ± 0.003 | N/A |
| $K^+ K^-$ | $(3.5 \pm 0.7) \times 10^{-5}$ [18] | -0.972 ± 0.012 [13] | 1.085 ± 0.014 | 1.042 ± 0.033 [19] |
| $D_s^+ D_s^-$ | $(1.04^{+0.29}_{-0.26}) \times 10^{-2}$ [18] | -0.995 ± 0.013 [16] | 1.088 ± 0.014 | N/A |

Large corrections!



more generally

End Digression

MLFV

Note: LN vs LF

- Distinguish Lepton Number (LN) violating interactions from Lepton Flavor (LF) violating interactions
- LN is a U(1) symmetry, assigning unit charge to all leptons (like baryon number for quarks)
 - Majorana mass breaks LN
- LF is an SU(3) symmetry, mixing different flavors
 - It commutes with $U(1)_{LN}$, *i.e.*, preserves the LN charge

Desirable to consider LFV at a ‘low scale’ (few TeV?),
while for see-saw want LNV at an intermediate scale

$$\Lambda_{\text{LF}} \ll \Lambda_{\text{LN}} \ll M_{\text{planck}}$$

- Two approaches. Field content below LFV scale is three families of L_i and eR_i
(plus H and gauge). Then:
 - Minimal: majorana mass is from non-renormalizable interaction
 - Extended: include very heavy v_{Ri} insofar as it dictates MFV coupling, but then integrate out

MLFV: Minimal Field Content

Assumptions:

1. The breaking of the $U(I)_{LN}$ is independent from the breaking of lepton flavor G_{LF} , with large Λ_{LN} (associated with see-saw)
2. There are only two irreducible sources of G_{LF} breaking, λ_e and g_v , defined by

$$\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) - \frac{1}{2\Lambda_{LN}} g_\nu^{ij} (\bar{L}_L^{ci} \tau_2 H) (H^T \tau_2 L_L^j) + \text{h.c.}$$

Ex: SUSY Triplet Model, A. Rossi, PRD66(2002)075003

Implementation of MLFV in Minimal Field Content Case

- Want to add all possible terms to the lagrangian consistent with assumptions (and usual stuff: Lorentz invariance, gauge symmetry, locality, ...)
- Need characterization of terms that are allowed
- Use spurion method:

$$L_L \rightarrow V_L L_L$$

$$e_R \rightarrow V_R e_R$$

$$\lambda_e \rightarrow V_R \lambda_e V_L^\dagger$$

$$g_\nu \rightarrow V_L^* g_\nu V_L^\dagger$$

(recall: $\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) - \frac{1}{2\Lambda_{LN}} g_\nu^{ij} (\bar{L}_L^{ci} \tau_2 H) (H^T \tau_2 L_L^j) + \text{h.c.}$)

Then write all operators of dimension 5, 6, ... consistent with assumptions.

For

need two lepton field ops:

$$\mu \rightarrow e\gamma, \quad \mu + N \rightarrow e + N',$$

Ops with LL

$$O_{LL}^{(1)} = \bar{L}_L \gamma^\mu \Delta L_L H^\dagger i D_\mu H$$

$$O_{LL}^{(2)} = \bar{L}_L \gamma^\mu \tau^a \Delta L_L H^\dagger \tau^a i D_\mu H$$

$$O_{LL}^{(3)} = \bar{L}_L \gamma^\mu \Delta L_L \bar{Q}_L \gamma_\mu Q_L$$

$$O_{LL}^{(4d)} = \bar{L}_L \gamma^\mu \Delta L_L \bar{d}_R \gamma_\mu d_R$$

$$O_{LL}^{(4u)} = \bar{L}_L \gamma^\mu \Delta L_L \bar{u}_R \gamma_\mu u_R$$

$$O_{LL}^{(5)} = \bar{L}_L \gamma^\mu \tau^a \Delta L_L \bar{Q}_L \gamma_\mu \tau^a Q_L$$

Ops with RL

$$O_{RL}^{(1)} = g' H^\dagger \bar{e}_R \sigma^{\mu\nu} \lambda_e \Delta L_L B_{\mu\nu}$$

$$O_{RL}^{(2)} = g H^\dagger \bar{e}_R \sigma^{\mu\nu} \tau^a \lambda_e \Delta L_L W_{\mu\nu}^a$$

$$O_{RL}^{(3)} = (D_\mu H)^\dagger \bar{e}_R \lambda_e \Delta D_\mu L_L$$

$$O_{RL}^{(4)} = \bar{e}_R \lambda_e \Delta L_L \bar{Q}_L \lambda_D d_R$$

$$O_{RL}^{(5)} = \bar{e}_R \sigma^{\mu\nu} \lambda_e \Delta L_L \bar{Q}_L \sigma_{\mu\nu} \lambda_D d_R$$

$$O_{RL}^{(6)} = \bar{e}_R \lambda_e \Delta L_L \bar{u}_R \lambda_U^\dagger i \tau^2 Q_L$$

$$O_{RL}^{(7)} = \bar{e}_R \sigma^{\mu\nu} \lambda_e \Delta L_L \bar{u}_R \sigma_{\mu\nu} \lambda_U^\dagger i \tau^2 Q_L$$

