

# QCD at the Energy Frontier

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WE Heraeus School on  
“QCD – Old Challenges and New Opportunities”



[www.ippp.dur.ac.uk](http://www.ippp.dur.ac.uk)



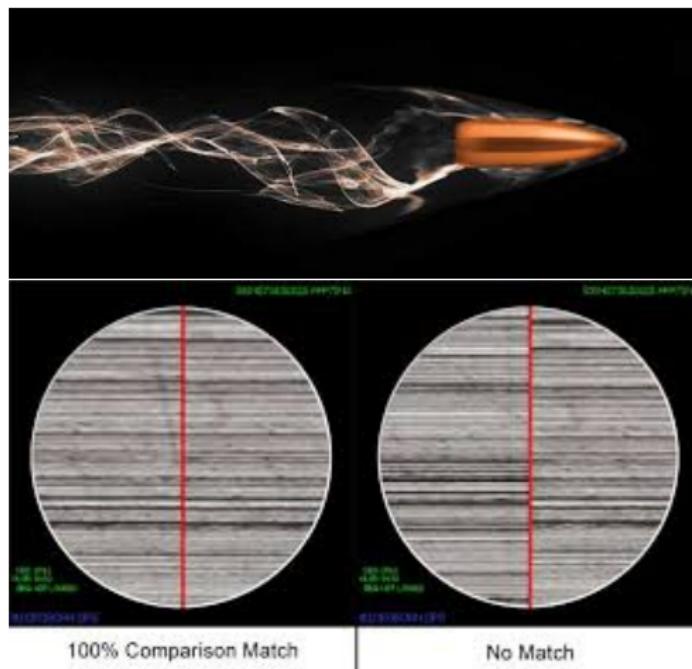
- what the talk is about
- lessons from the LHC
- the quest for precision
- anticipating the future
- summary

# motivation & introduction

# motivation

- QCD = well understood theory with subtle effects
- QCD radiation omnipresent at the LHC
- enters as signal (and background) in high- $p_{\perp}$  analyses
  - multi-jet signatures
    - multijet merging & higher-order matching
  - inner-jet structures e.g. from “fat jets”
    - parton shower algorithms
- begs the question: can we improve our understanding?  
(keep in mind: accuracy vs. precision)
- in addition: interesting physics in QCD alone  
(think about multi-parton interactions, collective phenomena, etc.)

- will need precision for ballistics of smoking guns



# lessons from the LHC

# lessons from the LHC

- jets are ubiquitous: QCD fills phase space if available:  
 $n$ -jet rates may scale beyond  $\alpha_S^n$
- if emissions well-separated: fixed order QCD  
→ works amazingly well
- however: subtle effects when emission logarithms become large  
→ QCD beyond fixed order!
- conceptual problems still open: mainly soft QCD  
hadronization, multiple parton interactions, the “ridge”

perturbation theory works!

# factorization: calculating observables for the LHC

- master formula

$$d\sigma_{pp \rightarrow X} = \sum_{ij} \int_0^1 dx_1 dx_2 f_i(x_1, \mu_F) f_j(x_2, \mu_F) \int d\Phi_X \hat{\sigma}_{ij \rightarrow X}(\{px\}; \mu_F, \mu_R)$$

relating parton-level  $\hat{\sigma}$  with particle-level (observable) cross section  $\sigma$

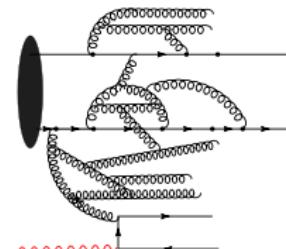
(partons = quarks and gluons)

- based on “factorization”:

