



# NLOs matching and multijet merging

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JHEP04(2013)027, JHEP01(2013)144

arXiv:1401.7971, arXiv:1402.6293, arXiv:1403.4788\*

LHCphenOnet




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\*in coll. with S. Höche, F. Krauss, P. Maierhöfer, S. Pozzorini, F. Siegert, J. Thompson, K. Zapp



# The SHERPA event generator framework

- Two multi-purpose Matrix Element (ME) generators

**AMEGIC++** JHEP02(2002)044, EPJC53(2008)501

**COMIX** JHEP12(2008)039, PRL109(2012)042001

- A Parton Shower (PS) generator

**CSSHOWER++** JHEP03(2008)038

- A multiple interaction simulation à la Pythia

**AMISIC++** hep-ph/0601012

- A cluster fragmentation module

**AHADIC++** EPJC36(2004)381

- A hadron and  $\tau$  decay package

**HADRONS++**

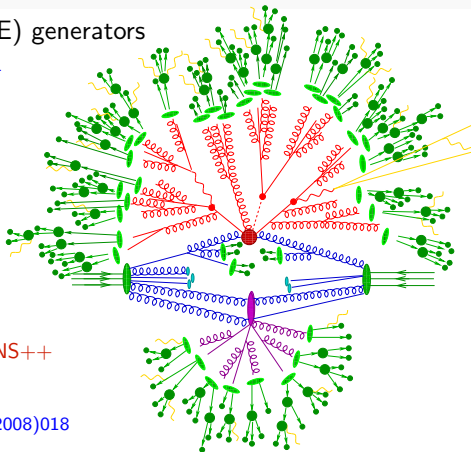
- A higher order QED generator using

YFS-resummation **PHOTONS++** JHEP12(2008)018

- A minimum bias simulation **SHRiMPS** to appear

**Sherpa's traditional strength is the perturbative part of the event**

MEPs (CKKW), S-Mc@NLO, MENLOs, MEPs@NLO



# Contents

## ① General NLOPS matching

Resummation properties of parton showers

NLOPS matching

Case study

## ② Multijet merging

MEPS – Multijet merging at leading order

MEPS@NLO – Multijet merging at next-to-leading order

Results

## ③ Conclusions



# Introduction

Importance of matching NLO calculations with parton showers

- exclusive final states
- observable independent combination of fixed order and resummation
- problem double counting: both NLO and PS are approximations to higher order corrections → MC@NLO and POWHEG

Importance of multijet merging

- simultaneous description multijet topologies  
→ every jet multiplicity at same fixed order accuracy
- resum hierarchies in emission scales

Uncertainties of NLOs matching/MEPS@NLO merging

- usual  $\mu_R$  and  $\mu_F$  variation as in NLO calculations
- also  $\mu_Q$ -variation as in analytic resummations



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# Resummation properties of parton showers

$$d\sigma^{\text{LO}^{\text{PS}}} = d\Phi_B B(\Phi_B) \left[ \Delta^{(\mathcal{K})}(t_c, \mu_Q^2) + \sum_i \int_{t_c}^{\mu_Q^2} d\Phi_1 \mathcal{K}_i \Delta^{(\mathcal{K})}(t, \mu_Q^2) \right]$$

- splitting kernel  $\mathcal{K}_n = \sum \mathcal{K}_i$  and  $\mathcal{K}_i(\Phi_1) \propto \frac{\alpha_s}{t} P_i(z)$ ,  $\Phi_1 = \{t, z, \phi\}$
- Sudakov form factor

$$\Delta^{(\mathcal{K})}(t, t') = \exp \left[ - \int_t^{t'} d\Phi_1 \mathcal{K}_n \right] = \exp [c_1 \alpha_s L^2 + c_2 \alpha_s L + \dots]$$

- parton shower starting scale  $\mu_Q$  plays role of resummation scale, at LO commonly identified with  $\mu_F$  to recover PDF evolution
- resummation in evolution variable  $t$ ,  $c_1$  correctly described,  $c_2$  at most in  $N_c \rightarrow \infty$  approximation
- 1-loop running  $\alpha_s \rightarrow \alpha_s(k_\perp)$  catches dominant terms of higher log. order  $\Rightarrow$  **crucial in defining “parton shower accuracy”**



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# Resummation properties of parton showers

Choices:

- precise definition of evolution variable,  
only needs to behave as  $\frac{dt}{t} = \frac{dp_{\perp}^2}{p_{\perp}^2}$  in the collinear limit  
→  $p_{\perp}^2, \theta, \tilde{p}_{\perp}^2, \dots$
- recoil scheme, only needs to be IR-safe  
→ at most power corrections, but can be numerically sizeable
- power corrections and finite terms in splitting functions  
→ (generalised) matrix element corrections
- $\alpha_s$ -running beyond 1-loop  
→ fix 1-loop running to  $\alpha_s(k_{\perp})$  by counterterm
- $g \rightarrow q\bar{q}$  splittings have no LL, free to choose  $\alpha_s$ -scale

⇒ **PS formulated probabilistically, no simple reweighting to other choices**



# NLOs matching

- NLO calculation matched to shower-like resummation

$$d\sigma^{\text{NLO}^{\text{PS}}} = d\Phi_B \left[ B + V + \sum_i \int d\Phi_1^i D_i^{(A)} \Theta(\mu_Q^2 - t) \right] \\ + d\Phi_R \left[ R - \sum_i D_i^{(A)} \Theta(\mu_Q^2 - t) \right]$$

- introduce set of resummation kernels  $D_i^{(A)}$   
 → needs to reproduce  $N_c = 3$  IR limits
- modified shower resummation with

$$\Delta^{(A)}(t, t') = \sum_i \int_t^{t'} d\Phi_1 \frac{D_i^{(A)}}{B}$$

- matching methods differ in choice of  $D_i^{(A)}$  and  $\mu_Q$



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# NLOs matching

POWHEG (e.g. in POWHEG-BOX, HERWIG++, SHERPA-1.3.x):

- $D_i^{(A)} = \rho_i \cdot R$ ,  $\mu_Q^2 = \frac{1}{2} s_{\text{had}}$  [Nason JHEP11\(2004\)040](#), [Frixione et.al. JHEP11\(2007\)070](#)
- modify kernels by  $f(p_\perp) = h^2/(p_\perp^2 + h^2)$  to emulate an upper limit on resummation phase space [Alioli et.al. JHEP04\(2009\)002](#)

MC@NLO (traditional scheme, e.g. in MC@NLO, aMC@NLO ):

- $D_i^{(A)} = B \cdot \mathcal{K}_i$ ,  $\mu_Q^2 = t_{\text{max}}$  [Frixione, Webber JHEP06\(2002\)029](#)
- modify soft limit by suitable  $f(p_\perp)$  such that  $N_c = 3$  limit reproduced [Frixione, Nason, Webber JHEP08\(2003\)007](#)

S-MC@NLO ( $N_c = 3$ -PS step, e.g. in SHERPA-1.4.x/2.x.y):

- $D_i^{(A)} = D_i^{(S)}$ ,  $\mu_Q^2 = t_{\text{max}}$  [Höche, Krauss, MS, Siegert JHEP09\(2012\)049](#)
- necessitates weighted shower as  $D_i^{(A)}$  not positive definite

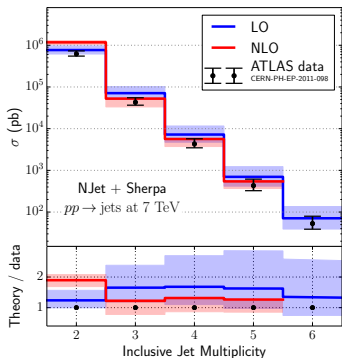


# Case study: Inclusive jet & dijet production

Badger, Biedermann, Uwer, Yundin Phys.Rev.D89(2014)034019

NLO:

- poor description in phase space regions with strongly hierarchical scales
- poor perturbative jet-modeling (at most two constituents)
- no hadronisation, MPI effects
- jet- $p_{\perp}$  turn negative in forward region unless  $y$ -dependent scale is used (e.g.  $H_T^{(y)}$ )



no. jets	ATLAS	LO	ME+PS	NLO	NP factor	NLO+NP
$\geq 2$	$620 \pm 1.3^{+110}_{-66} \pm 24$	$958(1)^{+316}_{-221}$	559(5)	$1193(3)^{+130}_{-135}$	0.95(0.02)	$1130(19)^{+124}_{-129}$
$\geq 3$	$43 \pm 0.13^{+12}_{-6.2} \pm 1.7$	$93.4(0.1)^{+50.4}_{-30.3}$	39.7(0.9)	$54.5(0.5)^{+2.2}_{-19.9}$	0.92(0.04)	$50.2(2.1)^{+2.0}_{-18.3}$
$\geq 4$	$4.3 \pm 0.04^{+1.4}_{-0.79} \pm 0.24$	$9.98(0.01)^{+7.40}_{-3.95}$	3.97(0.08)	$5.54(0.12)^{+0.08}_{-2.44}$	0.92(0.05)	$5.11(0.29)^{+0.08}_{-2.32}$

