

Status and perspectives on loop-induced processes

Marek Schönherr

Universität Zürich

ATLAS–CMS Monte Carlo Generators Workshop



**Universität
Zürich**^{UZH}



FONDS NATIONAL SUISSE
SCHWEIZERISCHER NATIONALFONDS
FONDO NAZIONALE SVIZZERO
SWISS NATIONAL SCIENCE FOUNDATION

Disclaimer

I am an author of the SHERPA event generator, but I will try to keep that bias out of the following summary.

This review cannot be exhaustive, but I will focus on most important processes/process classes and recent developments/tools.

I will restrict myself to published results, with the implicit understanding that modern automated one-loop programs can calculate these processes without a dedicated publication.

Introduction

- Common signature $gg \rightarrow$ EW bosons
exceptions e.g. same sign top production etc.
- Distinguish two cases
 - 1) Loop-induced as sole production mode, e.g. $gg \rightarrow h$
→ few cases with EFT approximation
 - 2) Tree-level production in $q\bar{q}$ dominant
→ gauge invariant subset of NNLO calculation
→ no guarantee that dominant part of NNLO correction
- Important production mechanism even if tree-level production exists
→ scales with $gg/q\bar{q}$ luminosities
- Implementations available in many parton level gens (MCFM, etc.)
→ will focus on particle level implementations
- when $q\bar{q}$ exists, then part of NNLO codes (for VV , VH etc.)
- Generally known only at LO, at most estimates of NLO corrections

Higgs production in gluon fusion

- for inclusive ggh coupling HEFT working well, correction to loop-induced flat and incorporated in every implementation
 - for $pp \rightarrow h + n$ jets HEFT good enough to be reweighted $\rightarrow \mathcal{O}(1)$ corrections throughout phase space
- \Rightarrow can be incorporated in all the multijet merged at NLO machinery available for HEFT
- available in MADGRAPH, OPENLOOPS, GOSAM

Hirschi, Mattelaer JHEP10(2015)146

Process	Syntax	Cross section (pb)	$\Delta_{\hat{\mu}}$	Δ_{PDF}	Ref.
Single boson + jets		$\sqrt{s} = 13$ TeV			
a.1 $pp \rightarrow H$	$p p > h$ [QCD]	17.79 ± 0.060	+31.3%	+0.5%	[49]
a.2 $pp \rightarrow H j$	$p p > h j$ [QCD]	12.86 ± 0.030	-23.1%	-0.9%	[49]
a.3 $pp \rightarrow H j j$	$p p > h j j$ QED=1 [QCD]	6.175 ± 0.020	+42.3%	+0.6%	[49]
\dagger d.1 $pp \rightarrow H j j j$	$p p > h j j j$ QED=1 [QCD]	2.519 ± 0.005	-27.7%	-0.9%	[49]
			+61.8%	+0.7%	[62]
			-35.6%	-0.9%	
			+75.1%	+0.6%	
			-39.8%	-0.6%	

Higgs production in gluon fusion

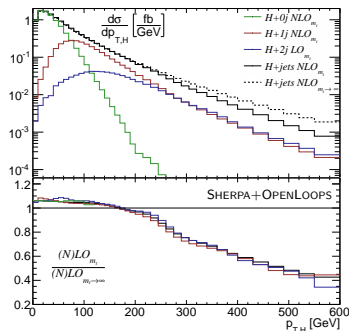
Buschmann, Goncalves, Kuttimalai, MS, Krauss, Plehn JHEP02(2015)038

$pp \rightarrow H + \text{jets production (ggF)}$

- correction factor/weight

$$r_t^{(n)} = \frac{|\mathcal{M}^{(n)}(m_t)|^2}{|\mathcal{M}^{(n)}(m_t \rightarrow \infty)|^2}$$

