

Monte Carlo event generation: Introduction

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Dakar, 07/08/2014

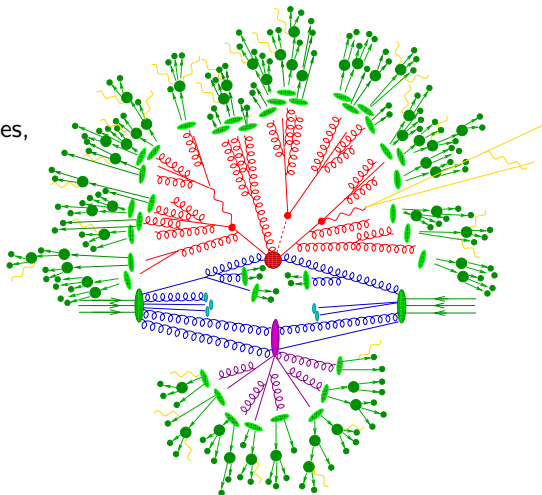


A hadron collider event

Event structure

Factorise into event stages according to characteristic scales, use relevant approximation in each regime

- Hard scattering
- Parton evolution
- Multiple interactions
- Hadronisation
- Hadron decays
- QED corrections



Monte Carlo event generation: Introduction

- 1 Parton evolution
- 2 Multi-parton interactions
- 3 Hadronisation
- 4 Hadron decays & QED corrections
- 5 Analysis and tuning
- 6 Summary

Parton evolution

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Parton evolution

Why is parton evolution important?

- accelerated charges radiate
acceleration = change in momentum, e.g. through interaction
- large momentum transfer \Rightarrow much radiation
- **QED**: electrons (em-charged) emit photons
photons split into electron-positron pairs
- **QCD**: quarks (colour-charged) emit gluons
gluons split into quark-anti-quark pairs
gluons split into gluons

\rightarrow gluons are colour-charged, photons are not em-charged

\Rightarrow cascade of emissions: **Parton shower**

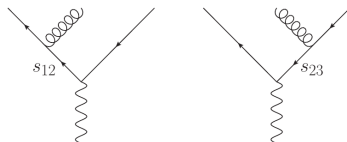
Parton showers – construction

- consider $e^+e^- \rightarrow q\bar{q}g$

$$\frac{q}{\sigma_{2 \rightarrow 2}} \frac{d\sigma_{2 \rightarrow 3}}{d\cos\theta dz} \propto C_F \frac{\alpha_s}{2\pi} \frac{2}{\sin^2\theta} \frac{1 + (1-z)^2}{z}$$

θ - angle of gluon emission

z - fractional energy of gluon



- divergent if emission collinear: $\theta \rightarrow 0, \pi$
soft: $z \rightarrow 0$

- separate collinear limits due to emission off quark and anti-quark

$$\frac{2d\cos\theta}{\sin^2\theta} = \frac{d\cos\theta}{1-\cos\theta} + \frac{d\cos\theta}{1+\cos\theta} = \frac{d\cos\theta}{1-\cos\theta} + \frac{d\cos\bar{\theta}}{1-\cos\bar{\theta}} \approx \frac{d\theta^2}{\theta^2} + \frac{d\bar{\theta}^2}{\bar{\theta}^2}$$

- independent evolution

$$d\sigma_3 \propto \sigma_2 \sum_{i=q,\bar{q}} C_F \frac{\alpha_s}{2\pi} \frac{d\theta^2}{\theta^2} dz \frac{1 + (1-z)^2}{z}$$


Parton shower – construction

- any variable with same limiting behaviour leads to same equation


- transverse momentum $k_{\perp}^2 = z^2(1-z)^2\theta^2 E^2$
- virtuality $q^2 = z(1-z)\theta^2 E^2$

$$\Rightarrow \frac{d\theta^2}{\theta^2} = \frac{dk_{\perp}^2}{k_{\perp}^2} = \frac{dq^2}{q^2} := \frac{dt}{t} \quad \longleftrightarrow \quad \text{collinear divergence}$$


- absorb z -dependence into flavour dependent splitting kernels $P_{ab}(z)$




$$= C_F \frac{1+z^2}{1-z}$$



$$= C_F \frac{1+(1-z)^2}{z}$$



$$= T_R [z^2 + (1-z)^2]$$



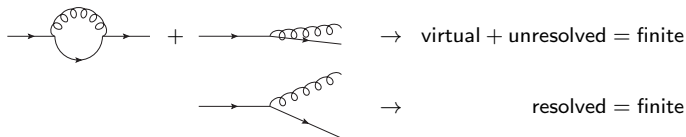
$$= C_A \left[\frac{z}{1-z} + \frac{1-z}{z} + z(1-z) \right]$$