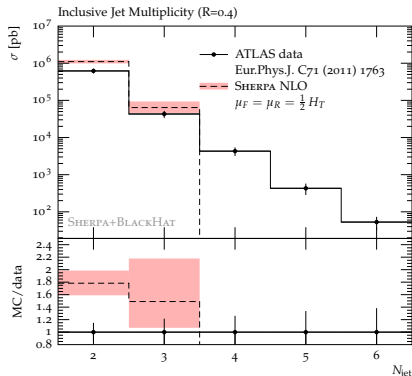
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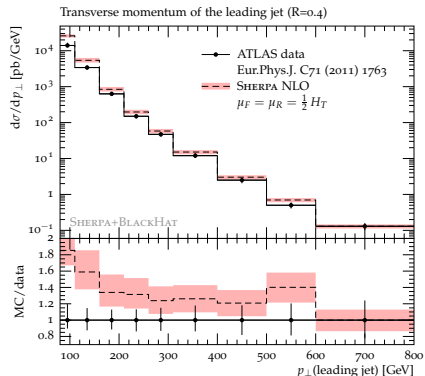
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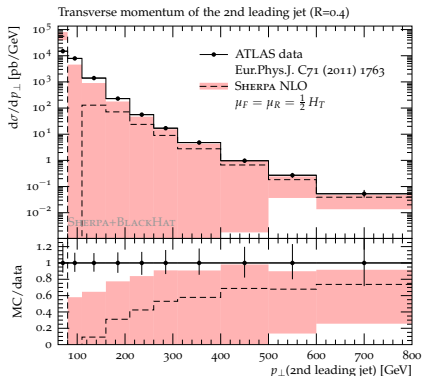
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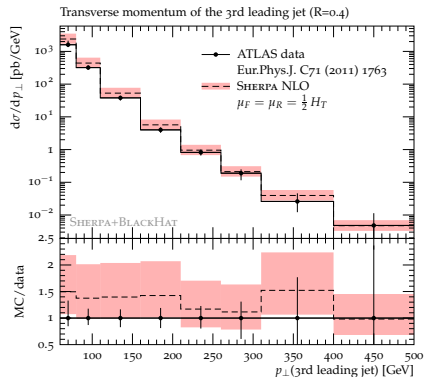
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Bern et al. Phys.Rev.Lett.109(2012)042001

## Case study: Inclusive jet & dijet production

Describe wealth of experimental data with a single sample (LHC@7TeV)

MC@NLO di-jet production:

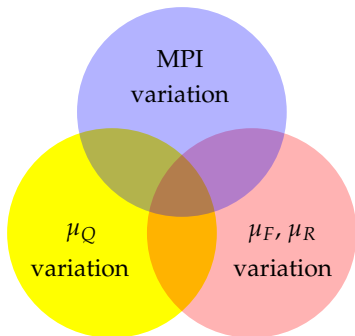
Höche, MS Phys.Rev.D86(2012)094042

- $\mu_{R/F} = \frac{1}{4} H_T$ ,  $\mu_Q = \frac{1}{2} p_{\perp}$
- CT10 PDF ( $\alpha_s(m_Z) = 0.118$ )
- hadron level calculation, MPI
- virtual MEs from BLACKHAT  
Giele, Glover, Kosower  
Nucl.Phys.B403(1993)633-670  
Bern et.al. arXiv:1112.3940

- $p_{\perp}^{j1} > 20$  GeV,  $p_{\perp}^{j2} > 10$  GeV

Uncertainty estimates:

- $\mu_{R/F} \in [\frac{1}{2}, 2] \mu_{R/F}^{\text{def}}$
- $\mu_Q \in [\frac{1}{\sqrt{2}}, \sqrt{2}] \mu_Q^{\text{def}}$
- MPI activity in tr. region  $\pm 10\%$





## Case study: Inclusive jet & dijet production

Describe wealth of experimental data with a single sample (LHC@7TeV)

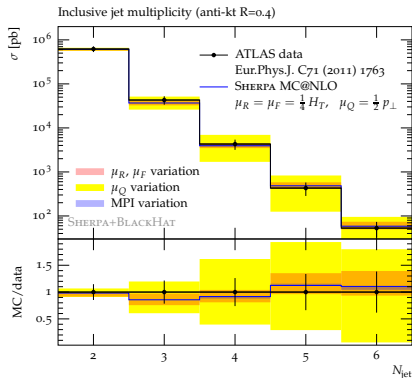
MC@NLO di-jet production:

Höche, *MS Phys.Rev.D86(2012)094042*

- $\mu_{R/F} = \frac{1}{4} H_T$ ,  $\mu_Q = \frac{1}{2} p_{\perp}$
- CT10 PDF ( $\alpha_s(m_Z) = 0.118$ )
- hadron level calculation, MPI
- virtual MEs from BLACKHAT  
Giele, Glover, Kosower  
*Nucl.Phys.B403(1993)633-670*  
Bern et.al. *arXiv:1112.3940*
- $p_{\perp}^{j1} > 20$  GeV,  $p_{\perp}^{j2} > 10$  GeV

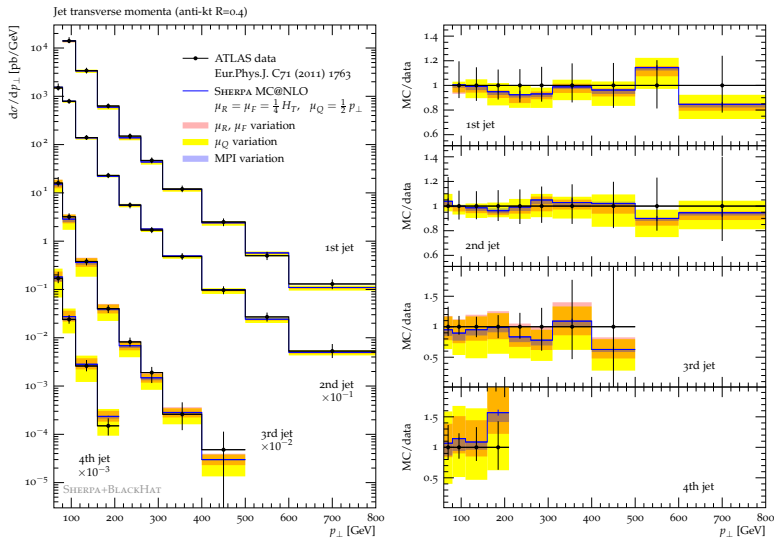
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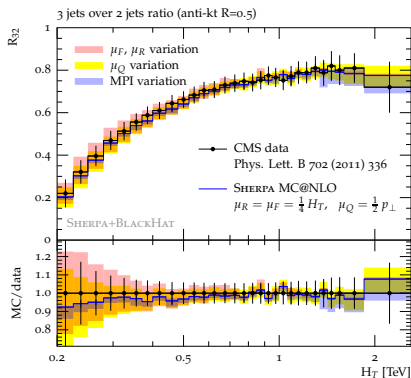


# Case study: Inclusive jet & dijet production





# Case study: Inclusive jet & dijet production

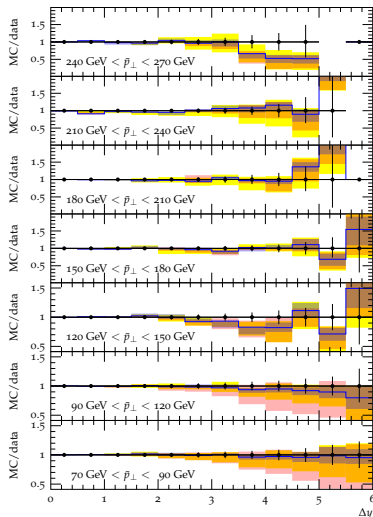
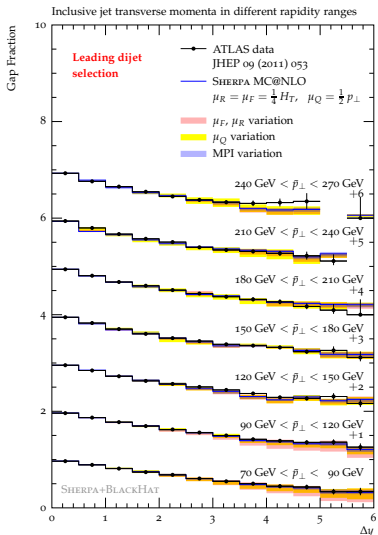


## 3-jet-over-2-jet ratio

- determined from incl. sample  
2-jet rate at NLO+NLL  
3-jet rate at LO+LL
- common scale choices  
→ varied simultaneously
- at large  $H_T$  large MPI  
uncertainties  
→ better MPI physics needed  
(soft QCD)
- similar description of related  
ATLAS observables

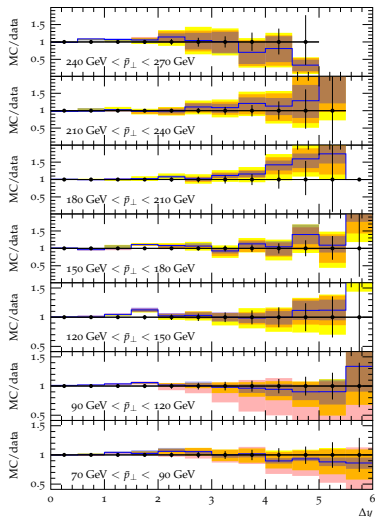
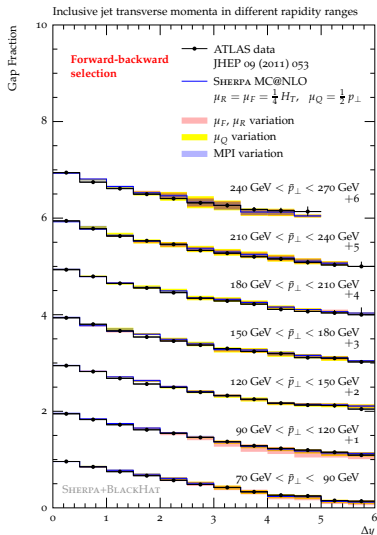


# Case study: Inclusive jet & dijet production





# Case study: Inclusive jet & dijet production



# Recent results

## Fixed-multiplicity NLOs (S-Mc@NLO)

- $pp \rightarrow W + 0, 1, 2, 3 \text{ jets}$  – SHERPA+BLACKHAT

Höche, Krauss, MS, Siebert [Phys.Rev.Lett.110\(2013\)052001](#)

- $pp \rightarrow \text{jets}$  – SHERPA+BLACKHAT

Höche, MS [Phys.Rev.D86\(2012\)094042](#)

- $pp \rightarrow t\bar{t}b\bar{b}$  – SHERPA+OPENLOOPS

Cascioli, Maierhöfer, Moretti, Pozzorini, Siebert [arXiv:1309.0500](#)

- $pp \rightarrow t\bar{t}H$  – SHERPA+TTH

S. Höche, L. Reina contribution to YR3 [arXiv:1307.1347](#)

# Contents

## ① General NLOPS matching

Resummation properties of parton showers

NLOPS matching

Case study

## ② Multijet merging

MEPS – Multijet merging at leading order

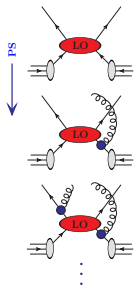
MEPS@NLO – Multijet merging at next-to-leading order