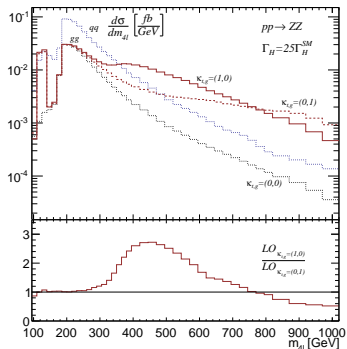
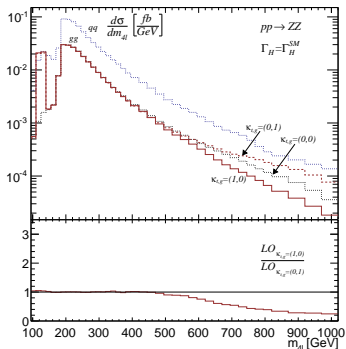
- loops from OPENLOOPS
- construct MEPS@NLO from reweighted S-MC@NLO
- factorised approach for unknown top mass dependence in V_n , otherwise exact NLO mass dependence



$$d\sigma_n = d\Phi_n r_t^{(n)} \left[B_n + V_n + \int d\Phi_1 D_n \right] \widetilde{\text{PS}}_n + d\Phi_{n+1} \left[r_t^{(n+1)} R_n - r_t^{(n)} D_n \right]$$

Interference in Higgs production

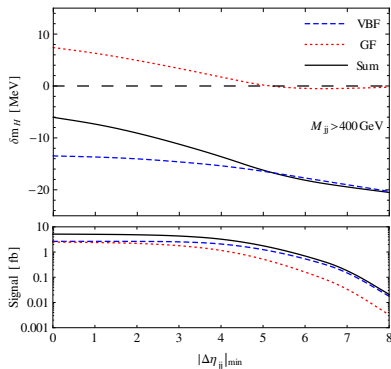
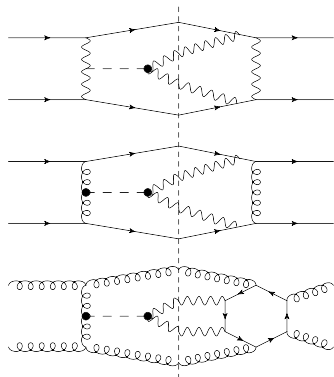
Buschmann, Goncalves, Kuttimalai, MS, Kraus, Plehn JHEP02(2015)038



investigate new physics in $pp \rightarrow 4\ell, q\bar{q} @ NLO, gg @ LO$
 parametrised in κ framework, SM: $(\kappa_t, \kappa_g) = (1, 0)$

Interference in Higgs production

Coradeschi, de Florian, Dixon, Fidanza, Höche, Ita, Li, Mazzitelli PRD92(2015)013004

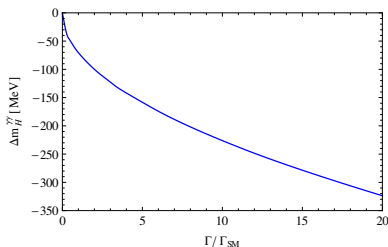
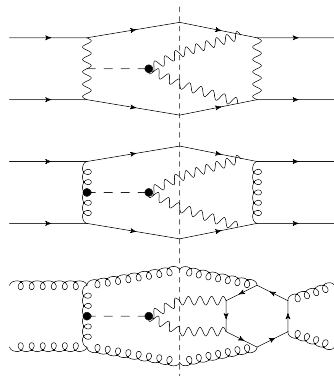


mass shift in $m_{\gamma\gamma}$ in VBF/GF-background interference

quickly increases with Γ_H

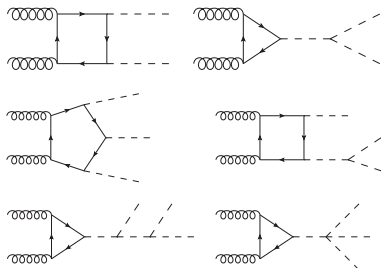
Interference in Higgs production

Coradeschi, de Florian, Dixon, Fianza, Höche, Ita, Li, Mazzitelli PRD92(2015)013004



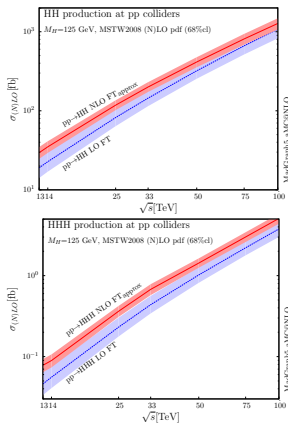
mass shift in $m_{\gamma\gamma}$ in VBF/GF-background interference
quickly increases with Γ_H