- universal collinear approximation

$$d\sigma_{n+1} \propto \sigma_n \sum_{\text{partons}} \frac{dt}{t} dz \frac{\alpha_s}{2\pi} P_{ab}(z)$$

Parton shower – construction

- collinear partons not separately resolvable
- introduce resolution criterion, e.g. $t > t_c$, also acts as infrared regulator



- Poisson statistics leads to no-emission probability

$$d\mathcal{P}_{\text{em}}(t) = \frac{dt}{t} \int dz \frac{\alpha_s}{2\pi} P_{ab}(z) \quad \rightarrow \quad \mathcal{P}_{\text{no-em}}(t, t') = \exp \left\{ - \int_t^{t'} \frac{d\bar{t}}{\bar{t}} \int dz \frac{\alpha_s}{2\pi} P_{ab}(z) \right\}$$

- **Sudakov form factor** $\Delta(t, t') := \mathcal{P}_{\text{no-em}}(t, t')$
- probability of a parton produced at t' to radiate/resolve another parton at t

$$d\mathcal{P}(t) = d\mathcal{P}_{\text{em}}(t) \mathcal{P}_{\text{no-em}}(t, t') = dt \frac{d\Delta(t, t')}{dt}$$

Parton shower – algorithm

$$\langle O \rangle^{\text{PS}} = \int d\Phi_B B(\Phi_B) \left[\Delta(t_c, t_{\text{max}}) \left[\dots \right] \right]$$

- start with set of n partons at scale t_{max}
- let them evolve collectively with

$$\Delta(t, t') = \prod_{i=1}^n \Delta_i(t, t') \quad \Delta_i(t, t') = \prod_{j=q,g} \Delta_{i \rightarrow j}(t, t')$$

- use veto algorithm to find new scale t where next emission occurs
- construct splitting kinematics
- continue on $n + 1$ parton state until $t < t_c$

Parton shower – algorithm

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 $t < t_c$: unresolved region, no explicit emission
 $t > t_c$: generate resolved emission at t
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 $\rightarrow n + 1$ parton configuration in collinear approximation
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Selecting from a Poisson distribution

- **Example:** Assume nuclear decay process described by $g(x)$
- nucleus can only decay if it has not yet decayed already
must account for survival probability \leftrightarrow **Poisson distribution**

$$\mathcal{G}(x) = g(x) \Delta(x, b) \quad \text{with} \quad \Delta(x, b) = \exp \left\{ - \int_x^b d\bar{x} g(\bar{x}) \right\}$$

- if $G(x)$ known, then integral of $\mathcal{G}(x)$ is

$$\int_x^b d\bar{x} \mathcal{G}(\bar{x}) = \int_x^b d\bar{x} \frac{d\Delta(\bar{x}, b)}{d\bar{x}} = 1 - \Delta(x, b)$$

- generate events by requiring $1 - \Delta(x, b) = 1 - R$

$$x = G^{-1} \left[G(b) + \log R \right]$$

The veto algorithm

- want to sample Poisson distributed process $f(x)$, but F unknown
- **Veto algorithm:** Hit-or-miss method for Poisson distribution
 - choose $g(x) > f(x)$ with known G and G^{-1}
 - generate random number x according to $\mathcal{G}(x)$
 - accept with $w(x) = f(x)/g(x) < 1$
 - if rejected, continue starting from x
- probability for immediate acceptance of x is

$$\frac{f(x)}{g(x)} g(x) \exp \left\{ - \int_x^b d\bar{x} g(\bar{x}) \right\}$$

- probability for acceptance of x after rejection at x' is

$$\frac{f(x)}{g(x)} g(x) \int dx' \exp \left\{ - \int_x^{x'} d\bar{x} g(\bar{x}) \right\} \left(1 - \frac{f(x')}{g(x')} \right) g(x') \exp \left\{ - \int_{x'}^b d\bar{x} g(\bar{x}) \right\}$$

- for n intermediate rejections \rightarrow n nested integrals $\int_x^b \int_{x'}^b \int_{x''}^b \dots$
- disentangling yields $1/n!$ and summing over all possible rejections

$$f(x) \exp \left\{ - \int_x^b d\bar{x} g(\bar{x}) \right\} \sum_{n=0}^{\infty} \frac{1}{n!} \left[\int_x^b d\bar{x} [g(\bar{x}) - f(\bar{x})] \right]^n = f(x) \exp \left\{ - \int_x^b d\bar{x} f(\bar{x}) \right\}$$