Results

## ③ Conclusions



# MEPs



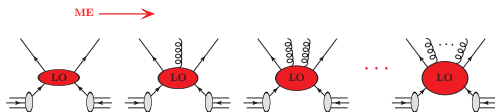
## Parton showers

resummation of (soft-)collinear limit  
 → intrajet evolution

- matrix elements (ME) and parton showers (PS) are approximations in different regions of phase space
- MEPS combines multiple LOPs – keeping either accuracy
- NLOPS elevate LOPs to NLO accuracy
- MENLOPS supplements core NLOPS with higher multiplicities LOPs



# MEPS



## Matrix elements

fixed-order in  $\alpha_s$

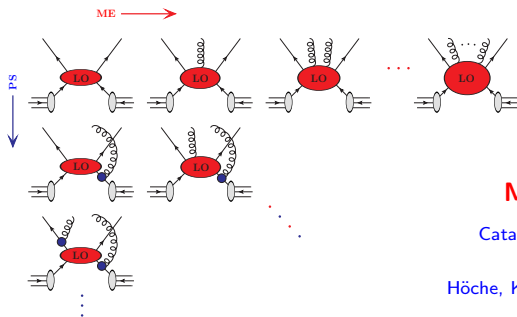
$\rightarrow$  hard wide-angle emissions

$\rightarrow$  interference terms

- matrix elements (ME) and parton showers (PS) are approximations in different regions of phase space
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  - NLOs elevate LOPS to NLO accuracy
  - MENLOPS supplements core NLOs with higher multiplicities LOPS



# MEPs



## MEPs (CKKW, MLM)

Catani, Krauss, Kuhn, Webber JHEP11(2001)063

Lönnblad JHEP05(2002)046

Höche, Krauss, Schumann, Siegert JHEP05(2009)053

- matrix elements (ME) and parton showers (PS) are approximations in different regions of phase space
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# MEPs

Parton showers (operate in  $N_c \rightarrow \infty$  limit):

$$PS_n(t_c, t_{\max}) = \Delta_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \mathcal{K}_n(t') \Delta_n(t', t_{\max})$$

Multijet merging at leading order:

$$d\sigma^{\text{MEPs}} = d\sigma_n^{\text{LO}} \otimes PS_n$$

- restrict the parton shower on  $2 \rightarrow n$  to emit only below  $Q_{\text{cut}}$
- arbitrary jet measure  $Q_n = Q_n(\Phi_n)$
- add the  $n + 1$  ME and its parton shower
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
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- if  $t_n(\Phi_n) \neq Q_n(\Phi_n)$  truncated shower needed to fill gaps



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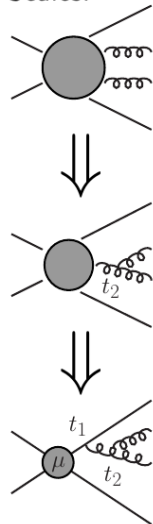
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• if  $t_n(\Phi_n) \neq Q_n(\Phi_n)$  truncated shower needed to fill gaps

Scales:



$$\alpha_s^{k+n}(\mu_R) = \alpha_s^k(\mu_{\text{core}}) \alpha_s(t_1) \cdots \alpha_s(t_n)$$



# MEPs

Parton showers (operate in  $N_c \rightarrow \infty$  limit):

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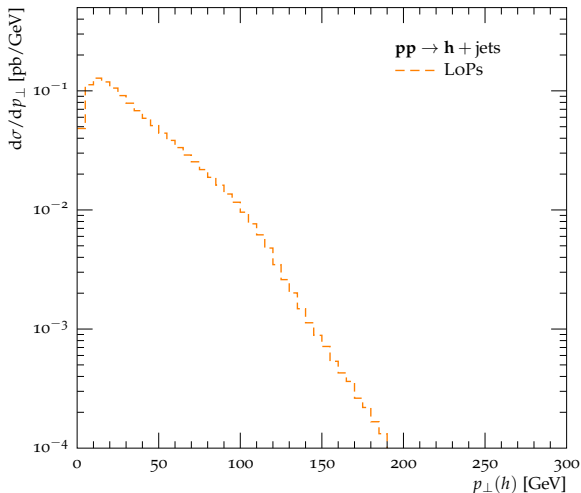
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# MEPs

Transverse momentum of the Higgs boson

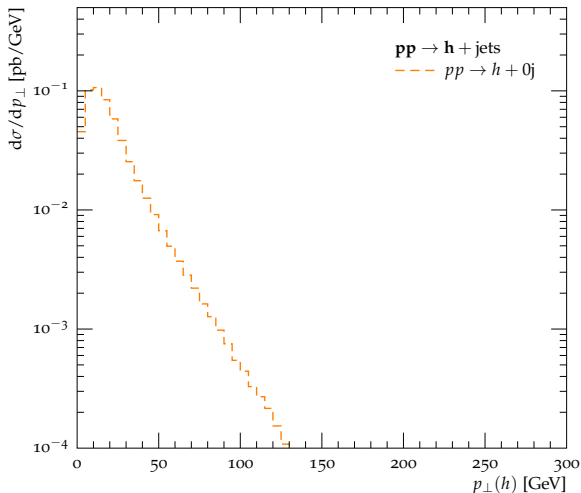


- first emission by PS
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- iterate
- sum all contributions



# MEPs

Transverse momentum of the Higgs boson

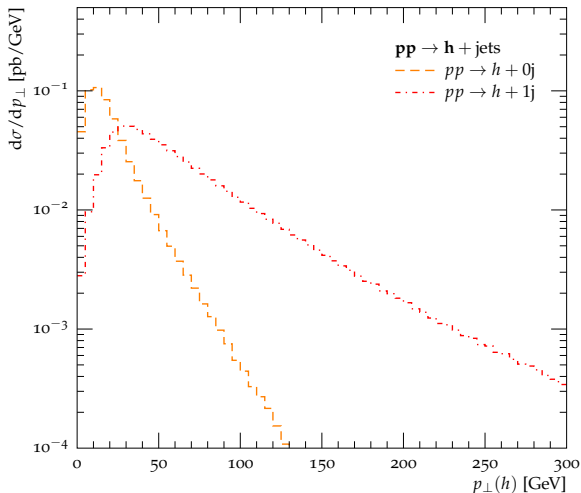


- first emission by PS, restrict to  $Q_{n+1} < Q_{\text{cut}}$
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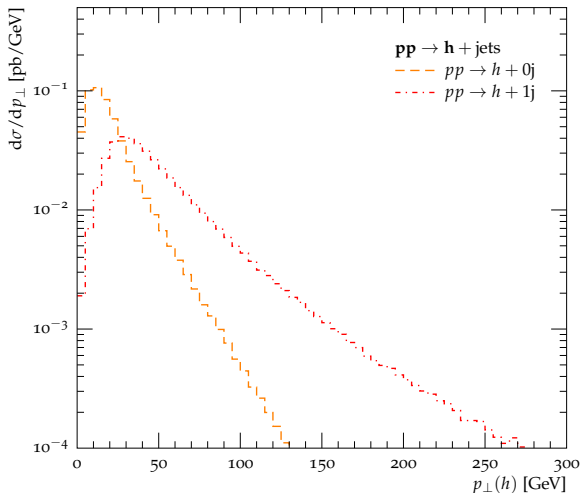


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# MEPS

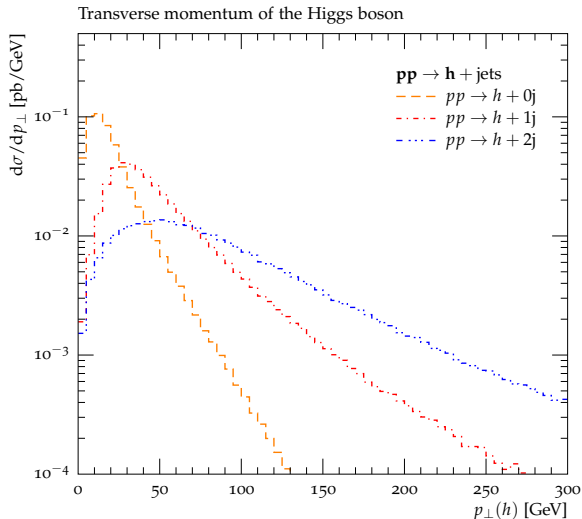
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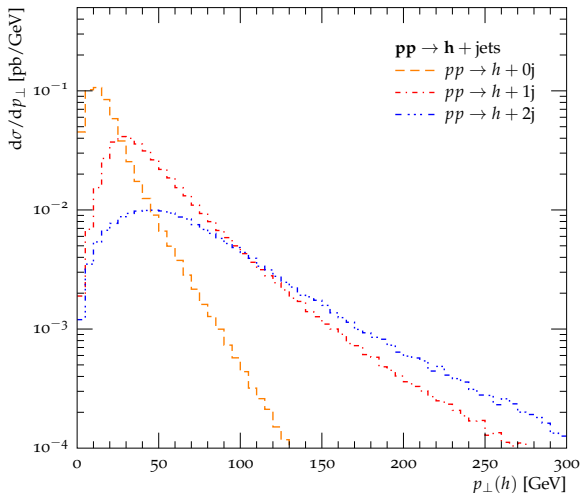