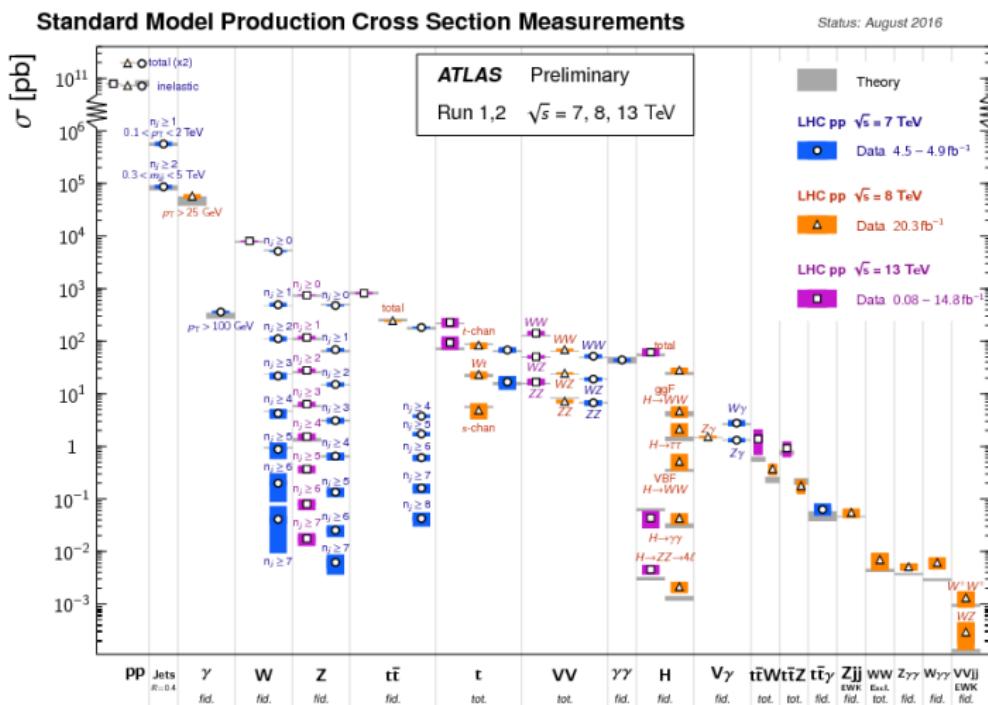
parton distribution function  $f_i(x, \mu_F)$

process-independent if typical momentum scale  $Q \approx \mu_F \gg m_{\text{proton}}$

(PDF = probability to find one parton of type  $i$  with energy fraction  $x$  at factorization scale  $\mu_F$  in proton)



# overall agreement with data



# soft QCD questions

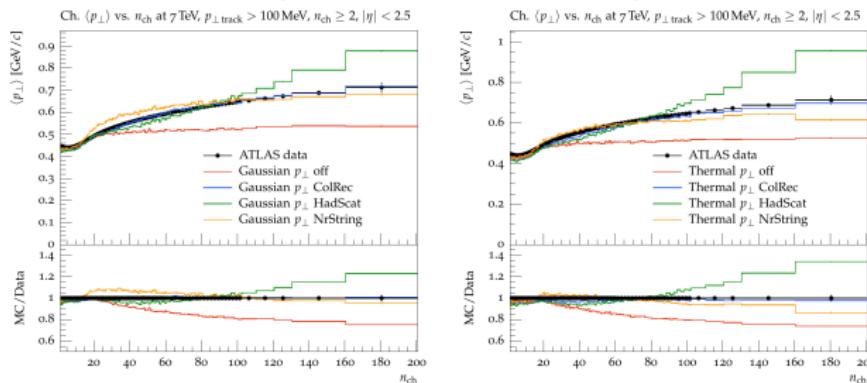
# colour reconnections and friends

(Fischer, Sjostrand, 1610:09818)

Collective flow observed in pp at LHC. Partly unexpected.  
New mechanisms required; could also (partly) replace CR.

Active field, e.g. N. Fischer & TS, arXiv:1610:09818 [hep-ph]:

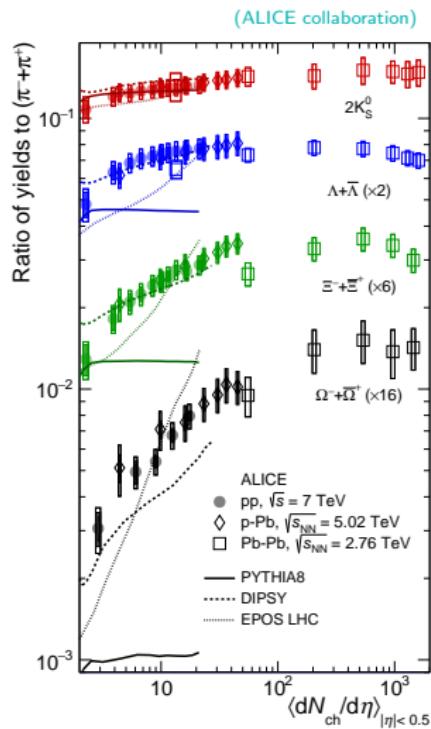
- Thermal  $\exp(-p_{\perp}/T) \rightarrow \exp(-m_{\perp}/T)$  hadronic spectrum.
- Close-packed strings  $\Rightarrow$  increased string  $\kappa$  or  $T$ .
- Dense hadronic gas  $\Rightarrow$  hadronic rescattering.



(slide stolen from Torbjorn Sjostrand)

# strange strangeness

- universality of hadronisation assumed
- parameters tuned to LEP data  
in particular: strangeness suppression
- for strangeness: flat ratios  
but data do not reproduce this
- looks like  $SU(3)$  restoration  
not observed for protons
- needs to be investigated



# beyond factorization

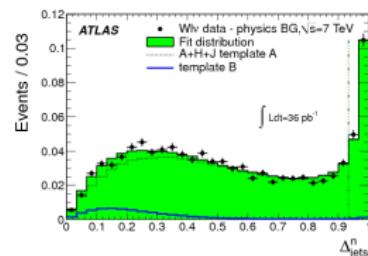
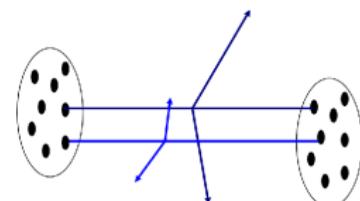
## example: multi-parton interactions

- protons = extended objects  
→ possibility of more parton pairs interacting  
resulting final states may be hard  
in “perturbative regime”  $p_{\perp} \geq$  few GeV
- but: no factorization theorem available  
→ no first-principles theory
- simplistic parameterization

$$\sigma_{X+Y}^{(DPS)} = \frac{\sigma_X \otimes \sigma_Y}{\sigma_{\text{eff}}}$$

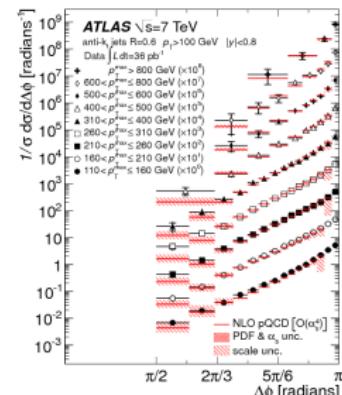
with  $\sigma_{\text{eff}} \approx 15 \text{ mb}$  (measured)

$(\sigma_{\text{tot}} \approx 100 \text{ mb} = 10^{-29} \text{ m}^2 \text{ at LHC})$

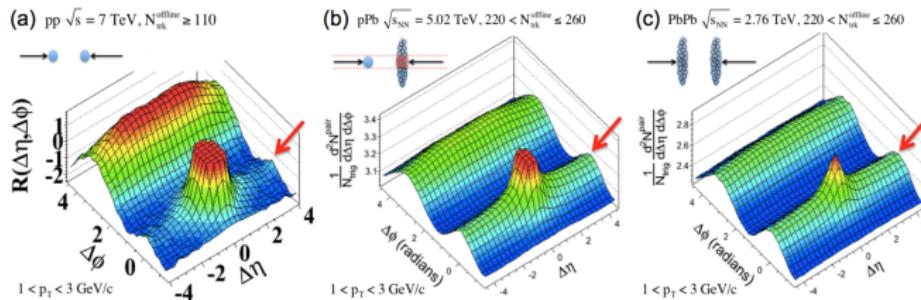


# example: the ridge

- momentum conservation in transverse plane:  
→ in  $2 \rightarrow 2$  collisions particles produced  
“back-to-back”  
→ decorrelation by additional radiation
- well understood in pert.QCD



- however: surprising structure in high-multiplicity  $pp$   
cannot be reproduced in standard pert.QCD Monte Carlo