Parton showers

	t	z	kernels
ARIADNE	dipole- k_{\perp}^2	rapidity	$2 \rightarrow 3$
fHERWIG	$E^2\theta^2$	energy fraction	$1 \rightarrow 2$
HERWIG++	$E^2\theta^2$	light-cone mom. fraction	$1 \rightarrow 2$
PYTHIA 6.x	q^2	energy fraction	$1 \rightarrow 2$
PYTHIA8	k_{\perp}^2	light-cone mom. fraction	$1 \rightarrow 2$ (IS), $2 \rightarrow 3$ (FS)
SHERPA 1.1.x	q^2	energy fraction	$1 \rightarrow 2$
SHERPA 1.2.x	dipole- k_{\perp}^2	light-cone mom. fraction	$2 \rightarrow 3$
VINCIA	dipole- k_{\perp}^2	light-cone mom. fraction	$2 \rightarrow 3$

Parton showers – improvements

Parton showers construct a collinear approximation for $\mathcal{O}(\alpha_s)$ corrections.

- want to improve description of emissions
 - matrix element corrections
 - multijet merging (CKKW & MLM)

Parton showers construct a collinear approximation for $\mathcal{O}(\alpha_s)$ corrections.

- ① parton shower: take collinear limit to $\mathcal{O}(\alpha_s)$ to construct an all-orders resummation (Sudakov form factor)
 - ② NLO calculation: all $\mathcal{O}(\alpha_s)$ terms, no resummation
- ⇒ no trivial combination as with leading order
→ NLOPS matching (MC@NLO & POWHEG)
identify common terms and remove

→ **beyond the scope of this lecture**

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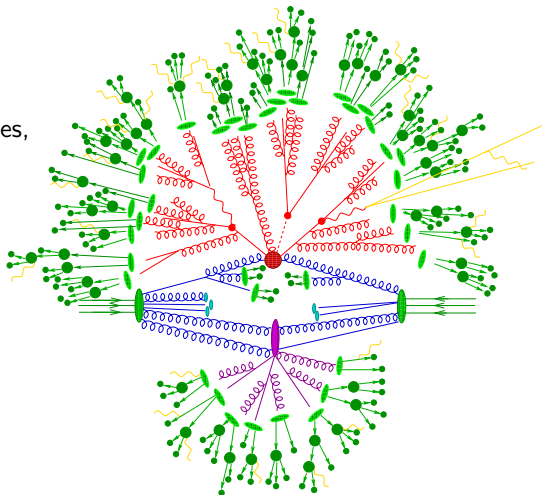
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Event structure

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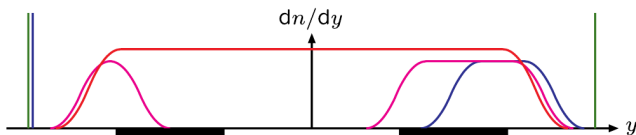
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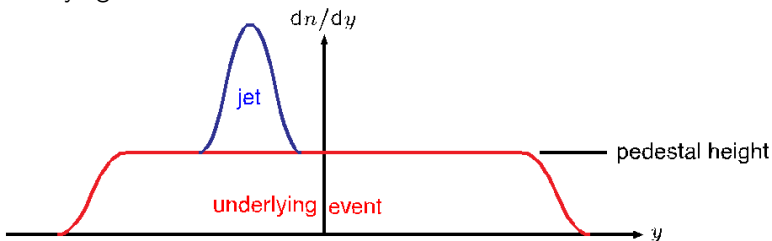
Classification

- Soft inclusive collision

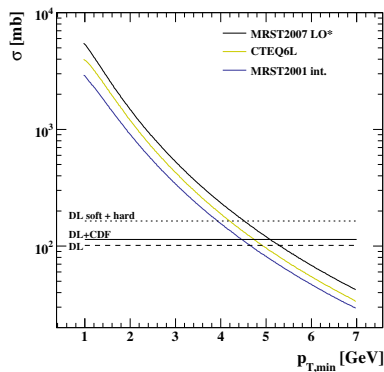
$$\sigma_{\text{tot}} = \sigma_{\text{elastic}} + \sigma_{\text{single diffractive}} + \sigma_{\text{double diffractive}} + \sigma_{\text{non-diffractive}}$$



- underlying event



Modelling the pedestal



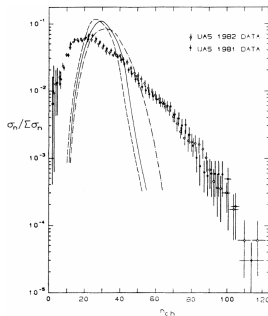
Sjöstrand, van Zijl Phys.Rev.D36(1987)2019