We have used

$$\Delta \equiv g_\nu^\dagger g_\nu \text{ with transformation}$$

$$\Delta \rightarrow V_L \Delta V_L^\dagger$$

Also neglected Δ^2

We have neglected

, hence no R operators

For $\mu \rightarrow ee\bar{e}$ need, in addition, four lepton operators

$$O_{4L}^{(1)} = \bar{L}_L \gamma^\mu \Delta L_L \bar{L}_L \gamma_\mu L_L$$

$$O_{4L}^{(2)} = \bar{L}_L \gamma^\mu \tau^a \Delta L_L \bar{L}_L \gamma_\mu \tau^a L_L$$

$$O_{4L}^{(3)} = \bar{L}_L \gamma^\mu \Delta L_L \bar{e}_R \gamma_\mu e_R$$

$$O_{4L}^{(4)} = \delta_{nj} \delta_{mi}^* \bar{L}_L^i \gamma^\mu L_L^j \bar{L}_L^m \gamma^\mu L_L^n$$

$$O_{4L}^{(5)} = \delta_{nj} \delta_{mi}^* \bar{L}_L^i \gamma^\mu \tau^a L_L^j \bar{L}_L^m \gamma^\mu \tau^a L_L^n$$

where we used $\delta = g_\nu$ (so we can use same expressions for extended field content case)

Up to dimension 6 operators, the new interactions are

$$\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda_{\text{LFV}}^2} \sum_{i=1}^5 \left(c_{LL}^{(i)} O_{LL}^{(i)} + c_{4L}^{(i)} O_{4L}^{(i)} \right) + \frac{1}{\Lambda_{\text{LFV}}^2} \left(\sum_{j=1}^2 c_{RL}^{(j)} O_{RL}^{(j)} + \text{h.c.} \right)$$

with coefficients naively

$$c \sim 1$$

We can now study the phenomenology of MLFV
with minimal field content.

Useful to look at parameters first

Also useful to contrast with results of extended field content

Use G_{LF} symmetry to rotate to the mass eigenstate basis (v = Higgs vev)

$$\lambda_e = \frac{m_\ell}{v} = \frac{1}{v} \text{diag}(m_e, m_\mu, m_\tau)$$

$$g_\nu = \frac{\Lambda_{LN}}{v^2} U^* m_\nu U^\dagger = \frac{\Lambda_{LN}}{v^2} U^* \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3}) U^\dagger$$

U is the PMNS matrix. It is determined from neutrino mixing:

$$U \approx \begin{pmatrix} ce^{i\alpha_1/2} & se^{i\alpha_2/2} & s_{13}e^{-i\delta} \\ -se^{i\alpha_1/2}/\sqrt{2} & ce^{i\alpha_2/2}/\sqrt{2} & 1/\sqrt{2} \\ se^{i\alpha_1/2}/\sqrt{2} & -ce^{i\alpha_2/2}/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}$$

Here $c \equiv \cos \theta_{\text{sol}}$ $s \equiv \sin \theta_{\text{sol}}$ $\theta_{\text{sol}} \simeq 32.5^\circ$

s_{13} is poorly known, $s_{13} < 0.3$

note added
sorry: two different δ

- Hence, amplitudes are given in terms of
 - Λ_{LN} and Λ_{LFV} (actually only ratio $\Lambda_{LN}/\Lambda_{LFV}$)
 - Coefficients, C , of order 1
 - Low energy measured (or measurable) masses and mixing angles
- In particular, the following two combinations appear in the operators:

$$\Delta = \frac{\Lambda_{LN}^2}{v^4} U m_\nu^2 U^\dagger \quad \delta = \delta^T = \frac{\Lambda_{LN}}{v^2} U^* m_\nu U^\dagger$$

MLFV: Extended Field Content

Recall, now we include RH neutrinos, flavor group has additional $SU(3)_{vR}$ factor

Assumptions:

1. The right handed neutrino mass is flavor neutral, ie, it breaks $SU(3)_{vR}$ to $O(3)_{vR}$. Denote $M_\nu^{ij} = M_\nu \delta^{ij}$
2. The right handed neutrino mass is the only source of LN breaking and Λ_{LFV}
3. Remaining LF-symmetry broken only by λ_e and λ_ν defined by

$$\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) + i\lambda_\nu^{ij} \bar{\nu}_R^i (H^T \tau_2 L_L^j) + \text{h.c.}$$

Implementation of MLFV in Extended Field Content Case

$$\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) + i\lambda_\nu^{ij} \bar{\nu}_R^i (H^T \tau_2 L_L^j) + \text{h.c.}$$

Same as before, but now transformations are:

$$L_L \rightarrow V_L L_L \quad e_R \rightarrow V_R e_R \quad \nu_R \rightarrow O_\nu \nu_R$$

$$\lambda_e \rightarrow V_R \lambda_e V_L^\dagger \quad \lambda_\nu \rightarrow O_\nu \lambda_\nu V_L^\dagger$$

Implementation of MLFV in Extended Field Content Case

$$\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) + i\lambda_\nu^{ij} \bar{\nu}_R^i (H^T \tau_2 L_L^j) + \text{h.c.}$$

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As before

$$\Delta = \lambda_\nu^\dagger \lambda_\nu \quad \Delta \rightarrow V_L \Delta V_L^\dagger$$