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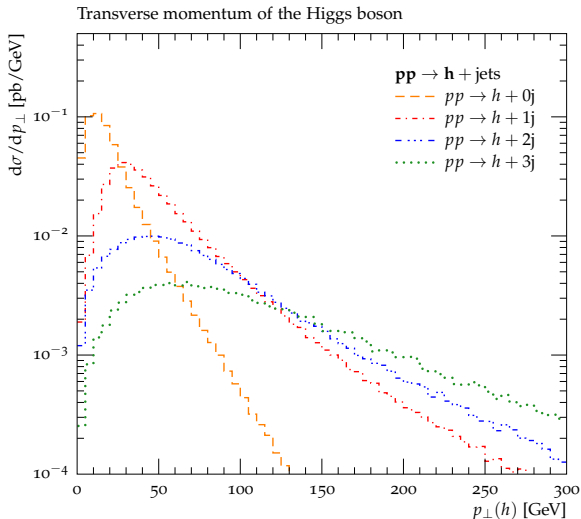
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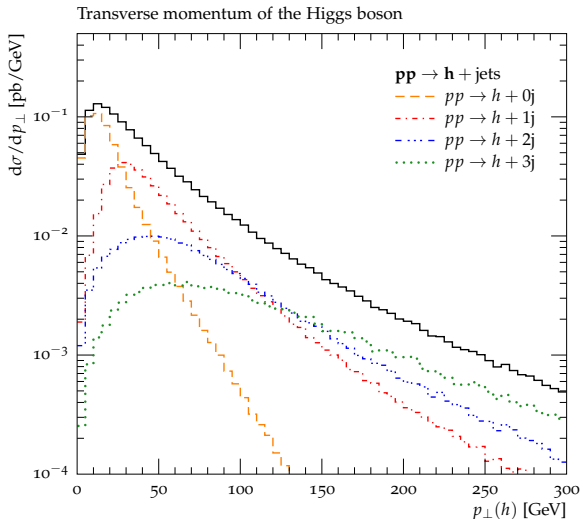
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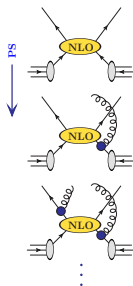
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# MEPs@NLO



## NLOs (MC@NLO, POWHEG)

Frixione, Webber JHEP06(2002)029

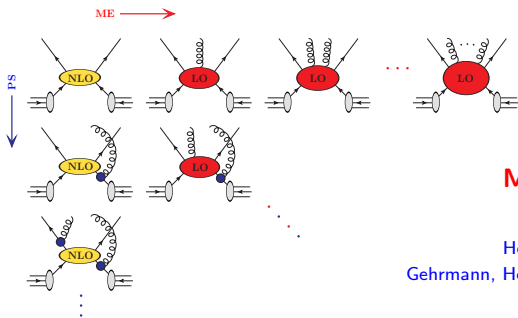
Nason JHEP11(2004)040, Frixione et.al. JHEP11(2007)070

Höche, Krauss, MS, Siebert JHEP09(2012)049

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# MEPs@NLO



## MENLOPS

Hamilton, Nason JHEP06(2010)039

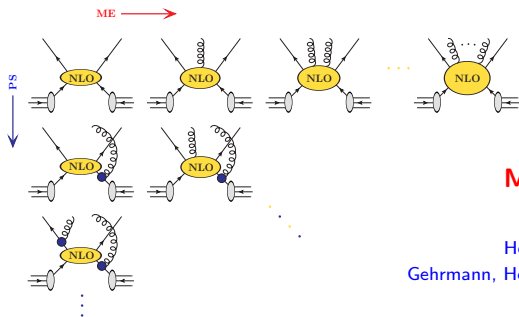
Höche, Krauss, MS, Siegert JHEP08(2011)123

Gehrmann, Höche, Krauss, MS, Siegert JHEP01(2013)144

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# MEPs@NLO



## MEPs@NLO

Lavesson, Lönnblad JHEP12(2008)070

Höche, Krauss, MS, Siegert JHEP04(2013)027

Gehrmann, Höche, Krauss, MS, Siegert JHEP01(2013)144

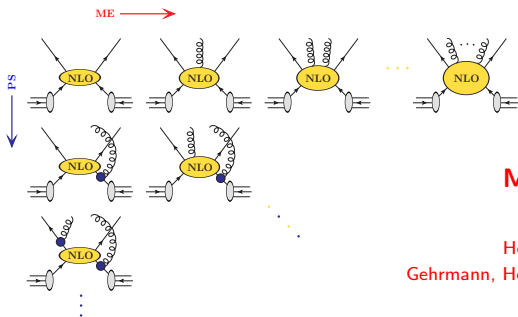
Lönnblad, Prestel JHEP03(2013)166

Plätzer JHEP08(2013)114

- matrix elements (ME) and parton showers (PS) are approximations in different regions of phase space
- MEPs combines multiple LOPS – keeping either accuracy
- NLOPS elevate LOPS to NLO accuracy
- MENLOPS supplements core NLOPS with higher multiplicities LOPS
- MEPs@NLO combines multiple NLOPS – keeping either accuracy



# MEPs@NLO



## MEPs@NLO

Lavesson, Lönnblad JHEP12(2008)070

Höche, Krauss, MS, Siebert JHEP04(2013)027

Gehrmann, Höche, Krauss, MS, Siebert JHEP01(2013)144

Lönnblad, Prestel JHEP03(2013)166

Plätzer JHEP08(2013)114

- matrix elements (ME) and parton showers (PS) are approximations in different regions of phase space
- MEPs combines multiple LOPS – keeping either accuracy
- NLOPS elevate LOPS to NLO accuracy
- MENLOPS supplements core NLOPS with higher multiplicities LOPS
- **MEPs@NLO combines multiple NLOPS – keeping either accuracy**



# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$d\sigma^{\text{MEPs@NLO}} = d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n(t_c, t_{\max}) + d\sigma_{n+1}^{\text{NLO}} \otimes \widetilde{\Delta}_n(t_c, t_{\max})$$

- NLOs for  $2 \rightarrow n$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
- remove overlap of  $\Delta_n$  and  $d\sigma_{n+1}^{\text{NLO}}$



# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} &= d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ &\quad + d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ &\quad + d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \quad \quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_{n+1}) \right) \otimes \widetilde{\text{PS}}_{n+2} \end{aligned}$$

- NLOs for  $2 \rightarrow n$  restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
- remove overlap of  $\Delta_n$  and  $d\sigma_{n+1}^{\text{NLO}}$



# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} &= d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ &\quad + d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ &\quad + d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \quad \quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_{n+1}) \right) \otimes \widetilde{\text{PS}}_{n+2} \end{aligned}$$

- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n+1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
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# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} = & d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ & + d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ & \quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ & + d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ & \quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_{n+1}) \right) \otimes \widetilde{\text{PS}}_{n+2} \end{aligned}$$

- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$ 
  - multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
  - remove overlap of  $\Delta_n$  and  $d\sigma_{n+1}^{\text{NLO}}$



# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} = & d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ & + d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ & \quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ & + d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ & \quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_{n+1}) \right) \otimes \widetilde{\text{PS}}_{n+2} \end{aligned}$$

- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
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# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} &= d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ &+ d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ &+ d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_{n+1}) \right) \otimes \widetilde{\text{PS}}_{n+2} \end{aligned}$$

- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
- remove overlap of  $\Delta_n$  and  $d\sigma_{n+1}^{\text{NLO}}$ . iterate



# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} &= d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ &+ d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ &+ d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_{n+1}) \right) \otimes \widetilde{\text{PS}}_{n+2} \end{aligned}$$

- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
- remove overlap of  $\Delta_n$  and  $d\sigma_{n+1}^{\text{NLO}}$ , iterate



# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular limits for 1st em.):

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t', t_{\max})$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} &= d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ &+ d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ &+ d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)}(t_{n+1}, t_n) \right) \\ &\quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_{n+1}) \right) \otimes \widetilde{\text{PS}}_{n+2} \end{aligned}$$

- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
- remove overlap of  $\Delta_n$  and  $d\sigma_{n+1}^{\text{NLO}}$ , iterate



# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular li

$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t')$$

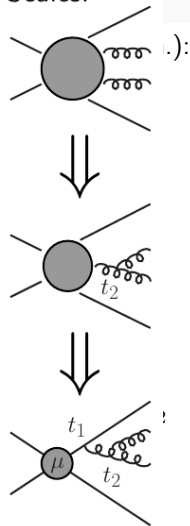
Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} = & d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ & + d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)} \right) \\ & \quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ & + d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)} \right) \\ & \quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_n) \right) \end{aligned}$$

- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation

• remove overlap of  $\Delta_n$  and  $d\sigma_{n+1}^{\text{NLO}}$ , iteratively  $\alpha_s^{k+n}(\mu_R) = \alpha_s^k(\mu_{\text{core}}) \alpha_s(t_1) \cdots \alpha_s(t_n)$

Scales:





# MEPs@NLO

Parton showers for NLOs (need to reproduce  $N_c = 3$  singular li

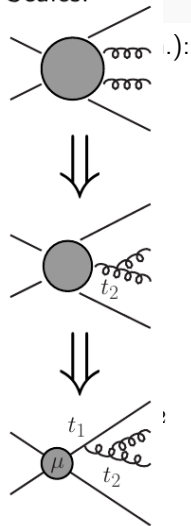
$$\widetilde{\text{PS}}_n(t_c, t_{\max}) = \widetilde{\Delta}_n(t_c, t_{\max}) + \int_{t_c}^{t_{\max}} dt' \widetilde{\mathcal{K}}_n(t') \widetilde{\Delta}_n(t')$$

Multijet merging at next-to-leading order:

$$\begin{aligned} d\sigma^{\text{MEPs@NLO}} = & d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\ & + d\sigma_{n+1}^{\text{NLO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)} \right) \\ & \quad \otimes \widetilde{\text{PS}}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\ & + d\sigma_{n+2}^{\text{NLO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \left( \Delta_n(t_{n+1}, t_n) - \Delta_n^{(1)} \right) \\ & \quad \times \left( \Delta_{n+1}(t_{n+2}, t_{n+1}) - \Delta_{n+1}^{(1)}(t_{n+2}, t_n) \right) \end{aligned}$$

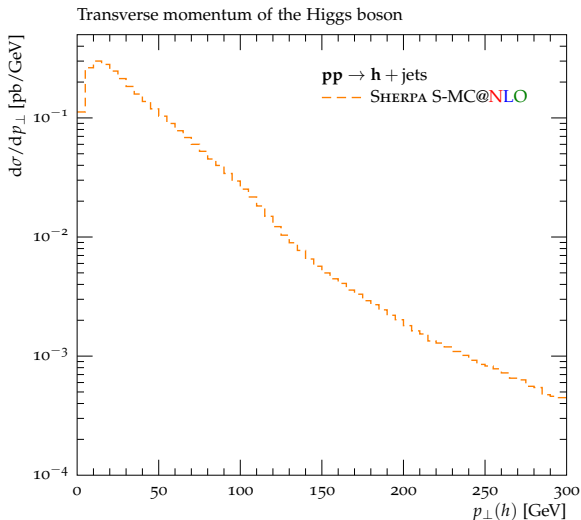
- NLOs for  $2 \rightarrow n$ , restricted to emit only below  $Q_{\text{cut}}$
- add the NLOs for  $2 \rightarrow n + 1$
- multiply by Sudakov wrt.  $2 \rightarrow n$  process to restore resummation
- if  $t_n(\Phi_n) \neq Q_n(\Phi_n)$  truncated shower needed to fill gaps