- partonic cross sections diverge like $d p_{\perp}^2 / p_{\perp}^4$
- ⇒ for small $p_{\perp} \approx 2 - 5$ GeV
 $\sigma_{\text{partonic}} > \sigma_{\text{non-diffractive}}$
- interpret as multiple hard scatters with

$$\langle n \rangle = \frac{\sigma_{\text{partonic}}(p_{\perp, \min})}{\sigma_{\text{non-diffractive}}}$$

- main parameter is $p_{\perp, \min}$, determines multiplicity $\langle n \rangle$

Modelling the pedestal



- simple model with

$$\langle n \rangle = \frac{\sigma_{\text{partonic}}}{\sigma_{\text{non-diffractive}}}$$

gives wrong charged multi distribution

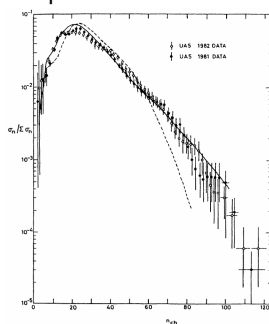
- incorporate hadron shape into prediction



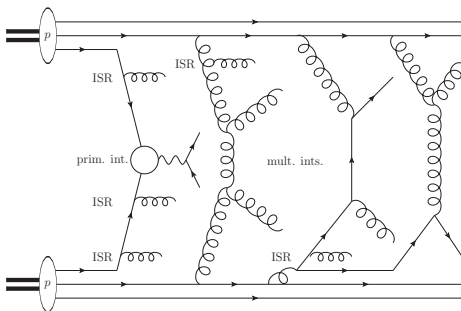
- various shape models to determine hadron-hadron overlap

$$\langle n(b) \rangle = f_c f(b) \frac{\sigma_{\text{partonic}}}{\sigma_{\text{non-diffractive}}}$$

- hardness of the collision determines overlap



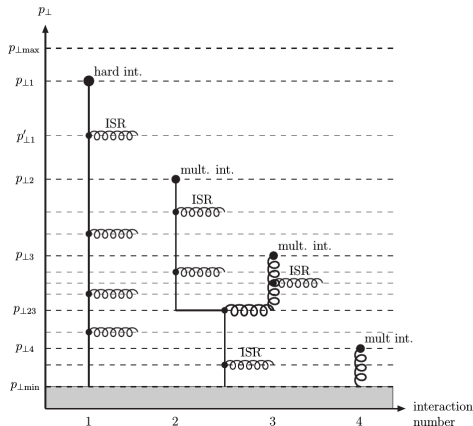
Combination with parton showers



- **naïve:** $\langle n(b) \rangle$ independent secondary interactions
- ⇒ separation of perturbative picture of hard interaction
- no way to include rescattering
- completely separate colour and momentum evolution

Combination with parton showers

Sjöstrand, Skands hep-ph/0408302



- **improvement:** interleaving
 - \mathcal{P}_{MPI} evolution kernel, combine w/ pert. IS evol.

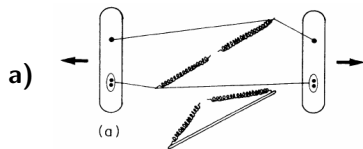
$$\mathcal{P} = \mathcal{P}_{\text{ISR}} + \mathcal{P}_{\text{MPI}}$$

- ⇒ interleaved colour and momentum structure, rescattering effects
- IS evolution not completely perturbative anymore

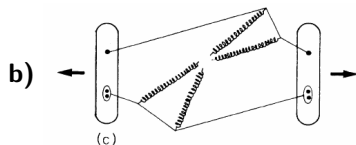
Colour connections and beam remnants

Sjöstrand, Skands hep-ph/0402078

- secondary scatterings need to be colour-connected to something



- simplest model would decouple them from proton remnants

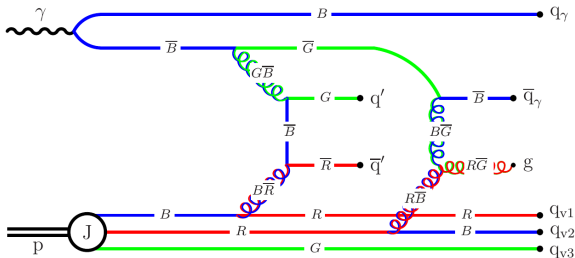


- next-to-simplest model would put all scatters on one colour string

Colour connections and beam remnants

Sjöstrand, Skands hep-ph/0402078

- example for colour connections



- embed additional scatters into existing topologies (respect colour conservation)



- three options:
 - at random
 - rapidity ordered
 - minimal string length

Multiple interactions models

	MPI model	Features
HERWIG++	form factor model	naïve comb. with PS soft diffractive model
PYTHIA8	Lund model	interleaved with PS several diffractive models
SHERPA	Lund model	naïve comb. with PS soft pomeron scattering model