Implementation of MLFV in Extended Field Content Case

$$\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) + i \lambda_\nu^{ij} \bar{\nu}_R^i (H^T \tau_2 L_L^j) + \text{h.c.}$$

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As before

$$\Delta = \lambda_\nu^\dagger \lambda_\nu \quad \Delta \rightarrow V_L \Delta V_L^\dagger$$

but now not directly related to mass matrix

$$m_\nu = \frac{v^2}{M_\nu} \lambda_\nu^T \lambda_\nu$$

Implementation of MLFV in Extended Field Content Case

$$\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) + i \lambda_\nu^{ij} \bar{\nu}_R^i (H^T \tau_2 L_L^j) + \text{h.c.}$$

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As before

$$\Delta = \lambda_\nu^\dagger \lambda_\nu \quad \Delta \rightarrow V_L \Delta V_L^\dagger$$

but now not directly related to mass matrix

$$m_\nu = \frac{v^2}{M_\nu} \lambda_\nu^T \lambda_\nu$$

However

$$\delta = \lambda_\nu^T \lambda_\nu \quad \delta \rightarrow V_L^* \delta V_L^\dagger$$

Implementation of MLFV in Extended Field Content Case

$$\mathcal{L}_{\text{Sym.Br.}} = -\lambda_e^{ij} \bar{e}_R^i (H^\dagger L_L^j) + i \lambda_\nu^{ij} \bar{\nu}_R^i (H^T \tau_2 L_L^j) + \text{h.c.}$$

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As before

$$\Delta = \lambda_\nu^\dagger \lambda_\nu \quad \Delta \rightarrow V_L \Delta V_L^\dagger$$

but now not directly related to mass matrix

$$m_\nu = \frac{v^2}{M_\nu} \lambda_\nu^T \lambda_\nu$$

However

$$\delta = \lambda_\nu^T \lambda_\nu \quad \delta \rightarrow V_L^* \delta V_L^\dagger$$

In CP limit

$$\lambda_\nu^* = \lambda_\nu \quad \text{and} \quad \Delta = \lambda_\nu^T \lambda_\nu$$

- Same operator basis as before
(chose Δ and δ by transformation properties)
- Same effective lagrangian, but with $\Lambda_{\text{NL}} \rightarrow M_\nu$
- Summary: In mass eigenstate basis

$$\Delta = \begin{cases} \frac{\Lambda_{\text{LN}}^2}{v^4} U m_\nu^2 U^\dagger & \text{minimal field content} \\ \frac{M_\nu}{v^2} U m_\nu U^\dagger & \text{extended field content, CP limit} \end{cases}$$

$$\delta = \delta^T = \begin{cases} \frac{\Lambda_{\text{LN}}}{v^2} U^* m_\nu U^\dagger & \text{minimal field content} \\ \frac{M_\nu}{v^2} U^* m_\nu U^\dagger & \text{extended field content} \end{cases}$$

MLFV: Phenomenology

- Future experiments will (continue to) look for flavor changing neutral interactions in the charged lepton sector:
 - MECO ... was cancelled, but ... mu₂e
 - PRIME at the PRISM muon facility at JPARC will measure μ -to-e conversion at 10^{-18} sensitivity
 - MEG at PSI looks for $\mu^+ \rightarrow e^+ \gamma$ at 10^{-13} single event sensitivity

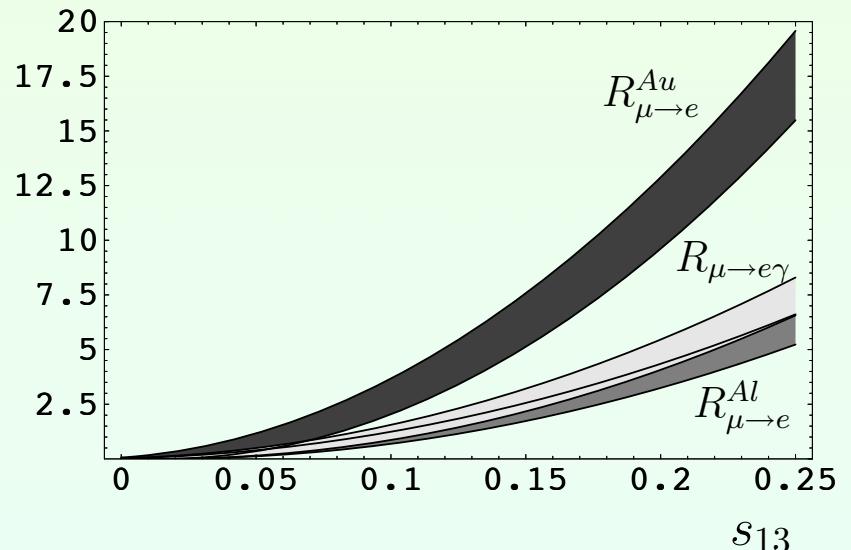


$\mu \rightarrow e\gamma$, μ -to- e conversion and their relatives I: minimal field content