Scales:





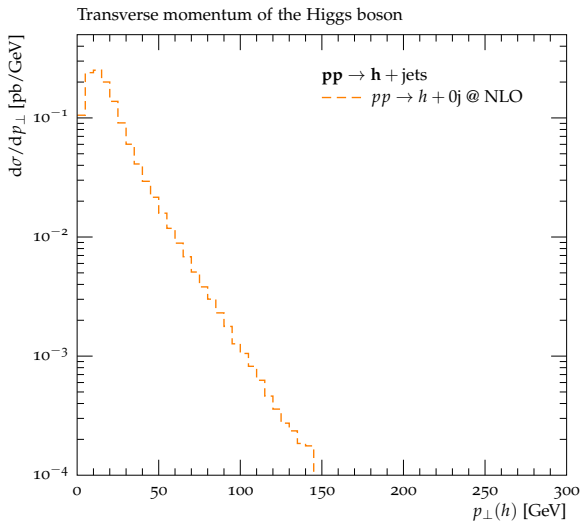
# MEPs@NLO



- first emission by NLOPS, restrict to  $Q_{n+1} < Q_{\text{cut}}$
- NLOPS  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $pp \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
- NLOPS  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate
- sum all contributions



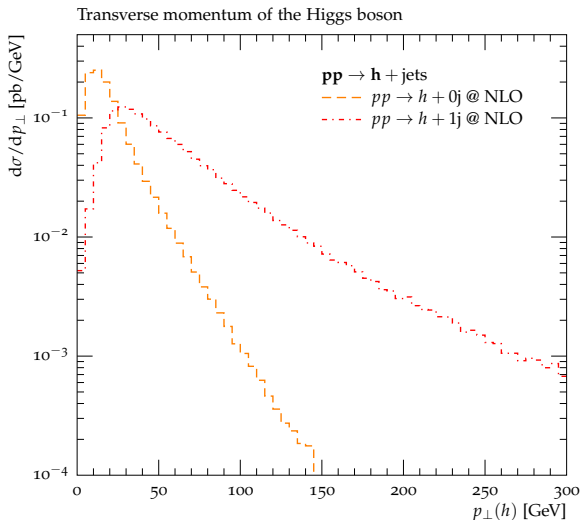
# MEPS@NLO



- first emission by NLOPS, restrict to  $Q_{n+1} < Q_{\text{cut}}$
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- NLOPS  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate
- sum all contributions



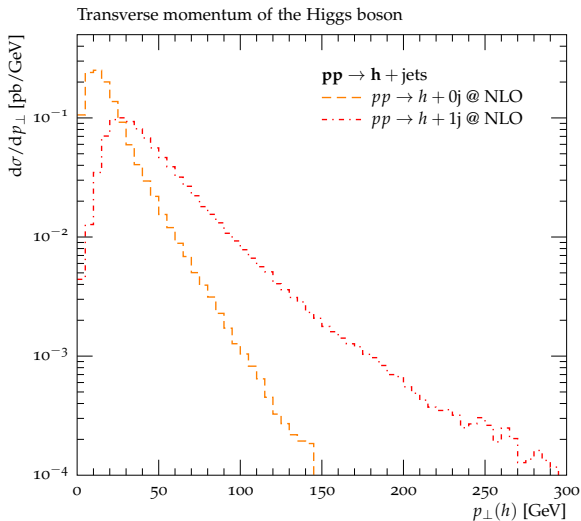
# MEPs@NLO



- first emission by NLOs , restrict to  $Q_{n+1} < Q_{\text{cut}}$
- NLOs  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$ 
  - restrict emission off  $pp \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
  - NLOs  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
  - iterate
  - sum all contributions



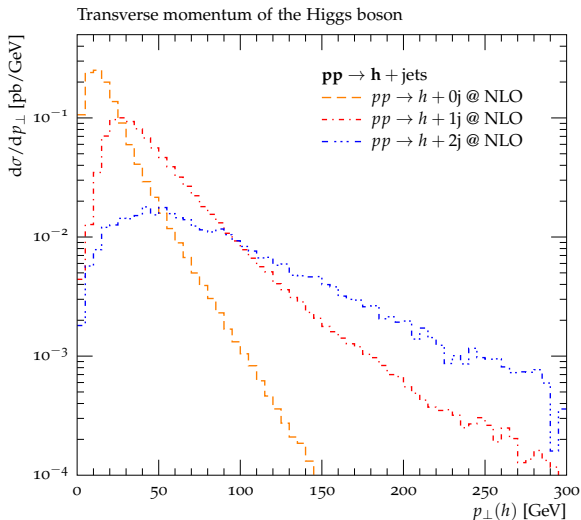
# MEPS@NLO



- first emission by NLOPS, restrict to  $Q_{n+1} < Q_{\text{cut}}$
- NLOPS  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
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- iterate
- sum all contributions



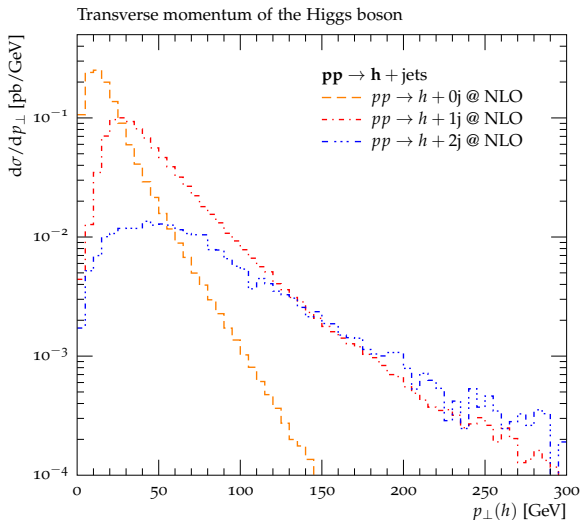
# MEPS@NLO



- first emission by NLOPS, restrict to  $Q_{n+1} < Q_{\text{cut}}$
- NLOPS  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $pp \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
- NLOPS  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate
- sum all contributions



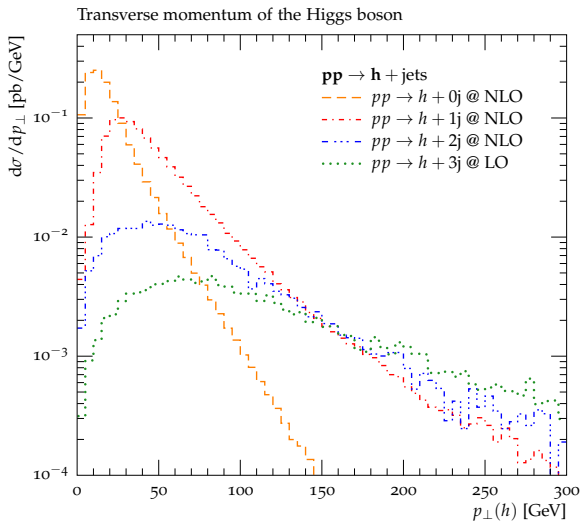
# MEPs@NLO



- first emission by NLOs , restrict to  $Q_{n+1} < Q_{\text{cut}}$
- NLOs  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $pp \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
- NLOs  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate
- sum all contributions



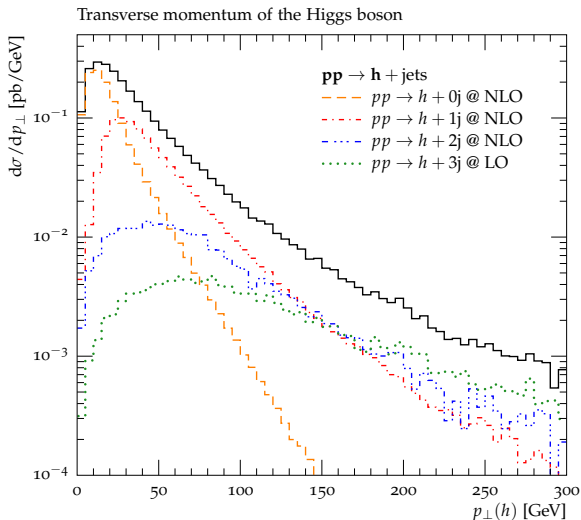
# MEPs@NLO



- first emission by NLOs , restrict to  $Q_{n+1} < Q_{\text{cut}}$
- NLOs  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $pp \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
- NLOs  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate
- sum all contributions



# MEPS@NLO



- first emission by NLOPS, restrict to  $Q_{n+1} < Q_{\text{cut}}$
- NLOPS  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $pp \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
- NLOPS  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate
- sum all contributions



## Recent results

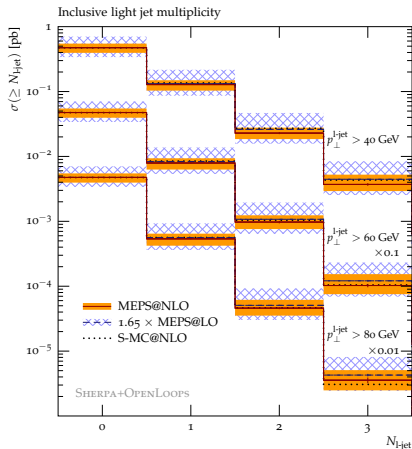
### Multijet merging at NLO accuracy (MEPS@NLO)