Monte Carlo event generation: Introduction

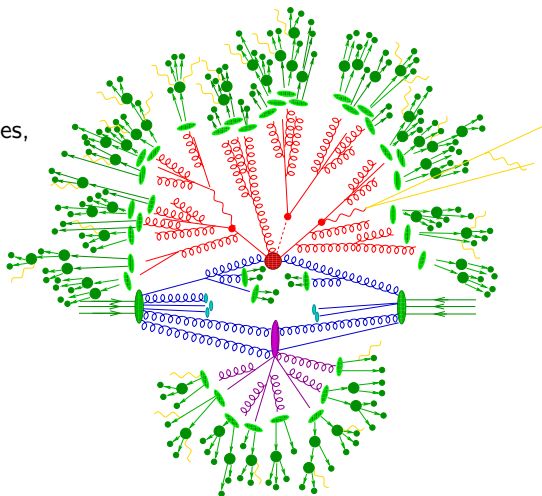
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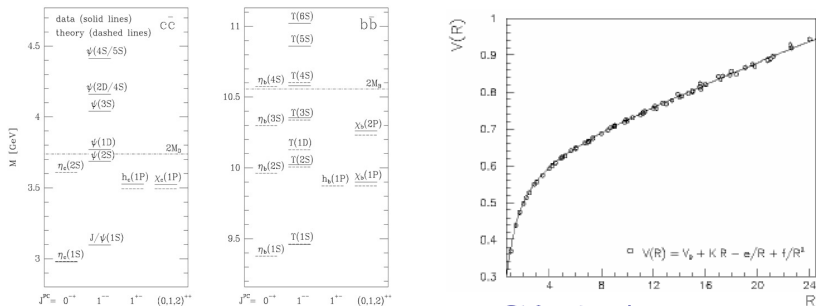
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Confinement and interquark potential

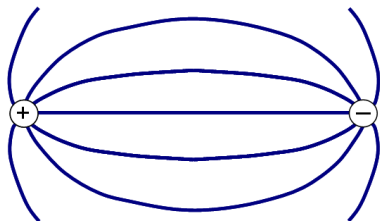
- Hadronisation is QCD at low scales where α_s is $\mathcal{O}(1)$
- ⇒ non-perturbative dynamics, not easily calculable from first principles



- measure QCD potential from quarkonia masses
 - or calculate using lattice QCD
- ⇒ approximately linear potential

Confinement and interquark potential

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QED dipole



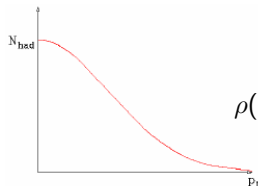
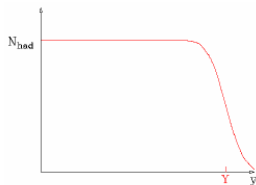
QCD dipole

⇒ formation of flux tubes in QCD

Feynman-Field model

Feynman, Field NPB136(1978)1

Experimental findings:




$$\rho(p_{\perp}^2) = \exp(-p_{\perp}^2/\sigma^2)$$

Realisation:

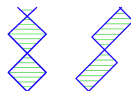
- recursively split $q \rightarrow q' + \text{hadron}$
 - transverse momentum from fitted Gaussian
 - longitudinal momentum arbitrary (fitted to measurements)
 - flavour from symmetry arguments+measurements
- **problems:** frame dependent, “last quark”, infrared safety, no link to perturbation theory


Lund string model

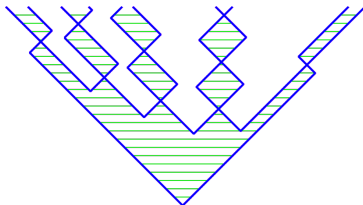
Andersson, Gustafson, Ingelman, Sjöstrand PR97(1983)31

- start with $e^+e^- \rightarrow q\bar{q}$
- QCD flux tube with constant energy per unit rapidity \leftrightarrow 
- new $q\bar{q}$ -pairs by pair creation in the flux tube (κ -string tension)

$$\frac{d\mathcal{P}}{dxdt} = \exp\left\{-\frac{\pi^2 m_q^2}{\kappa}\right\}$$



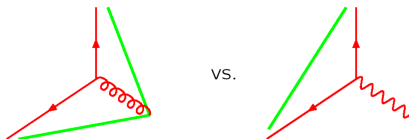
- expanding string breaks into hadrons, then yoyo modes 
- mesons as quark-antiquark pairs, baryons as quark-diquark pairs