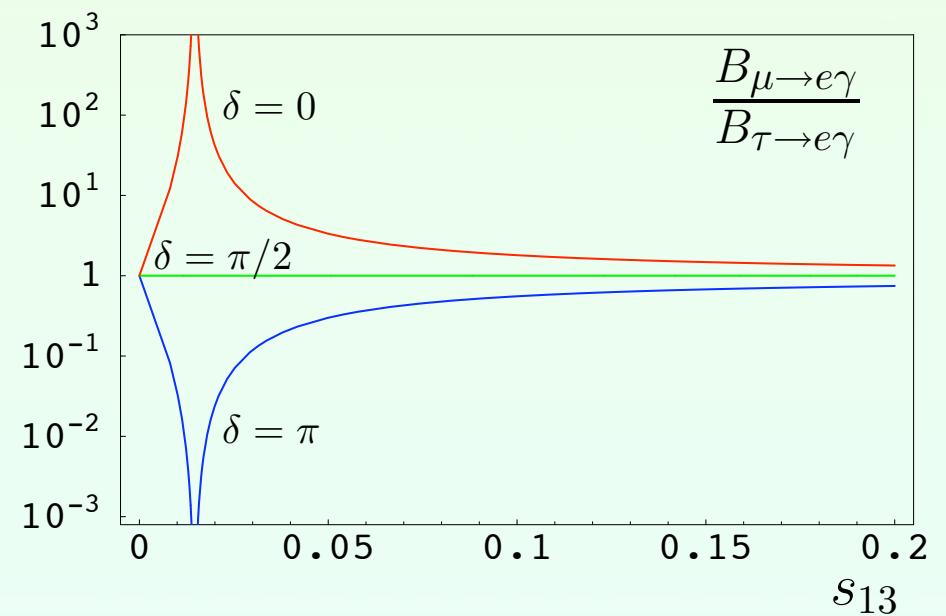
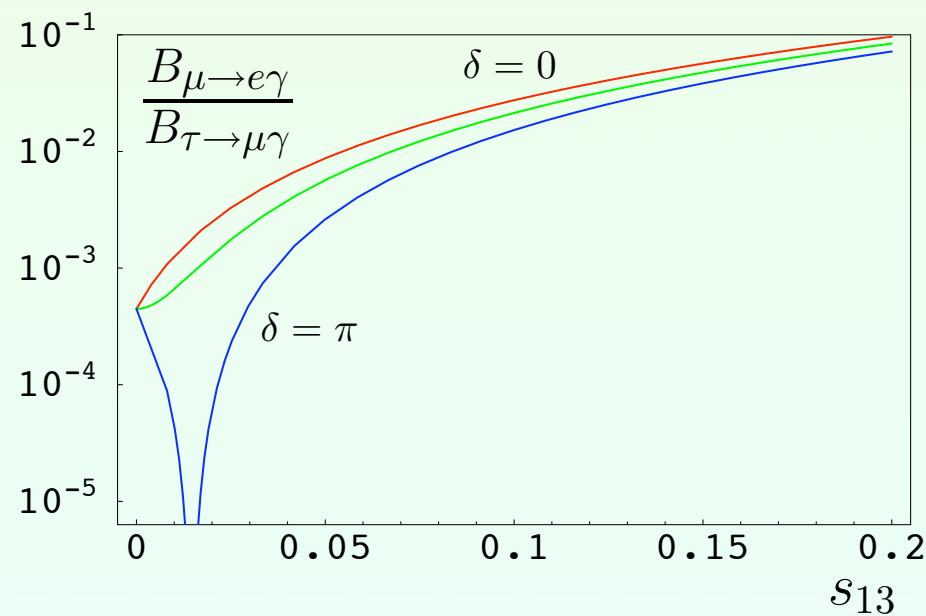
$$B_{\ell_i \rightarrow \ell_j(\gamma)} = 10^{-50} \left(\frac{\Lambda_{\text{LN}}}{\Lambda_{\text{LFV}}} \right)^4 R_{\ell_i \rightarrow \ell_j(\gamma)}(s_{13}, \delta; c^{(i)})$$

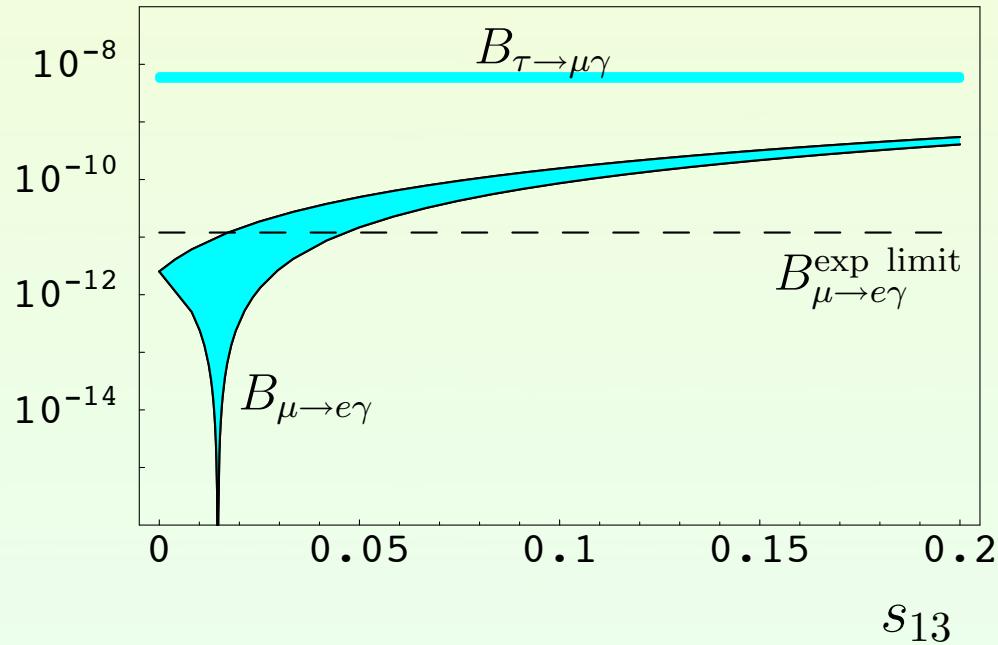
- since $\Delta \propto U(m_\nu)^2 U^\dagger$, only differences of m^2 enter; these are measured!