- $pp \rightarrow W + \text{jets}$  – SHERPA+BLACKHAT Höche, Krauss, MS, Siegert JHEP04(2013)027
- $e^+e^- \rightarrow \text{jets}$  – SHERPA+BLACKHAT  
Gehrmann, Höche, Krauss, MS, Siegert JHEP01(2013)144
- $pp \rightarrow h + \text{jets}$  – SHERPA+GOSAM/MCFM  
Höche, Krauss, MS, Siegert, contribution to YR3 arXiv:1307.1347  
Höche, Krauss, MS arXiv:1401.7971  
MS, Zapp, contribution to LH13
- $p\bar{p} \rightarrow t\bar{t} + \text{jets}$  – SHERPA+GOSAM/OPENLOOPS  
Höche, Huang, Luisoni, MS, Winter Phys.Rev.D88(2013)014040  
Höche, Krauss, Maierhöfer, Pozzorini, MS, Siegert arXiv:1402.6293
- $pp \rightarrow 4\ell + \text{jets}$  – SHERPA+OPENLOOPS  
Cascioli, Höche, Krauss, Maierhöfer, Pozzorini, Siegert JHEP01(2014)046
- $pp \rightarrow VH + \text{jets}$ ,  $pp \rightarrow VV + \text{jets}$ ,  $pp \rightarrow VVV + \text{jets}$   
– SHERPA+OPENLOOPS  
Höche, Krauss, Pozzorini, MS, Thompson, Zapp arXiv:1403.7516



# Results – $pp \rightarrow t\bar{t} + \text{jets}$

Höche, Krauss, Maierhöfer, Pozzorini, MS, Siegert in arXiv:1401.7971



$pp \rightarrow t\bar{t} + \text{jets}$  (0,1,2 @ NLO; 3 @ LO)

- scales:

$$\alpha_s^{2+n}(\mu_R) = \alpha_s^2(\mu_{\text{core}}) \prod_{i=1}^n \alpha_s(t_i),$$

$$\mu_F = \mu_Q = \mu_{\text{core}} \text{ on } 2 \rightarrow 2$$

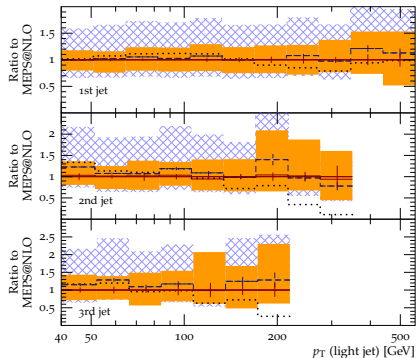
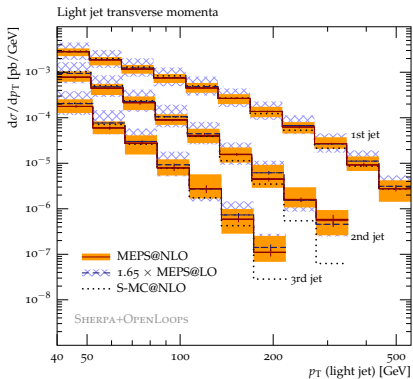
$$Q_{\text{cut}} = 30 \text{ GeV}$$

$$\mu_{\text{core}} = - \frac{2}{\frac{1}{p_0 p_1} + \frac{1}{p_0 p_2} + \frac{1}{p_0 p_3}}$$

- $\mu_{R/F} \in [\frac{1}{2}, 2] \mu_{R/F}^{\text{def}}$
- $\mu_Q \in [\frac{1}{\sqrt{2}}, \sqrt{2}] \mu_Q^{\text{def}}$
- $Q_{\text{cut}} \in \{20, 30, 40\} \text{ GeV}$



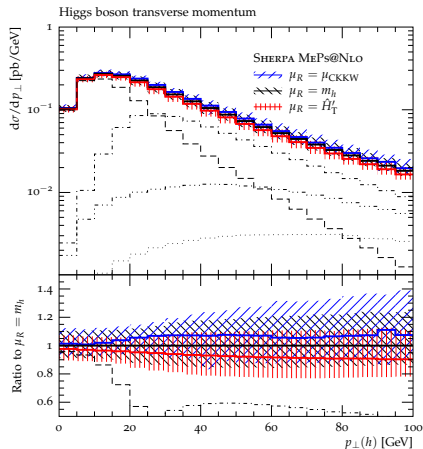
# Results – $pp \rightarrow t\bar{t} + \text{jets}$



- Shapes are stable
- Uncertainties are much smaller where higher accuracy is employed



# Results – $pp \rightarrow h + \text{jets}$



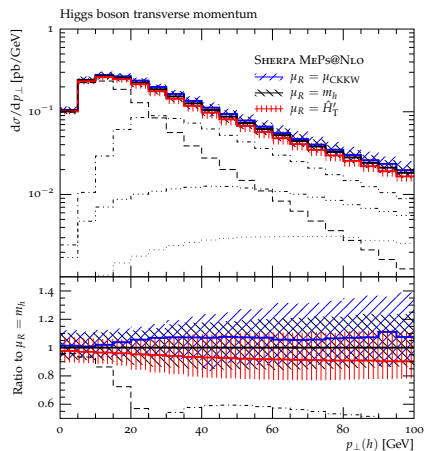
Höche, Krauss, MS, in arXiv:1401.7971

$pp \rightarrow h + \text{jets}$  (0,1,2 @ NLO; 3 @ LO)

- $\mu_{R/F} \in [\frac{1}{2}, 2] \mu_{R/F}^{\text{def}}$
- $\mu_Q \in [\frac{1}{\sqrt{2}}, \sqrt{2}] \mu_Q^{\text{def}}$
- $Q_{\text{cut}} \in \{15, 20, 30\}$  GeV
- virtual MEs from MCFM ( $hjj$ )



# Results – pp → h+jets



⇒ difference beyond accuracy

scale choices:  $\mu_F = \mu_Q = m_h$

- $\mu_R = \mu_{\text{CKKW}}$

$$\alpha_s^{2+n}(\mu_{\text{CKKW}}) = \alpha_s^2(m_h) \alpha_s(t_1) \cdots \alpha_s(t_n)$$

- $\mu_R = m_h$

- $\mu_R = \hat{H}'_T$

need to include ren. term

$$B_n \frac{\alpha_s(\mu_R)}{\pi} \beta_0 \left( \log \frac{\mu_R}{\mu_{\text{CKKW}}} \right)^{2+n}$$

to restore 1-loop running to  $\mu_{\text{CKKW}}$   
 → otherwise PS-accuracy violated

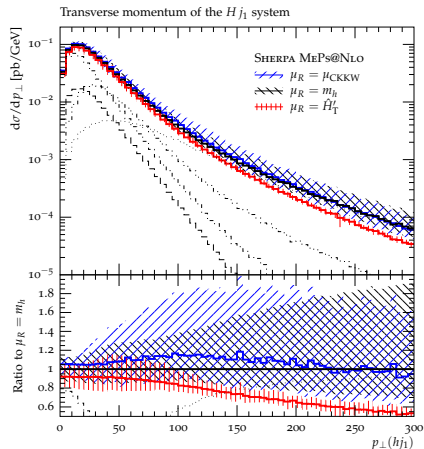
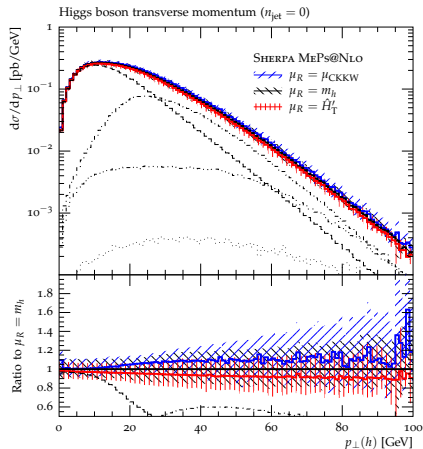
→ same as in UNLOPs approach

Lönnblad, Prestel JHEP03(2013)166

Plätzer JHEP08(2013)114



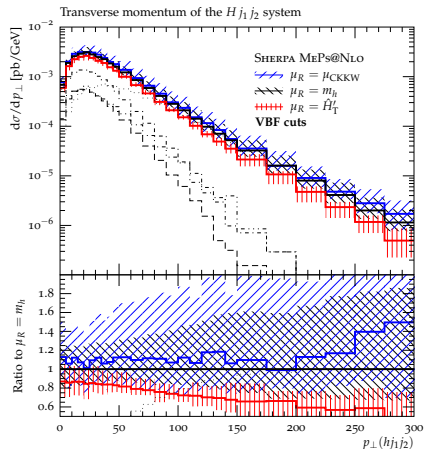
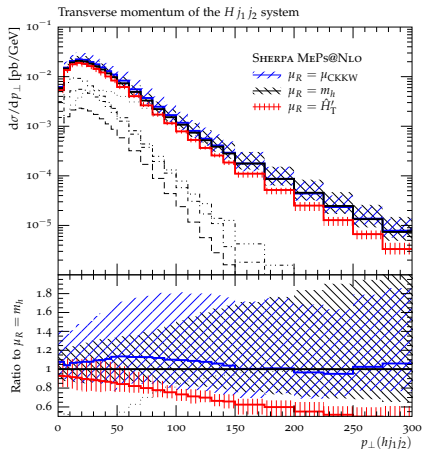
# Results – $pp \rightarrow h + \text{jets}$



- all predictions identical to MEPS@NLO accuracy
- vastly differing size of uncertainties



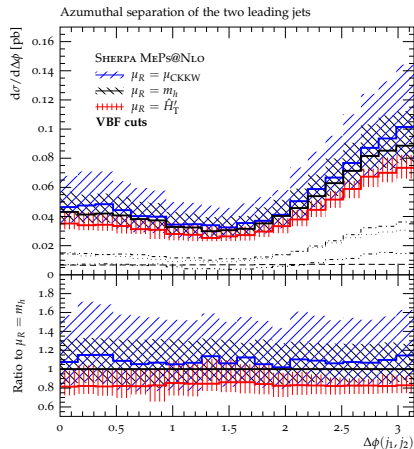
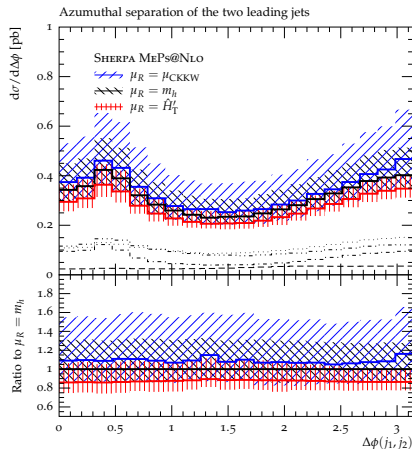
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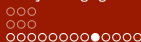
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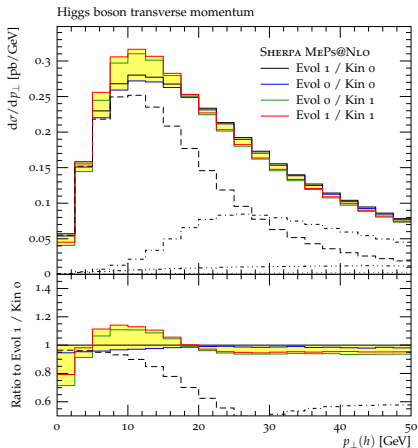
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- vastly differing size of uncertainties