Lund string model

Andersson, Gustafson, Ingelman, Sjöstrand PR97(1983)31

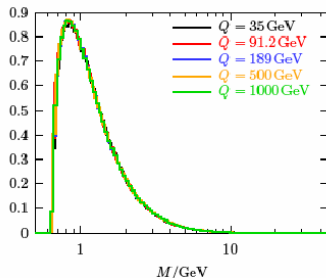
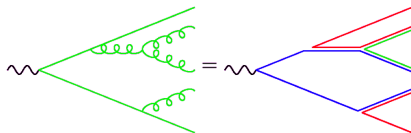
- Lund string model very well motivated, but many parameters
- ⇒ gives genuine prediction of “string effect”
- strings span between quarks and anti-quarks, gluons form kinks in string
 - string accelerated in direction of gluon
 - infrared safe matching to parton showers
 - gluons with $k_{\perp} \lesssim 1/\kappa$ irrelevant



Cluster model

Webber NPB238(1984)492

- underlying idea: preconfinement
- ⇒ follow colour structure of parton showers, colour singlets end up close in phase space
- singlet mass $\mathcal{O}(t_c)$
- ⇒ **primordial clusters** independent of collider energy



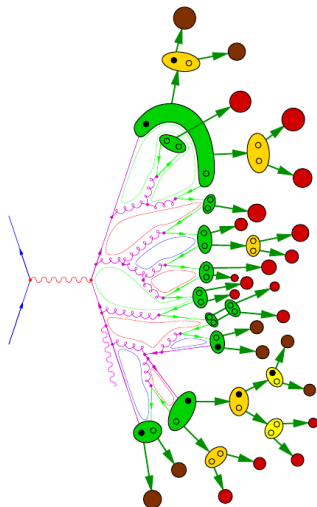
Cluster model

Naïve model:

- split gluons non-perturbatively into $q\bar{q}$ -pairs
- colour-adjacent pairs form primordial clusters
- clusters decay into hadrons according to phase space
→ diquark & heavy quark production suppressed

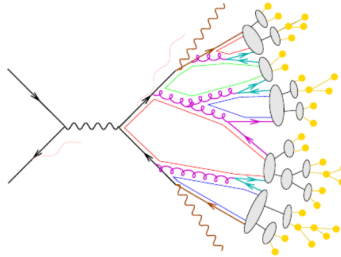
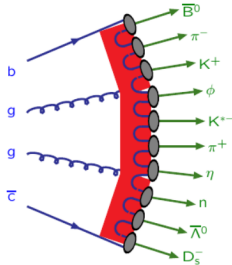
Improved model:

- heavy cluster decay first into lighter cluster, or radiate a hadron
 $C \rightarrow CC$, $C \rightarrow CH$, $C \rightarrow HH$
- leading particle effects incorporated naturally



String vs cluster

Sjöstrand, Durham '09



program	PYTHIA	HERWIG
model	string	cluster
energy-momentum picture	powerful	simple
parameters	predictive	unpredictive
flavour composition	few	many
parameters	messy	simple
	unpredictive	in-between
	many	few

“There ain't no such thing as a parameter-free *good* description”

Hadronisation models

	Hadronisation model
HERWIG++	cluster model
PYTHIA8	Lund string model
SHERPA	modified cluster model

Monte Carle event generation: Introduction

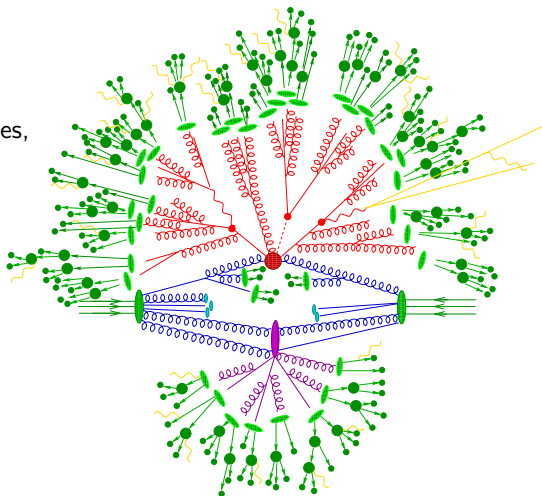
- 1 Parton evolution
- 2 Multi-parton interactions
- 3 Hadronisation
- 4 Hadron decays & QED corrections**
- 5 Analysis and tuning
- 6 Summary

A hadron collider event

Event structure

Factorise into event stages according to characteristic scales, use relevant approximation in each regime

- Hard scattering
- Parton evolution
- Multiple interactions
- Hadronisation
- Hadron decays
- QED corrections



Hadron decays

Manifold task:

- Primordial hadrons are mostly unstable \rightarrow will decay
- > 1000 different decay channels
- vast amount of measured decay tables in PDG
- form factor models for many decays known

Problems:

- BR's in PDG decay tables have uncertainties and in many cases do not add up to one
- specifics of many decays are unknown

Non-trivial effects:

- significantly effects hadronisation yields, event shapes, etc.