- s_{13} and δ unknown PMNS parameters (scan on δ)
- choose $c^{(i)}$ of order one for the estimate
- ratio of scales can be large:
perturbative $g_v \Rightarrow \Lambda_{\text{LN}} \lesssim 3 \times 10^{13} (1 \text{ eV}/m_\nu) \text{ GeV}$
so $\Lambda_{\text{LFV}} \sim 1 \text{ TeV} \Rightarrow \Lambda_{\text{LN}}/\Lambda_{\text{LFV}} \lesssim 10^{10}$



Predictive: $l \rightarrow l' \gamma$ patterns are independent of unknown input parameters (scales cancel in ratios, in this case $c^{(i)}$'s cancel too, and all other parameters are from long distance)





If s_{13} is small, look at tau modes.

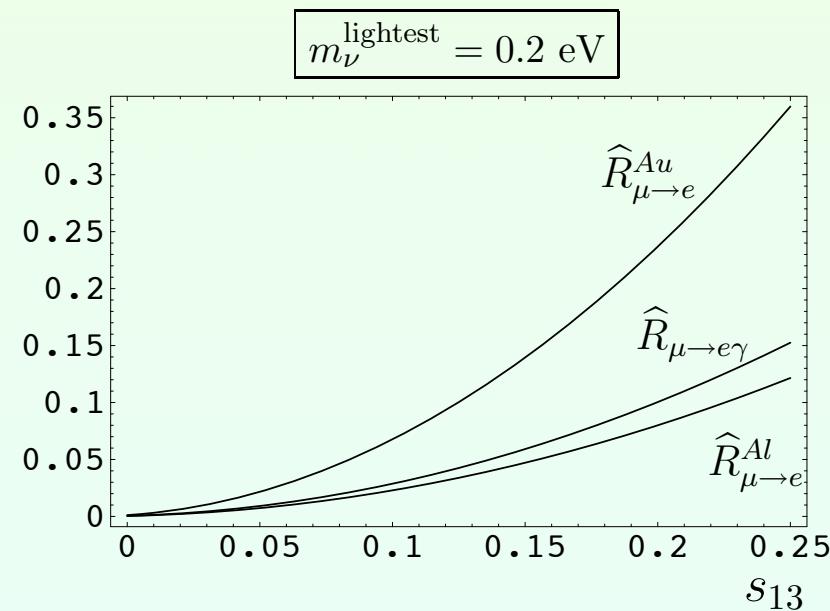
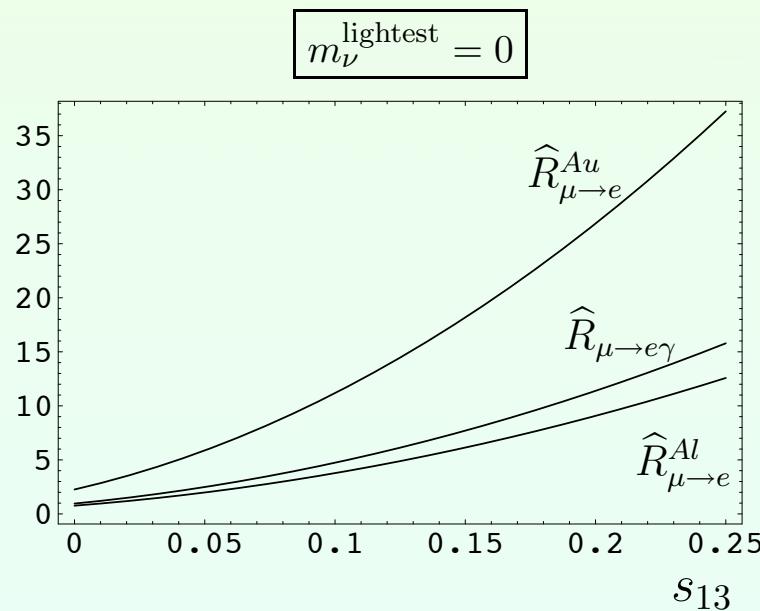
Here $\Lambda_{LN}/\Lambda_{LFV} = 10^{10}$ and $c_{RL}^{(1)} - c_{RL}^{(2)} = 1$

Belle and BaBar have recent bounds (summer '05)

of a few $\times 10^{-7}$ for $\text{Br}(\tau \rightarrow l\gamma)$ and $\text{Br}(\tau \rightarrow ll\bar{l})$

$\mu \rightarrow e\gamma$, μ -to- e conversion and their relatives II: extended field content

- Replace $\Lambda_{LN}^2/\Lambda_{LFV}^2$ by vM_ν/Λ_{LFV}^2
- Now $\Delta \propto U m_\nu U^\dagger$ so amplitudes depend on overall neutrino mass scale (ie, lightest neutrino mass)