- typically explained as “collective effect”  
in heavy-ion collisions: “hydrodynamics”  
in  $pp$ : colour-ropes, “glasma”

( colour-glass condensate = non-pert. in weak coupling, glasma = Bose enhancement + Pauli blocking)

- conceptually different from textbook perturbation theory

# the quest for precision

# precision at fixed order

# complex inputs I: parton distribution functions

- PDFs not known from first principles, only their scaling with  $\mu_F$   
(from the Altarelli-Parisi equations)
- fitted from data at different processes, at different,  $\mu_F$ , at different experiments, with different systematics
- current accuracy: next-to-next-to-leading order (NNLO)  
(various collaborations: CTEQ, MMHT, NNPDF, ABM, GRV, HeraPDF)
- needs NNLO calculations and three-loop kernels driving the evolution  
(4-loop kernels partially known; Moch et al., 1707.08315)
- but:  $\alpha_S^2$  is  $\mathcal{O}(1\%)$  – must also include electromagnetic and weak evolution at (N)LO  
(current frontier: LUXqed; Manohar PRL 117 (2016) 242002)

determining reliable PDFs — a complex endeavour

## complex inputs II: partonic cross sections $\hat{\sigma}$

- fully automated evaluation of  $\hat{\sigma}$  at LO and NLO,  
integral over phase space  $d\Phi_X$  with  $3n - 2$  dimensions for  $n$  particles  
→ Monte Carlo methods with involved sampling strategies
- problem beyond LO: occurrence of divergent structures when
  - momenta  $k \rightarrow \infty$  ("ultraviolet divergence")  
regularization and renormalization
  - or  $k \rightarrow 0$  ("infrared divergence")  
regularization and **exact cancellation** between contributions

(Kinoshita–Lee–Nauenberg theorem)

- regularization by analytic continuation  $d^4 k \rightarrow d^D k$  with  $D = 4 + 2\epsilon$   
divergences manifest as poles  $1/\epsilon$
- straightforward for UV divergences but tricky for IR divergences:  
**cancellation** is between contributions of different multiplicity

(and phase space integrals are usually done with Monte Carlo methods)

# the aftermath of the NLO (QCD) revolution

- establishing a wide variety of automated tools for NLO calculations

([BLACKHAT](#), [GoSam](#), [MADGRAPH](#), [NJET](#), [OPENLOOPS](#), [RECOLA](#) + automated IR subtraction methods ([MADGRAPH](#), [SHERPA](#))

- first full NLO (EW) results with automated tools
- technical improvements still mandatory

(higher multis, higher speed, higher efficiency, easier handling, . . . )

- start discussing scale setting prescriptions

(simple central scales for complicated multi-scale processes? test smarter prescriptions?)

- steep learning curve still ahead: “NLO phenomenology”

(example: methods for uncertainty estimates beyond variation around central scale)

# pushing the perturbative order: $gg \rightarrow H$

NLO  $\mathcal{O}(\alpha_s)$

(Dawson; Djouadi et al.; 1990)



NNLO  $\mathcal{O}(\alpha_s^2)$

(Harlander et al., Anastasiou et al.; 2002)



Double virtual

Real-virtual

NNNLO  $\mathcal{O}(\alpha_s^3)$

(Anastasiou et al.; 2015)