Hadron decays: Many aspects

Example decay chain:

$$\begin{aligned} B^{*0} &\rightarrow \gamma B^0 \\ &\rightarrow \bar{B}^0 \\ &\rightarrow e^- \bar{\nu}_e D^{*+} \\ &\rightarrow \pi^+ D^0 \\ &\rightarrow K^- \rho^+ \\ &\rightarrow \pi^+ \pi^0 \\ &\rightarrow \gamma\gamma \end{aligned}$$

Hadron decays: Many aspects

Example decay chain:

$$B^{*0} \rightarrow \gamma B^0$$

$$\rightarrow \bar{B}^0$$

$$\rightarrow e^- \bar{\nu}_e D^{*+}$$

$$\rightarrow \pi^+ D^0$$

$$\rightarrow K^- \rho^+$$

$$\rightarrow \pi^+ \pi^0$$

$$\rightarrow \gamma\gamma$$

EM decay

Hadron decays: Many aspects

Example decay chain:

$$\begin{aligned}
 B^{*0} &\rightarrow \gamma B^0 \\
 &\rightarrow \bar{B}^0 \\
 &\rightarrow e^- \bar{\nu}_e D^{*+} \\
 &\rightarrow \pi^+ D^0 \\
 &\rightarrow K^- \rho^+ \\
 &\rightarrow \pi^+ \pi^0 \\
 &\rightarrow \gamma\gamma
 \end{aligned}$$

Weak neutral meson mixing

Hadron decays: Many aspects

Example decay chain:

$$\begin{aligned} B^{*0} &\rightarrow \gamma B^0 \\ &\rightarrow \bar{B}^0 \\ &\rightarrow e^- \bar{\nu}_e D^{*+} \\ &\quad \rightarrow \pi^+ D^0 \\ &\quad \quad \rightarrow K^- \rho^+ \\ &\quad \quad \quad \rightarrow \pi^+ \pi^0 \\ &\quad \quad \quad \quad \rightarrow \gamma\gamma \end{aligned}$$

Weak decay, three body with form factor models

Hadron decays: Many aspects

Example decay chain:

$$\begin{aligned} B^{*0} &\rightarrow \gamma B^0 \\ &\rightarrow \bar{B}^0 \\ &\rightarrow e^- \bar{\nu}_e D^{*+} \\ &\rightarrow \pi^+ D^0 \\ &\rightarrow K^- \rho^+ \\ &\rightarrow \pi^+ \pi^0 \\ &\rightarrow \gamma\gamma \end{aligned}$$

Strong decay

Hadron decays: Many aspects

Example decay chain:

$$\begin{aligned} B^{*0} &\rightarrow \gamma B^0 \\ &\rightarrow \bar{B}^0 \\ &\rightarrow e^- \bar{\nu}_e D^{*+} \\ &\rightarrow \pi^+ D^0 \\ &\rightarrow K^- \rho^+ \\ &\rightarrow \pi^+ \pi^0 \\ &\rightarrow \gamma\gamma \end{aligned}$$

Weak decay, ρ mass smearing $\Gamma \sim m$

Hadron decays: Many aspects

Example decay chain:

$$\begin{aligned}
 B^{*0} &\rightarrow \gamma B^0 \\
 &\rightarrow \bar{B}^0 \\
 &\rightarrow e^- \bar{\nu}_e D^{*+} \\
 &\rightarrow \pi^+ D^0 \\
 &\rightarrow K^- \rho^+ \\
 &\rightarrow \pi^+ \pi^0 \\
 &\rightarrow \gamma\gamma
 \end{aligned}$$

ρ polarised, angular correlations

Hadron decays: Many aspects

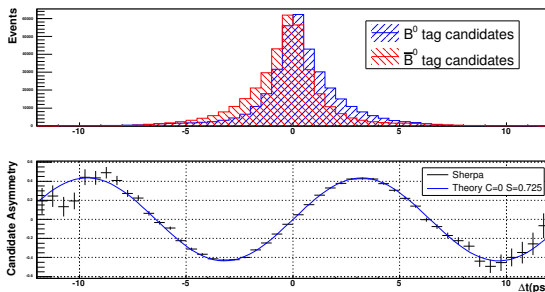
Example decay chain:

$$\begin{aligned}
 B^{*0} &\rightarrow \gamma B^0 \\
 &\rightarrow \bar{B}^0 \\
 &\rightarrow e^- \bar{\nu}_e D^{*+} \\
 &\rightarrow \pi^+ D^0 \\
 &\rightarrow K^- \rho^+ \\
 &\rightarrow \pi^+ \pi^0 \\
 &\rightarrow \gamma\gamma
 \end{aligned}$$