Double/Triple Higgs production in gluon fusion



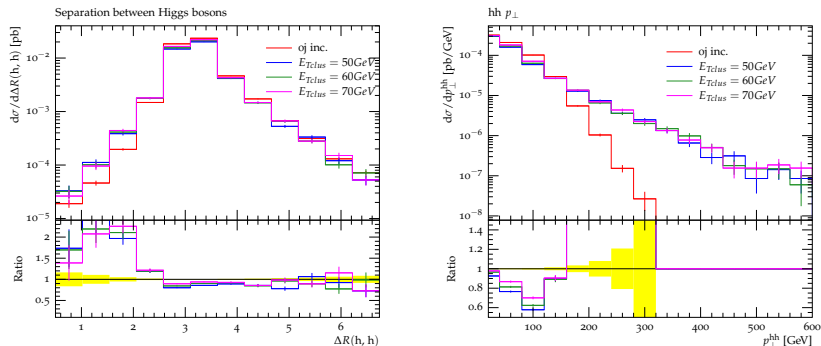
- reweight in $d\Phi_B$ with r_t^B ,
in $d\Phi_R$ with r_t^R
- factorised approach for virtual corrections

Maltoni, Vryonidou, Zaro JHEP11(2014)079



Double Higgs production in gluon fusion

Maierhöfer, Papaefstathiou JHEP03(2014)126



- LO merging for $pp \rightarrow hh + 0, 1$ jets in MLM scheme
- use exact loop-induced, no reweighting
- using HERWIG++ + OPENLOOPS

Associated Higgs production

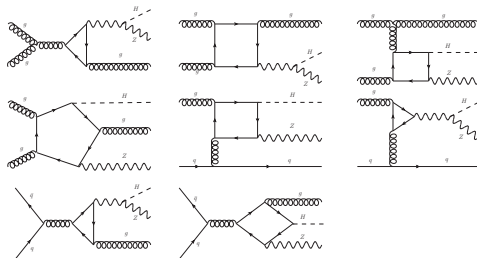
- only $gg \rightarrow HZ$, $gg \rightarrow HZg$, $gq \rightarrow HZq$ and $gg \rightarrow H\gamma g$
- relative size of contribution strongly dependent on observable

Hirschi, Mattelaer JHEP10(2015)146

Process	Syntax	Cross section (pb)	$\Delta_{\hat{\mu}}$	Δ_{PDF}	Ref.
Double bosons + jet		$\sqrt{s} = 13 \text{ TeV}$			
*b.3 $pp \rightarrow H\gamma j$	$p p > h a j$ [QCD]	$4.225 \pm 0.006 \cdot 10^{-3}$	+38.6%	+0.4%	[52]
*b.4 $gg \rightarrow HZ$	$g g > h z$ [QCD]	$6.537 \pm 0.030 \cdot 10^{-2}$	-25.9%	-0.7%	[53]
*b.5 $gg \rightarrow HZg$	$g g > h z g$ [QCD]	$5.465 \pm 0.020 \cdot 10^{-2}$	+29.4%	+1.0%	[52]
			-21.3%	-1.1%	
			+46.0%	+1.2%	[52]
			-29.4%	-1.3%	

Associated Higgs production

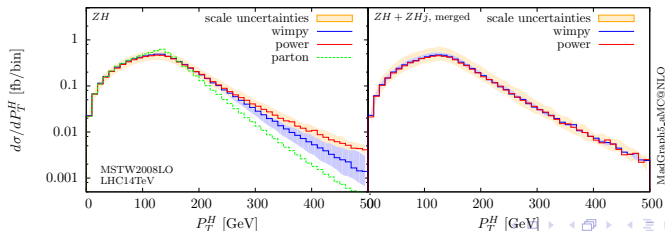
Hespel, Maltoni, Vryonidou JHEP06(2015)065