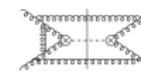
Triple virtual

Real-virtual squared

Double virtual real



Double real



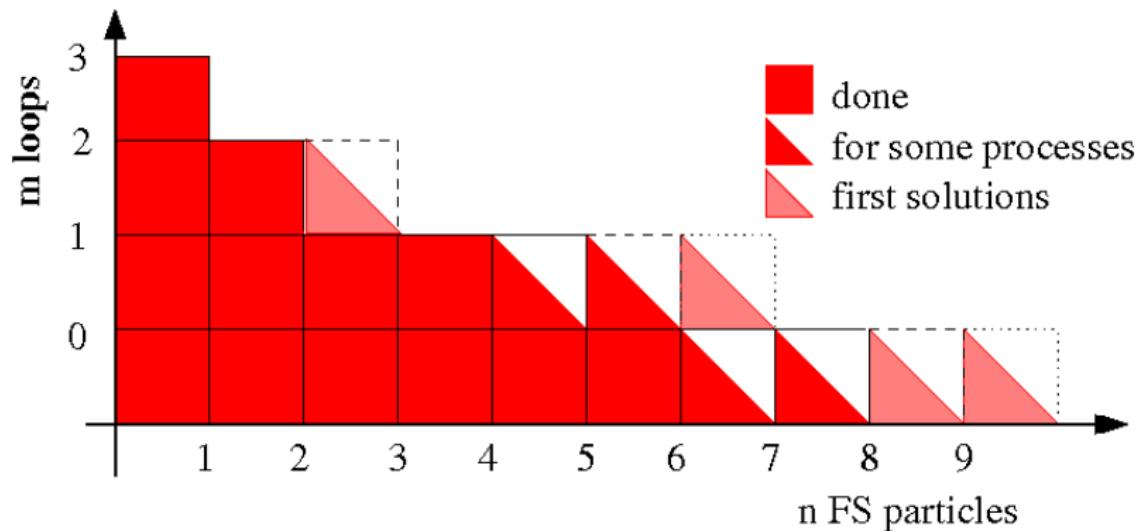
Double real virtual



Triple real

- $\sim 1,000$  Feynman diagrams at NNLO
- $\sim 100,000$  Feynman diagrams at  $N^3LO$   
reduced to  $\sim 1000$  master integrals  $\longrightarrow$  "Symbols"

# technological/complexity limit



# the looming revolution: going beyond NLO

- $H$  in ggF at  $N^3\text{LO}$  (Anastasiou, Duhr and others)
- explosive growth in NNLO (QCD)  $2 \rightarrow 2$  results

(apologies for any unintended omissions)

- $t\bar{t}$  ([1303.6254](#); [1508.03585](#); [1511.00549](#))
- single- $t$  ([1404.7116](#))
- $VV$  ([1507.06257](#); [1605.02716](#); [1604.08576](#); [1605.02716](#))
- $HH$  ([1606.09519](#))
- $VH$  ([1407.4747](#); [1601.00658](#); [1605.08011](#))
- $V\gamma$  ([1504.01330](#))
- $\gamma\gamma$  ([1110.2375](#); [1603.02663](#))
- $Vj$  ([1507.02850](#); [1512.01291](#); [1602.06965](#); [1605.04295](#); [1610.07922](#))
- $Hj$  ([1408.5325](#); [1504.07922](#); [1505.03893](#); [1508.02684](#); [1607.08817](#))
- $jj$  ([1310.3993](#); [1611.01460](#))

- NLO corrections to  $gg \rightarrow VV$  ([1605.04610](#))
- $WBF$  at NNLO ([1506.02660](#)) and  $N^3\text{LO}$  ([1606.00840](#))
- different IR subtraction schemes:  
N-jettiness slicing, antenna subtraction, sector decomposition,

# living with the revolution

- we will include them into full simulations

(I am willing to place a bet: 3 years at most!)

- practical limitations/questions to be overcome:

- dealing with IR divergences at NNLO: slicing vs. subtracting

(I'm not sure we have THE solution yet)

- how far can we push NNLO? are NLO automated results stable enough for NNLO at higher multiplicity?
  - matching for generic processes at NNLO?

(MINLO or UN<sup>2</sup>LoPs or something new?)

- more scales (internal or external) complicated – need integrals

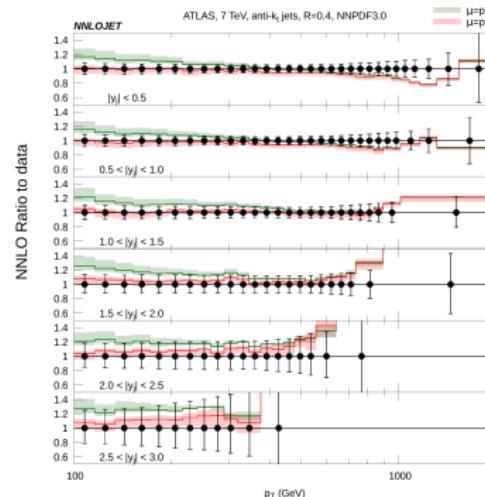
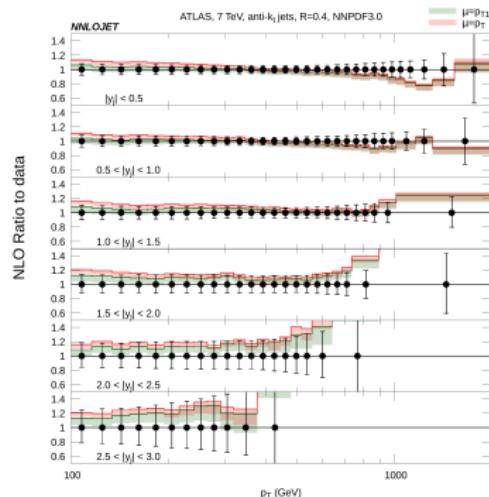
- more philosophical questions:

- going to higher power of  $N$  often driven by need to include larger FS multiplicity – maybe not the most efficient method
  - limitations of perturbative expansion:
    - breakdown of factorisation at HO (Seymour et al.)
    - higher-twist: compare  $(\alpha_S/\pi)^n$  with  $\Lambda_{\text{QCD}}/M_Z$

# a scale puzzle at NNLO

J. Currie et al., Acta Phys.Polon. B48 (2017) 955

- common lore: higher orders stabilise/reduce scale dependence
- but: look at inclusive jet- $p_T$

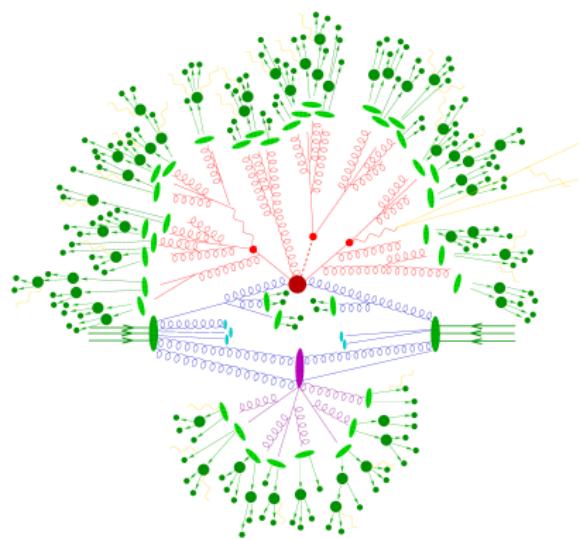


# status of precision simulations

# embedding in full simulations

- fixed-order perturbation theory does not give full picture of  $p\bar{p}$  collisions at LHC.
- more particles produced by
  - radiation of secondaries
  - all-orders PT in approximation
  - transition from quarks & gluons to hadrons
  - decays of unstable hadrons & QED radiation
  - multiple interactions
- all in numerical simulation

combination of first principles PT, effective theories, heavy modelling, and fitting to data



## reminder: how parton showers work

- parton showers are approximations, based on  
leading colour, leading logarithmic accuracy, spin-average
- parametric accuracy by comparing Sudakov form factors:

$$\Delta = \exp \left\{ - \int \frac{dk_\perp^2}{k_\perp^2} \left[ A \log \frac{k_\perp^2}{Q^2} + B \right] \right\},$$

where  $A$  and  $B$  can be expanded in  $\alpha_S(k_\perp^2)$

- $Q_T$  resummation includes  $A_{1,2,3}$  and  $B_{1,2}$   
(transverse momentum of Higgs boson etc.)
- showers usually include terms  $A_{1,2}$  and  $B_1$   
 $A$  = cusp terms ("soft emissions"),  $B \sim$  anomalous dimensions  $\gamma$

# a new shower implementation — DIRE

(S.Höche & S.Prestel, Eur.Phys.J. C75 (2015) 461)

- evolution and splitting parameter  $((ij) + k \rightarrow i + j + k)$ :

$$\kappa_{j,ik}^2 = \frac{4(p_i p_j)(p_j p_k)}{Q^4} \quad \text{and} \quad z_j = \frac{2(p_j p_k)}{Q^2}.$$