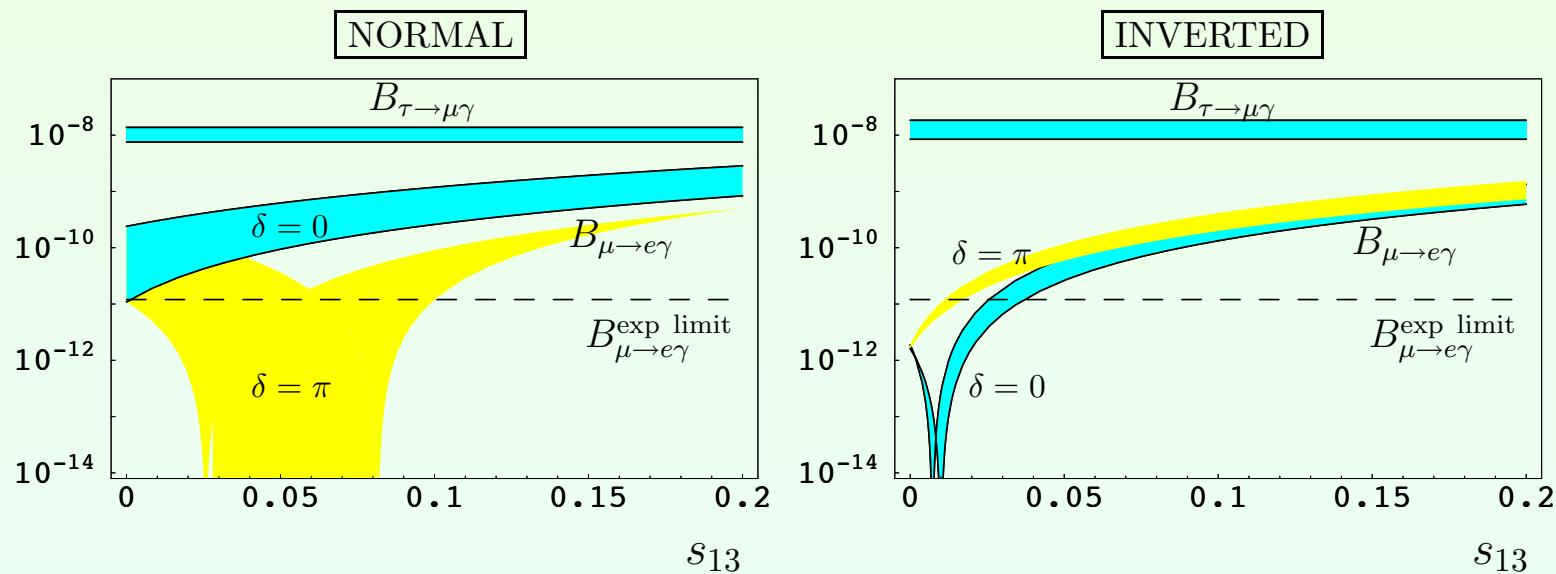


$$B_{\ell_i \rightarrow \ell_j(\gamma)} = 10^{-25} \left(\frac{v M_\nu}{\Lambda_{LFV}^2} \right)^2 \hat{R}_{\ell_i \rightarrow \ell_j(\gamma)}(s_{13}, m_\nu^{\text{lightest}}; c^{(i)})$$

perturbative $\lambda_v \Rightarrow M_v \lesssim 10^{13} \text{ GeV};$ with $\Lambda_{LFV} \geq 1 \text{ TeV},$

$$\frac{v M_\nu}{\Lambda_{LFV}^2} \leq 10^9$$

One final note: results depend on hierarchy of neutrino masses,
normal ($m_{\nu 1} \sim m_{\nu 2} \ll m_{\nu 3}$) vs. *inverted* ($m_{\nu 1} \ll m_{\nu 2} \sim m_{\nu 3}$)