MLM merge loop-induced
ZH production

$gg \rightarrow ZH$

$gg \rightarrow ZHq$ and $gq \rightarrow ZHq$

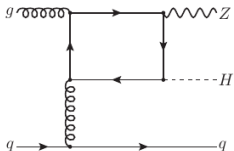


Associated Higgs production

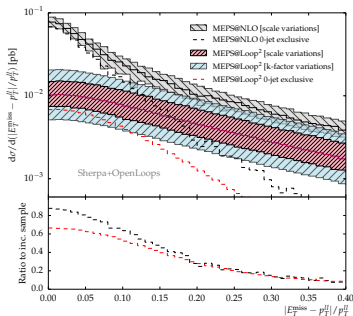
Goncalves, Krauss, Kuttimalai, Maierhöfer PRD92(2015)7,073006

$pp \rightarrow \ell\ell H + \text{jets production}$

- MEPS@NLO for $q\bar{q}$
MEPS@LOOP² for gg
- care for $qg \rightarrow ZHq$:



- part of NLO ZHj
- in loop-induced as gauge inv. subset of NNLO ZHj



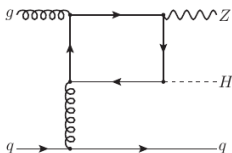
$pp \rightarrow Z[\rightarrow \ell\ell]H[\rightarrow \text{inv}] + \text{jets}$

Associated Higgs production

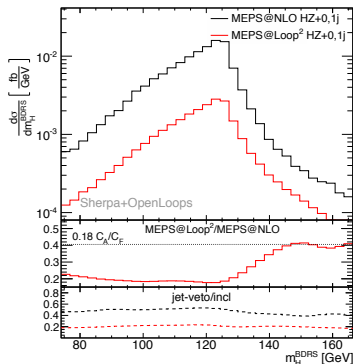
Goncalves, Krauss, Kuttimalai, Maierhöfer PRD92(2015)7,073006

$pp \rightarrow \ell\ell H + \text{jets}$ production

- MEPS@NLO for $q\bar{q}$
MEPS@LOOP² for gg
- care for $qg \rightarrow ZHq$:



- part of NLO ZHj
- in loop-induced as gauge inv. subset of NNLO ZHj



$pp \rightarrow Z[\rightarrow \ell\ell] H[\rightarrow b\bar{b}] + \text{jets}$

Vector boson pair production

- relative size of contribution strongly dependent on observable, but typically $< 10\%$

Hirschi, Mattelaer JHEP10(2015)146

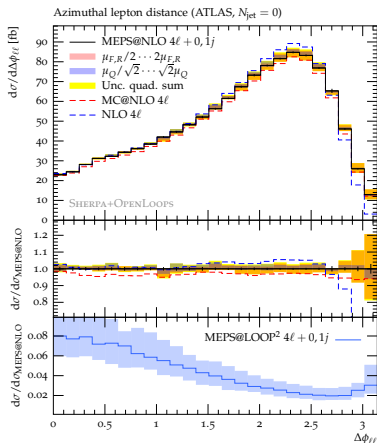
Process	Syntax	Cross section (pb)	$\Delta_{\hat{\mu}}$	Δ_{PDF}	Ref.
Double bosons + jet		$\sqrt{s} = 13 \text{ TeV}$			
b.6	$gg \rightarrow ZZ$	$g g > z z$ [QCD]	1.313 ± 0.004	+27.1% +0.7% -20.1% -1.0%	[42]
*b.7	$gg \rightarrow ZZg$	$g g > z z g$ [QCD]	0.6361 ± 0.002	+45.4% +1.0% -29.1% -1.2%	[54]
b.8	$gg \rightarrow Z\gamma$	$g g > z a$ [QCD]	1.265 ± 0.0007	+30.2% +0.6% -22.2% -1.0%	[42]
*b.9	$gg \rightarrow Z\gamma g$	$g g > z a g$ [QCD]	0.4604 ± 0.001	+43.7% +0.8% -28.4% -1.1%	[55]
b.10	$gg \rightarrow \gamma\gamma$	$g g > a a$ [QCD]	$5.182 \pm 0.010 \cdot 10^{+2}$	+72.3% +1.0% -43.4% -1.3%	[42]
*b.11	$gg \rightarrow \gamma\gamma g$	$g g > a a g$ [QCD]	19.22 ± 0.030	+59.7% +0.7% -35.7% -1.0%	[56]
b.12	$gg \rightarrow W^+W^-$	$g g > w^+ w^-$ [QCD]	4.099 ± 0.010	+26.5% +0.7% -19.7% -1.0%	[57]
*b.13	$gg \rightarrow W^+W^-g$	$g g > w^+ w^- g$ [QCD]	1.837 ± 0.004	+45.2% +0.9% -29.0% -1.1%	[58]