# Results – pp → h+jets



## Parton shower uncertainties

- evolution scale

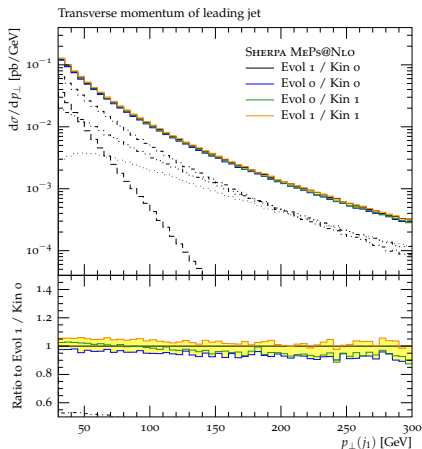
		Final State
0		$2 p_i p_j \tilde{z}_{i,jk} (1 - \tilde{z}_{i,jk})$
1	$2 p_i p_j$	$\tilde{z}_{i,jk} (1 - \tilde{z}_{i,jk})$ if $i, j = g$
		$1 - \tilde{z}_{i,jk}$ if $j = g$
		$\tilde{z}_{i,jk}$ if $i = g$
		1 else
		Initial State
0		$2 p_a p_j (1 - x_{a,j,k})$
1	$2 p_a p_j$	$1 - x_{a,j,k}$ if $j = g$
		1 else

- recoil scheme

0	initial state as if final state + $\perp$ -boost <a href="#">Höhe, Schumann, Siebert Phys.Rev.D81(2010)034026</a>
1	original CS <a href="#">Catani, Seymour Nucl.Phys.B485(1997)291-419</a> <a href="#">Schumann, Krauss JHEP03(2008)038</a>
	→ similar ideas in <a href="#">Gieseke, Plätzer JHEP01(2011)024</a>



# Results – pp → h+jets



## Parton shower uncertainties

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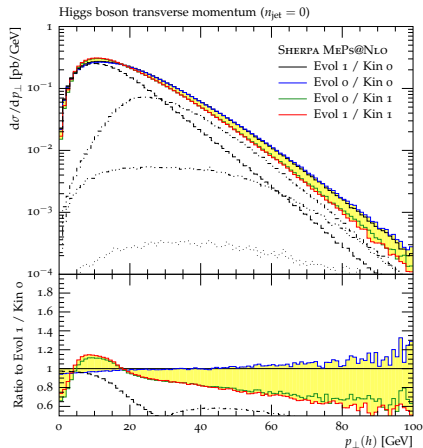
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0		$2 p_i p_j \tilde{z}_{i,jk} (1 - \tilde{z}_{i,jk})$
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# Results – pp → h+jets



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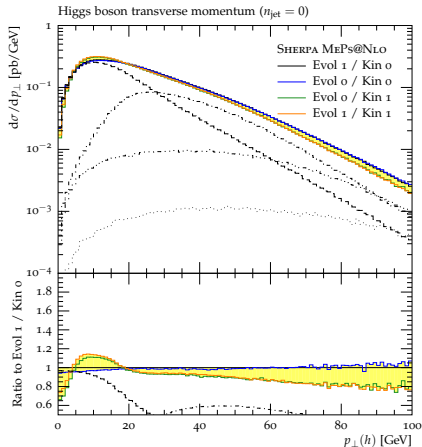
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# Results – pp → h+jets



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→ similar ideas in [Gieseke, Plätzer JHEP01\(2011\)024](#)



## Results – Trilepton production

Höche, Krauss, Pozzorini, MS, Thompson, Zapp arXiv:1403.4788

- trilepton ( $e, \mu$ ) production analysis in  $VH$  search regions  
→ focus on theoretical uncertainties
- model all signal and background processes with consistent setup at largest available accuracy at particle level  
→ need to describe lepton isolation and jet veto efficiency simultaneously
- produce bosons on shell, model off-shell effects through Breit-Wigner smearing  
→ QCD/QED corrections to intermediate states and decay products
- most important event selection criteria

	CMS-inspired analysis	ATLAS-inspired analysis
$Z$ veto	$ m_Z - m_{\text{SFOS}}  > 25 \text{ GeV}$	no SFOS
jet veto	$p_{\perp}^{\text{jet}} < 40 \text{ GeV}$	$p_{\perp}^{\text{jet}} < 20 \text{ GeV}$

- include  $V \rightarrow \tau \rightarrow e, \mu$  decay chains and possibilities to “loose” leptons
- separate  $VVVj(j)$  from  $tVV$  and  $t\bar{t}W$  by disallowing final state  $b$ -quarks



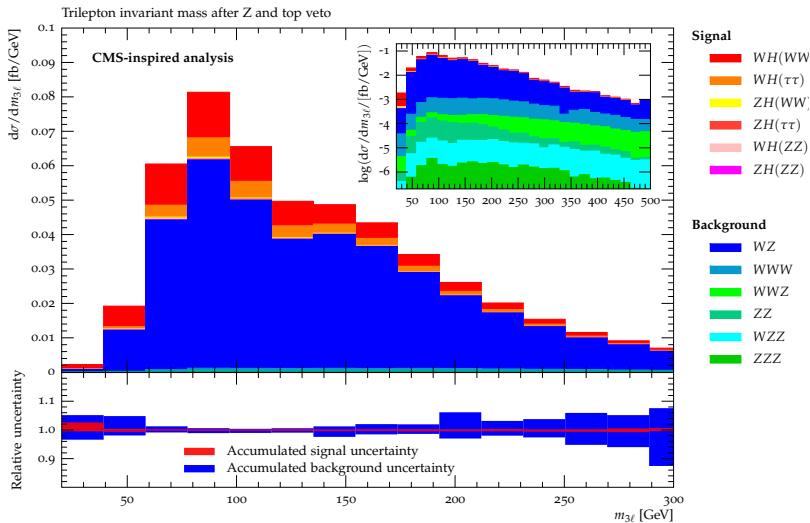
# Results – Tripleton production

Höche, Krauss, Pozzorini, MS, Thompson, Zapp [arXiv:1403.4788](https://arxiv.org/abs/1403.4788)

Process	Accuracy	Decays ( $\ell = e, \mu, \tau$ )
$WH$ +jets	0,1j@NLO, 2j@LO	$H \rightarrow WW, W \rightarrow \ell\nu, Z \rightarrow \ell\ell, \tau \rightarrow \ell\nu\nu$ $H \rightarrow \tau\tau, W \rightarrow \ell\nu, Z \rightarrow \ell\ell, \tau \rightarrow \ell\nu\nu$
$ZH$ +jets	0,1j@NLO, 2j@LO	$H \rightarrow ZZ, W \rightarrow \text{all}, Z \rightarrow \text{all}, \tau \rightarrow \text{all}$ $H \rightarrow WW, W \rightarrow \text{all}, Z \rightarrow \ell\ell, \tau \rightarrow \text{all}$ $H \rightarrow \tau\tau, Z \rightarrow \ell\ell, \tau \rightarrow \text{all}$ $H \rightarrow ZZ, Z \rightarrow \text{all}, \tau \rightarrow \text{all}$
$WZ$ +jets	0,1j@NLO, 2j@LO	$W \rightarrow \ell\nu, Z \rightarrow \ell\ell, \tau \rightarrow \ell\nu\nu$
$WW$ +jets	0,1j@NLO, 2j@LO	$W \rightarrow \ell\nu, \tau \rightarrow \ell\nu\nu$
$WWZ$ +jets	0j@NLO, 1,2j@LO	$W \rightarrow \text{all}, Z \rightarrow \ell\ell, \tau \rightarrow \text{all}$
$ZZ$ +jets	0j@NLO, 1,2j@LO	$Z \rightarrow \ell\ell, \tau \rightarrow \text{all}$
$WZZ$ +jets	0j@NLO, 1,2j@LO	$W \rightarrow \text{all}, Z \rightarrow \text{all}, \tau \rightarrow \text{all}$
$ZZZ$ +jets	0j@NLO, 1,2j@LO	$W \rightarrow \text{all}, Z \rightarrow \text{all}, \tau \rightarrow \text{all}$

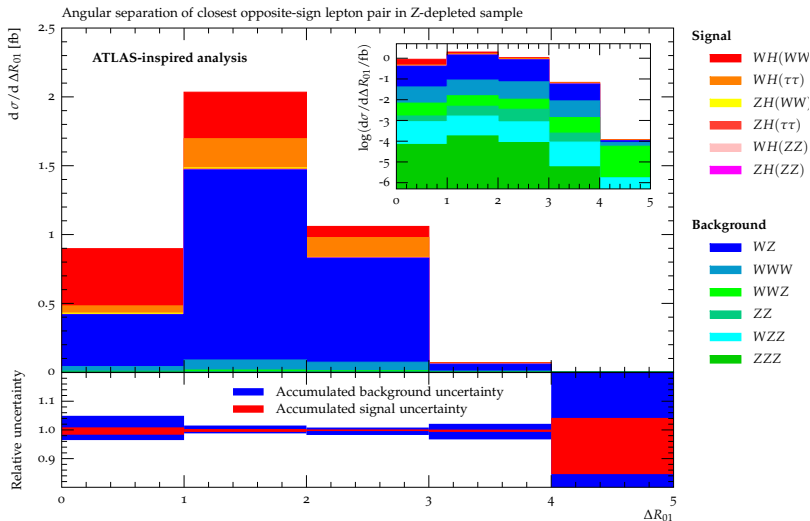


# Results – Trilepton production





# Results – Trilepton production



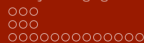


# Conclusions

- NLOs matching is dependent on specifics of resummation  
→ choose resummation kernels and  $\mu_Q^2$
- multijet merging at NLO proceeds schematically as at LO  
→ introduce MC-counterterm to retain NLO accuracy
- preserves NLO accuracy of the ME and accuracy of the PS in resumming hierarchies of emission scales  
→ scale setting essential for recovering PS resummation  
→ beyond 1-loop running the scales can of course be freely chosen
- full uncertainty evaluation (perturbative and non-perturbative) in controlled environment feasible
- includes spin correlated  $1 \rightarrow 2$  and  $1 \rightarrow 3$  decays, with intermediate parton showering and QED corrections

current release SHERPA-2.1.0

<http://sherpa.hepforge.org>



Thank you for your attention!