$$(vM_\nu)/\Lambda_{\text{LFV}}^2 = 5 \times 10^7$$

$$c_{RL}^{(1)} - c_{RL}^{(2)} = 1$$

shading: $0 \leq m_\nu^{\text{lightest}} \leq 0.02 \text{ eV}$

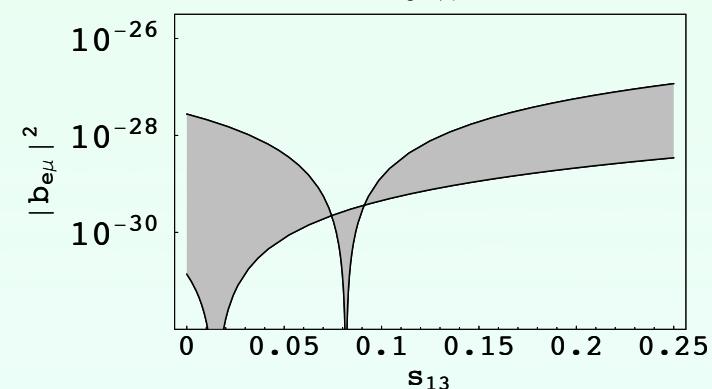
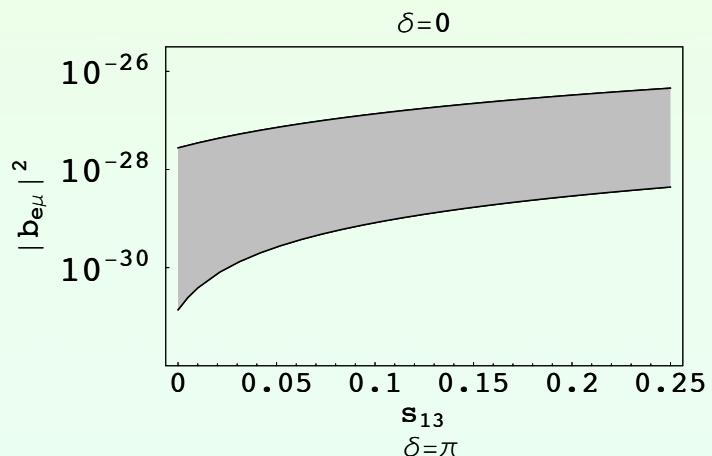
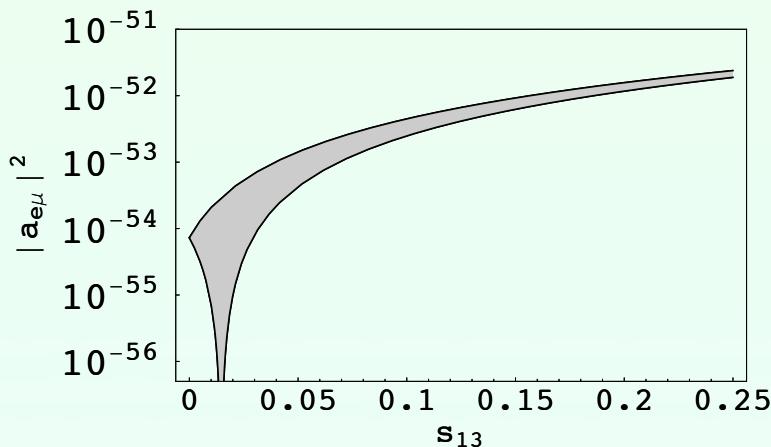
β^1 Decays: 4L operators

$$\Gamma_{\mu \rightarrow 3e} / \Gamma_{\mu \rightarrow e\nu\bar{\nu}} = \left[|a_+|^2 + 2|a_-|^2 - 8\text{Re}(a_0^* a_-) - 4\text{Re}(a_0^* a_+) + 6I|a_0|^2 \right] \begin{cases} \left(\frac{\Lambda_{\text{LN}}}{\Lambda_{\text{LFV}}} \right)^4 |a_{e\mu}|^2 & \text{minimal} \\ \left(\frac{v M_\nu}{\Lambda_{\text{LFV}}^2} \right)^2 |b_{e\mu}|^2 & \text{extended} \end{cases}$$

$$a_+ = \sin^2 \theta_w (c_{LL}^{(1)} + c_{LL}^{(2)}) + c_{4L}^{(3)}$$

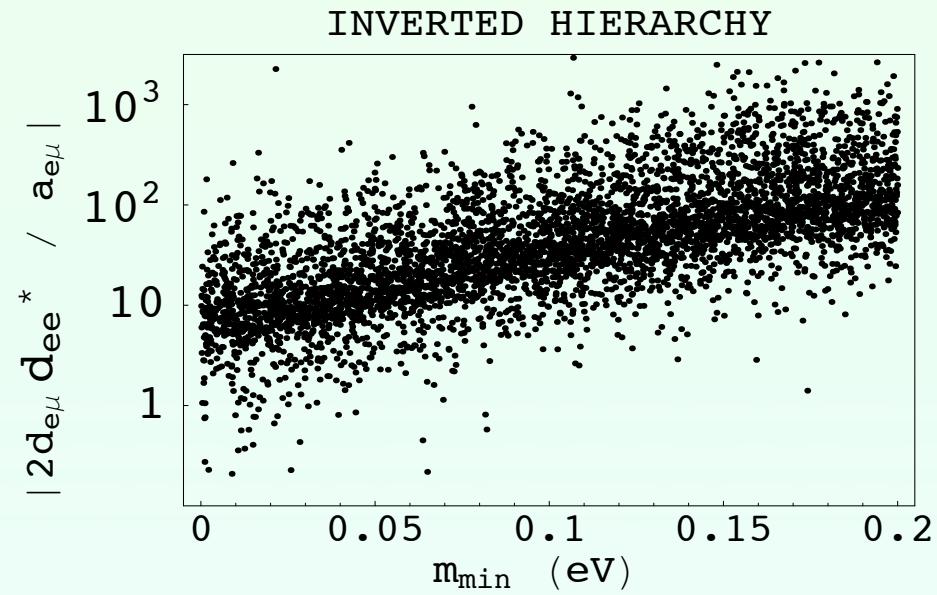
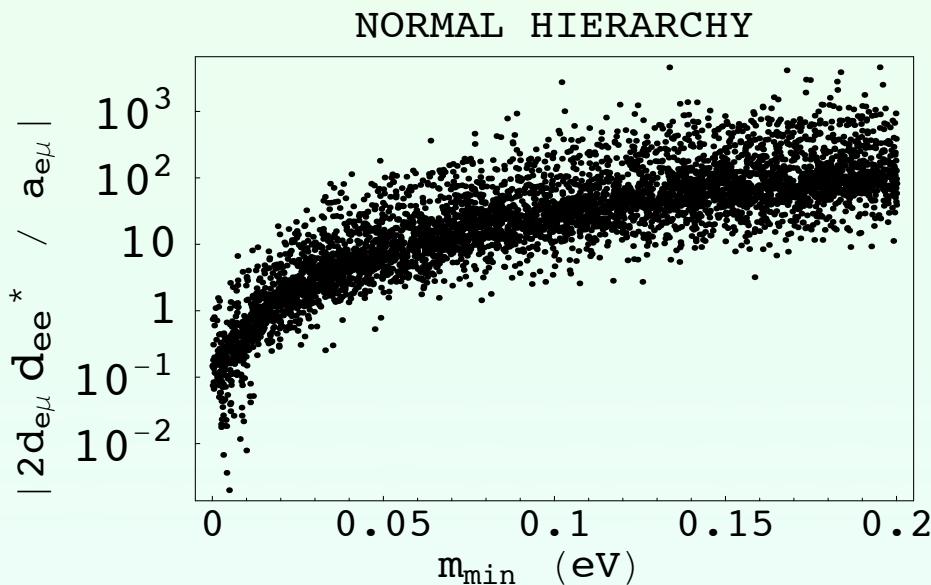
$$a_- = (\sin^2 \theta_w - \frac{1}{2})(c_{LL}^{(1)} + c_{LL}^{(2)}) + c_{4L}^{(1)} + c_{4L}^{(2)} + \frac{2\delta_{e\mu}\delta_{ee}^*}{\Delta_{e\mu}} (c_{4L}^{(4)} + c_{4L}^{(5)})$$