EM decay

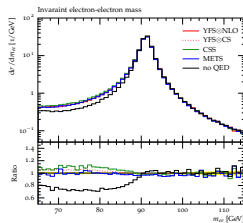
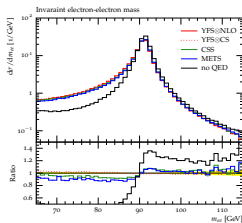
Hadron decays

- previous generation of generators relied on external packages for most important decays: EVTGEN (B -decays) & TAUOLA (τ -decays)
- HERWIG++ & SHERPA contain in-built modules with at least as good a description including spin-correlations and neutral meson mixing
- no interfacing issues as complete information can be passed internally



QED corrections

- previous generation of generators relied on external package for QED corrections: PHOTOS
 - HERWIG++ & SHERPA contain in-built modules with at least as good a description including higher order corrections and preserving spin-correlations,
- both employ YFS-type soft photon resummation
- no interfacing issues as complete information can be passed internally



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Analysis and tuning

RIVET [Buckley et.al. arXiv:0103.0694](#)

- LHC successor to HZT00L collection of exp. data & corresponding analyses
- spirit: “right MC describes everything simultaneously”

PROFESSOR [Buckley et.al. arXiv:0907.2973](#)

- tuning in multi-dimensional model parameter space
- calculate observables at random parameter points
- parametrise to approximate generator response for each observable (bin)
- find parameter point of min. χ^2

Tune comparisons

Deviation metrics per gen/tune and observable group:

Gen	Tune	UE	Dijets	Multijets	Jet shapes	W and Z	Fragmentation	B frag
AlpGen	HERWIG6	—	1.83	5.36	2.48	0.91	—	—
	PYTHIA6-AMBT1	—	1.55	2.80	0.61	0.53	—	—
	PYTHIA6-D6T	—	1.38	2.67	2.31	1.67	—	—
	PYTHIA6-P2010	—	1.09	2.65	2.03	1.48	—	—
	PYTHIA6-P2011	—	1.12	2.60	0.48	0.24	—	—
	PYTHIA6-ZZ	—	1.48	2.63	0.55	0.48	—	—
	PYTHIA6-profQ2	—	1.16	2.65	1.43	1.29	—	—
HERWIG	AUET2-CTEQ6L1	0.43	0.55	0.77	0.35	0.58	22.80	2.38
	AUET2-LOxx	0.25	0.71	0.60	0.39	0.88	22.13	2.29
Herwig++	2.5.1-UE-EE-3-CTEQ6L1	0.27	0.87	0.78	0.51	0.98	10.58	1.32
	2.5.1-UE-EE-3-MRSTLOxx	0.23	1.05	0.78	0.50	0.65	10.58	1.32
PYTHIA6	AMBT1	0.39	1.20	0.54	0.77	0.27	0.93	1.65
	AUET2B-CTEQ6L1	0.16	0.92	0.44	0.59	0.74	0.67	1.29
	AUET2B-LOxx	0.13	1.33	0.55	0.58	1.15	0.67	1.30
	D6T	0.58	0.79	0.50	0.56	1.25	0.36	2.63
	DW	0.81	0.78	0.61	0.56	1.33	0.36	2.63
	P2010	0.30	0.93	0.82	1.07	0.30	0.44	1.75
	P2011	0.12	0.89	0.67	1.02	0.53	0.43	2.13
	ProfQ2	0.51	0.67	0.81	0.51	0.64	0.30	1.65
	ZZ	0.18	0.94	0.73	0.80	0.30	0.95	2.78
	Pythia8	4C	0.30	0.97	0.93	0.50	0.90	0.38
Sherpa	1.3.1	0.68	0.47	0.34	0.71	0.36	0.75	2.48

LH'11 SM WG [arXiv:1203.6803](#)

Summary: MC event generators II

Lecture:

- low energy QCD calculated not from first principles but using phenomenological models
→ many parameters, need tuning to data
- underlying event typically calculated as multiple parton interactions
- two models (string & cluster) for parton to hadron fragmentation
- hadron decays important, $\mathcal{O}(100)$ hadrons with $\mathcal{O}(1000)$ decay channels
- higher order QED corrections from first principles

Tutorial I & II:

- Structure of a Monte Carlo event
- Effect & impact of the individual event stages
- Understand the consequences of the employed approximations

Monte Carlo

training studentships



3-6 month fully funded studentships for current PhD students at one of the MCnet nodes. An excellent opportunity to really understand the Monte Carlos you use!

Application rounds every 3 months.



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Thank you for your attention!