# MENLOPs

$$\begin{aligned}
 d\sigma^{\text{MENLOPs}} = & d\sigma_n^{\text{NLO}} \otimes \widetilde{\text{PS}}_n \Theta(Q_{\text{cut}} - Q_{n+1}) \\
 & + k_n(\Phi_{n+1}) d\sigma_{n+1}^{\text{LO}} \Theta(Q_{n+1} - Q_{\text{cut}}) \Delta_n(t_{n+1}, t_n) \\
 & \quad \otimes \text{PS}_{n+1} \Theta(Q_{\text{cut}} - Q_{n+2}) \\
 & + k_n(\Phi_{n+1}(\Phi_{n+2})) d\sigma_{n+2}^{\text{LO}} \Theta(Q_{n+2} - Q_{\text{cut}}) \\
 & \quad \times \Delta_n(t_{n+1}, t_n) \Delta_{n+1}(t_{n+2}, t_{n+1}) \otimes \text{PS}_{n+2}
 \end{aligned}$$

- restrict MC@NLO expression to region  $Q < Q_{\text{cut}}$
- add in real radiation explicitly, as in MEPS
- restore logarithmic behaviour by explicit Sudakov
- local K-factor for continuity at  $Q_{\text{cut}}$

$$k_n(\Phi_{n+1}) = \frac{\bar{B}_n(\Phi_n)}{B_n(\Phi_n)} \left( 1 - \frac{H_n(\Phi_{n+1})}{R_n(\Phi_{n+1})} \right) + \frac{H_n(\Phi_{n+1})}{R_n(\Phi_{n+1})}$$

- iterate



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# General NLO calculations

- NLO calculation with subtraction methods

Frixione, Kunszt, Signer Nucl.Phys.B467(1996)399-442

Catani, Seymour Nucl.Phys.B485(1997)291-419

$$\begin{aligned}
 \langle O \rangle^{\text{NLO}} = & \int d\Phi_B \left[ B(\Phi_B) + V(\Phi_B) + I(\Phi_B) \right] O(\Phi_B) \\
 & + \int d\Phi_R \left[ \phantom{B(\Phi_B) + V(\Phi_B) + I(\Phi_B)} - \sum_i D_i^{(S)}(\Phi_R) \phantom{O(\Phi_B)} \right] O(\Phi_{B_i}) \\
 & + \int d\Phi_R \left[ R(\Phi_R) \phantom{- \sum_i D_i^{(S)}(\Phi_R)} \right] O(\Phi_R)
 \end{aligned}$$

- introduce second set of resummation kernels  $D_i^{(A)}$
- $D_i^{(A)}$  and  $D_i^{(S)}$  need to have same momentum maps and IR limit



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 &+ \int d\Phi_R \left[ \sum_i D_i^{(A)}(\Phi_R) O(\Phi_{B_i}) - \sum_i D_i^{(S)}(\Phi_R) O(\Phi_{B_i}) \right] \\
 &+ \int d\Phi_R \left[ R(\Phi_R) - \sum_i D_i^{(A)}(\Phi_R) \right] O(\Phi_R) + \langle O \rangle_{\text{corr}}^{(A)} \\
 \langle O \rangle_{\text{corr}}^{(A)} &= \int d\Phi_R \sum_i D_i^{(A)} [O(\Phi_R) - O(\Phi_{B_i})]
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# General NLO calculations

- NLO calculation with subtraction methods

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## NLOs matching

- parton shower/resummation kernel  $\mathcal{K}_i(\Phi_1)$ ,  $\Phi_1 = \{t, z, \phi\}$

$$\begin{aligned} \langle O \rangle^{\text{PS}} &= \int d\Phi_B B(\Phi_B) O(\Phi_B) \\ &= \int d\Phi_B B(\Phi_B) O(\Phi_B) + \end{aligned}$$

- Sudakov form factor  $\Delta^{(\mathcal{K})}(t, t') = \exp \left[ - \int_t^{t'} d\Phi_1 \mathcal{K}(\Phi_1) \right]$  contains resummation features
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- use  $D_i^{(A)}$  as resummation kernels
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  - starting scale of parton shower evolution
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- **POWHEG and MC@NLO now differ in choice of  $D_i^{(A)}$  and  $\mu_Q^2$**



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- **SHERPA:**  $D_i^{(A)} = D_i^{(S)} \Theta(\mu_Q^2 - t)$  ( $N_c = 3$  **CS kernels**),  $\mu_Q$  free



# POWHEG

## Special choices:

Nason JHEP11(2004)040, Frixione et.al. JHEP11(2007)070

- exponentiation kernel  $D_i^{(A)} = \rho_i \cdot R$  with  $\rho_i = D_i^{(S)} / \sum_i D_i^{(S)}$   
 → each  $\rho_i \cdot R$  contains only one divergence structure as defined by  $D_i^{(S)}$

## Consequences:

- no  $\mathbb{H}$ -events, resummation scale  $\mu_Q^2$  at kinematic limit  $\frac{1}{2} s_{\text{had}}$
- in CS-subtraction instabilities in  $\rho_i$  due to different cuts on  $R$  and  $D_i^{(S)}$
- exponentiation of  $R$  through matrix element corrected parton shower  
 NLO accuracy depends crucially on presence of exact same terms in subtraction and parton shower

## Modifications:

- introduce suppression function  $f(p_\perp) = h^2 / (p_\perp^2 + h^2)$  Alioli et.al. JHEP04(2009)002  
 →  $D_i^{(A)} = \rho_i \cdot R \cdot f(p_\perp)$   
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# Mc@NLO – traditional scheme

## Special choices:

Frixione, Webber JHEP06(2002)029

- exponentiation kernel  $D_i^{(A)} = B \cdot \mathcal{K}_i$  with  $\mathcal{K}_i$  parton shower kernels

## Consequences:

- resummation scale  $\mu_Q^2 = t_{\max}$  parton shower starting scale
- in general,  $D_i^{(A)}$  only leading colour approximation  
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- introduce soft modification function  $f(p_\perp)$  such that

$$\sum B \cdot \mathcal{K}_i \cdot f(p_\perp) \xrightarrow{p_\perp \rightarrow 0} \sum D_i^{(S)}$$

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# S-Mc@NLO

## Special choices:

Höche, Krauss, MS, Siebert JHEP09(2012)049

- exponentiation kernel  $D_i^{(A)} = D_i^{(S)}$

## Consequences:

- simplification of  $\bar{B}^{(A)}$ -integral
- resummation scale  $\mu_Q^2 = t_{\max}$  set by phase space limitation of subtraction terms
  - subtraction constrained in parton shower  $t$  needed for physical resummation
  - instructive example: use  $\alpha_{\text{cut}}$  to explore effects Nagy PRD68(2003)094002
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# S-Mc@NLO

Implemented in SHERPA – full-colour first parton shower emission

**Tricky point:**  $D_i^{(A)} < 0$  e.g. for subleading colour dipoles

**Use modified Sudakov veto algorithm** Höche, Krauss, MS, Siegert JHEP09(2012)049

- Assume  $f(t)$  as function to be generated, and overestimate  $g(t)$   
Standard probability for *one* acceptance with  $n$  rejections

$$\frac{f(t)}{g(t)} g(t) \exp \left\{ - \int_t^{t_1} d\bar{t} g(\bar{t}) \right\} \prod_{i=1}^n \left[ \int_{t_{i-1}}^{t_{n+1}} dt_i \left( 1 - \frac{f(t_i)}{g(t_i)} \right) g(t_i) \exp \left\{ - \int_{t_i}^{t_{i+1}} d\bar{t} g(\bar{t}) \right\} \right]$$

- Can split weight into MC and **analytic** part using auxiliary function  $h(t)$

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$$w(t, t_1, \dots, t_n) = \frac{g(t)}{h(t)} \prod_{i=1}^n \frac{g(t_i)}{h(t_i)} \frac{h(t_i) - f(t_i)}{g(t_i) - f(t_i)}$$



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Identify  $f(t)$ ,  $g(t)$ ,  $h(t)$ :

- $f(t)$  determined by Mc@NLO  $\Rightarrow D_i^{(A)}$
- $h(t)$  determined by parton shower  $\Rightarrow D_i^{(PS)}$
- $g(t)$  **can be chosen freely**  $\Rightarrow \text{const.} \cdot f$   
constraints:  $\text{sign}(f) = \text{sign}(g)$ ,  $|f| \leq |g|$



## NLO merging – Generation of MC counterterm

$$\left[ 1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 \mathcal{K}_n \right]$$

- same form as exponent of Sudakov form factor  $\Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2)$
- truncated parton shower on  $n$ -parton configuration underlying  $n + 1$ -parton event
  - 1 no emission  $\rightarrow$  retain  $n + 1$ -parton event as is
  - 2 first emission at  $t'$  with  $Q > Q_{\text{cut}}$ , multiply event weight with  $B_{n+1}/\bar{B}_{n+1}^{(A)}$ , restart evolution at  $t'$ , do not apply emission kinematics
  - 3 treat every subsequent emission as in standard truncated vetoed shower
- generates

$$\left[ 1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 \mathcal{K}_n \right] \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2)$$

$\Rightarrow$  **identify  $\mathcal{O}(\alpha_s)$  counterterm with the omitted emission**