Vector boson pair production

Cascoli, Höche, Krauss, Maierhöfer, Pozzorini, Siegert arXiv:1309.5912

$pp \rightarrow 4\ell + 0, 1$ jets
and $pp \rightarrow 2\ell 2\nu + 0, 1$ jets

- MEPS@NLO for $q\bar{q}$
MEPS@LOOP² for gg
- includes loop-induced
 $gg \rightarrow 4\ell$,
 $gg \rightarrow 4\ell + g$, $gq \rightarrow 4\ell + q$,
 $q\bar{q} \rightarrow 4\ell + g$

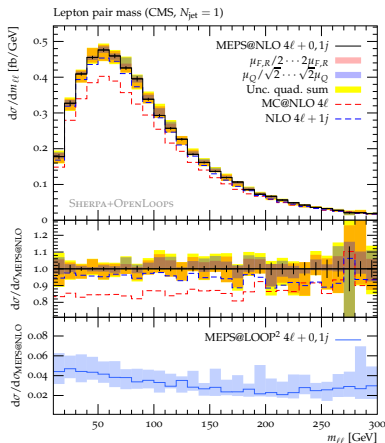


Vector boson pair production

Cascioli, Höche, Krauss, Maierhöfer, Pozzorini, Siegart arXiv:1309.5912

$pp \rightarrow 4\ell + 0, 1$ jets
and $pp \rightarrow 2\ell 2\nu + 0, 1$ jets

- MEPS@NLO for $q\bar{q}$
MEPS@LOOP² for gg
- includes loop-induced
 $gg \rightarrow 4\ell$,
 $gg \rightarrow 4\ell + g$, $gq \rightarrow 4\ell + q$,
 $q\bar{q} \rightarrow 4\ell + g$



Multiboson production

- many process, generally very small cross section

Hirschi, Mattelaer JHEP10(2015)146

Process	Syntax	Cross section (pb)	$\Delta_{\hat{\mu}}$	Δ_{PDF}	Ref.
Triple bosons					
$\sqrt{s} = 13 \text{ TeV}$					
*c.1 $pp \rightarrow HHH$	$p p > h h h$ [QCD]	$3.968 \pm 0.010 \cdot 10^{-5}$	+31.8%	+1.4%	[59]
†c.2 $gg \rightarrow HHZ$	$g g > h h z$ [QCD]	$5.260 \pm 0.009 \cdot 10^{-5}$	-22.6%	-1.4%	[-]
†c.3 $gg \rightarrow HZZ$	$g g > h z z$ [QCD]	$1.144 \pm 0.004 \cdot 10^{-4}$	+31.2%	+1.3%	[-]
†c.4 $gg \rightarrow HZ\gamma$	$g g > h z a$ [QCD]	$6.190 \pm 0.020 \cdot 10^{-6}$	-22.2%	-1.3%	[-]
†c.5 $pp \rightarrow H\gamma\gamma$	$p p > h a a$ [QCD]	$6.058 \pm 0.004 \cdot 10^{-6}$	+31.1%	+1.2%	[-]
*c.6 $gg \rightarrow HW^+W^-$	$g g > h w^+ w^-$ [QCD]	$2.670 \pm 0.007 \cdot 10^{-4}$	-22.2%	-1.3%	[60]
†c.7 $gg \rightarrow ZZZ$	$g g > z z z$ [QCD]	$6.964 \pm 0.009 \cdot 10^{-5}$	+30.9%	+1.2%	[-]
†c.8 $gg \rightarrow ZZ\gamma$	$g g > z z a$ [QCD]	$3.454 \pm 0.010 \cdot 10^{-6}$	-22.1%	-1.3%	[-]
*c.9 $gg \rightarrow Z\gamma\gamma$	$g g > z a a$ [QCD]	$3.079 \pm 0.005 \cdot 10^{-4}$	+28.7%	+0.9%	[61]
†c.10 $gg \rightarrow ZW^+W^-$	$g g > z w^+ w^-$ [QCD]	$8.595 \pm 0.020 \cdot 10^{-3}$	-20.9%	-1.1%	[-]
†c.12 $gg \rightarrow \gamma W^+W^-$	$g g > a w^+ w^-$ [QCD]	$1.822 \pm 0.005 \cdot 10^{-2}$	+28.0%	+0.7%	[-]
			-20.9%	-1.1%	[-]