$$a_0 = 2e^2 (c_{RL}^{(1)} - c_{RL}^{(2)})^*$$

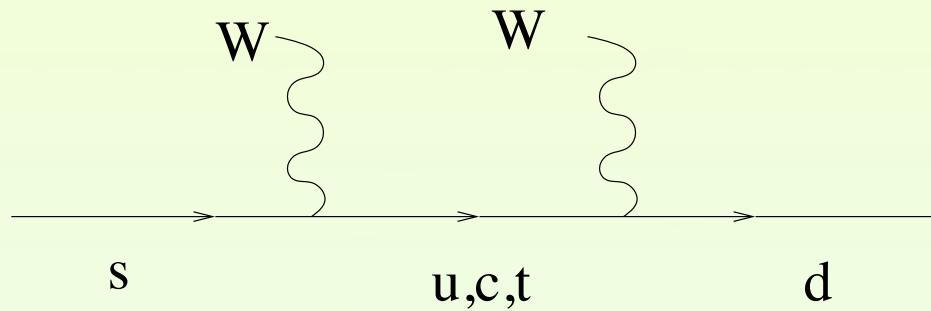


$$\Gamma_{\tau \rightarrow e \mu \bar{\mu}} = \Gamma_{\tau \rightarrow e \nu \bar{\nu}} \frac{v^4 |\Delta_{e\tau}|^2}{\Lambda_{\text{LFV}}^4} \left[|a_+|^2 + |\tilde{a}_-|^2 - 4\text{Re}[a_0^*(a_+ + \tilde{a}_-)] + 12\tilde{I}|a_0|^2 \right]$$

$$\Gamma_{\tau \rightarrow \mu \mu \bar{e}} = \Gamma_{\tau \rightarrow e \nu \bar{\nu}} \frac{v^4 |2\delta_{e\tau}\delta_{\mu\mu}|^2}{\Lambda_{\text{LFV}}^4} |c_L^{(4)} + c_L^{(5)}|^2$$



d_{xx} is δ_{xx}



Part of loop graph (W is virtual).

For any one intermediate quark amplitude is

$$M_W^D F(m_q^2/M_W^2, \mu/M_W)$$

Sum over intermediate quarks and expand

$$\sum_q V_{qd} V_{qs}^* F(m_q^2/M_W^2) \approx \sum_q V_{qd} V_{qs}^* \left[F(0) + \frac{m_q^2}{M_W^2} F'(0) + \dots \right]$$

For first term use

$$\sum_q V_{qd} V_{qs}^* = 0 \quad \text{and for second}$$

$$\sum_{q \neq u} V_{qd} V_{qs}^* = -V_{ud} V_{us}^*$$

$$\Rightarrow \sum_q m_q^2 V_{qd} V_{qs}^* = \sum_{q \neq u} (m_q^2 - m_u^2) V_{qd} V_{qs}^*$$

Decays of/to hadrons

Hopelessly small!

Br

$$\pi^0 \rightarrow \mu^+ e^- \quad 10^{-25}$$

$$\Upsilon \rightarrow \tau \mu \quad 10^{-20}$$

$$\tau \rightarrow \pi \mu \quad 10^{-15}$$

- We have also explored the effects of deleting a class of operators.
- For example: assume 4L operators are not present
- Can we get 3l decays? Yes, through loops
- Need care in loops of light quarks: chiral lagrangian does the job
- Result: amplitude is ~ 0.1 of 4L ops (large logs)
- Equivalently, these give a $\sim 20\%$ correction to rate
- Patterns are similar to those from 4L