Tools

Process specific tools:

- $gg2VV+HERWIG/PYTHIA$

[Kauer JHEP12\(2013\)082](#)

- $gg \rightarrow 2l2\nu, 4l$

⋮

General tools:

- $MADGRAPH+HERWIG/PYTHIA$

[Hirschi, Mattelaer JHEP10\(2015\)146](#)

- all on-shell $2 \rightarrow 2$ and $2 \rightarrow 3$ processes, some $2 \rightarrow 4$ in SM
- MLM merging possible with PYTHIA6

- $SHERPA+OPENLOOPS$

[several publications](#)

- all off-shell $2 \rightarrow 2$ and $2 \rightarrow 3$, e.g. $gg \rightarrow 4lg$
- MEPS@LOOP² merging possible

Timings – MADGRAPH

Timing for 10k unweighted events (number of phase space points needed)

Helicity sum	Monte-Carlo	Exact	
Loop Reduction	CUTTOOLS	CUTTOOLS	TIR
Survey			
$pp \rightarrow hj$	13m (125k)	32m (260k)	9m (260k)
$pp \rightarrow hjj$	2d4h (1.2M)	16d10h (5.4M)	9d13h (5.4M)*
$gg \rightarrow zz$	1h06m (34k)	12h50m (255k)	1h44m (255k)
$gg \rightarrow zhg$	11h13m (110k)	1d8h (516k)	1d4h (516k)*
Refine			
$pp \rightarrow hj$	1h43m (385k)	23m (431k)	6m (431k)
$pp \rightarrow hjj$	7d17h (2.18M)	75d1h (20.6M)	51d19h (20.6M)*
$gg \rightarrow zz$	7h20m (407k)	4d13h (4.55M)	23h07m (5.78M)
$gg \rightarrow zhg$	23h03m (277k)	2d22h (1.13M)	3d14h (1.4M)*

Timings – OPENLOOPS

Timing per phase space point using COLLIER

Process	ms/point	Process	ms/point	Process	ms/point
$gg \rightarrow h$	0.11	$gg \rightarrow hh$	1.3		
$gg \rightarrow hg$	1.6	$gg \rightarrow hhg$	47	$gg \rightarrow \gamma g$	2.7
$gg \rightarrow hgg$	50			$gg \rightarrow \gamma gg$	117
$gg \rightarrow he^+e^-$	2.0	$gg \rightarrow e^+e^-$	0.28	$gg \rightarrow e^+e^-\gamma$	4.3
$gg \rightarrow he^+e^-g$	61	$gg \rightarrow e^+e^-g$	4.9	$gg \rightarrow e^+e^-\gamma g$	128

Process	ms/point	Process	ms/point
$gg \rightarrow e^+e^-\mu^+\mu^-$	8.9	$gg \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu$	2.0
$gg \rightarrow e^+e^-\mu^+\mu^-g$	238	$gg \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu g$	72
$gg \rightarrow e^+e^-e^+e^-$	25	$gg \rightarrow e^+\nu_e e^-\bar{\nu}_e$	6.2
$gg \rightarrow e^+e^-e^+e^-g$	638	$gg \rightarrow e^+\nu_e e^-\bar{\nu}_e g$	202

Conclusion

- all processes in SM available by several tools
process specific, MADGRAPH+HERWIG/PYTHIA,
SHERPA+OPENLOOPS, SHERPA+GOSAM
- improve EFT used otherwise
include important subleading process where $q\bar{q}$ channel exists,
 gg has different properties
calculate signatures inaccessible otherwise
- NLO corrections are two-loop, usually with many mass scales
→ generally not available
- NLO K -factors are estimated to be large ≈ 2
- selected BSM processes appeared in the literature
- timings/efficiencies vary between tools

Thank you for your attention!