- splitting functions including IR regularisation

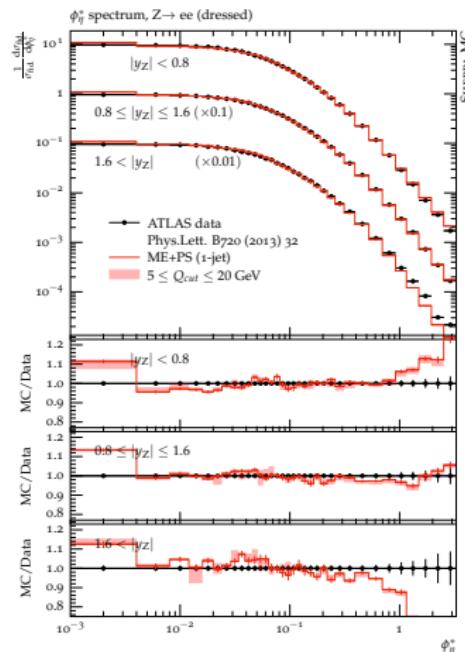
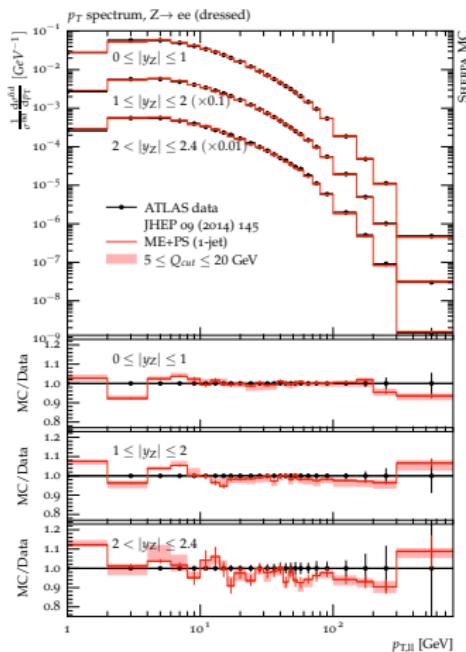
(a la Curci, Furmanski & Petronzio, Nucl.Phys. B175 (1980) 27-92)

$$\begin{aligned} P_{qq}^{(0)}(z, \kappa^2) &= 2C_F \left[ \frac{1-z}{(1-z)^2 + \kappa^2} - \frac{1+z}{2} \right], \\ P_{qg}^{(0)}(z, \kappa^2) &= 2C_F \left[ \frac{z}{z^2 + \kappa^2} - \frac{2-z}{2} \right], \\ P_{gg}^{(0)}(z, \kappa^2) &= 2C_A \left[ \frac{1-z}{(1-z)^2 + \kappa^2} - 1 + \frac{z(1-z)}{2} \right], \\ P_{gq}^{(0)}(z, \kappa^2) &= T_R \left[ z^2 + (1-z)^2 \right] \end{aligned}$$

- renormalisation/factorisation scale given by  $\mu = \kappa^2 Q^2$
- combine gluon splitting from two splitting functions with different spectators  $k \rightarrow$  accounts for different colour flows

# LO results for Drell-Yan

(example of accuracy in description of standard precision observable)



# $g \rightarrow Q\bar{Q}$ — a systematic nightmare

- parton showers geared towards collinear & soft emissions of gluons

(double log structure)



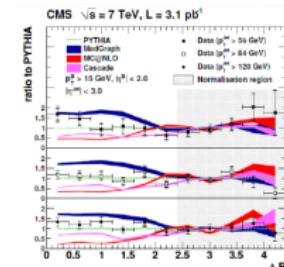
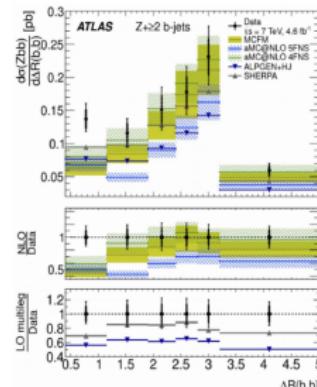
- $g \rightarrow q\bar{q}$  only collinear
- old measurements at LEP of  $g \rightarrow b\bar{b}$  and  $g \rightarrow c\bar{c}$  rate

- fix this at LHC for modern showers

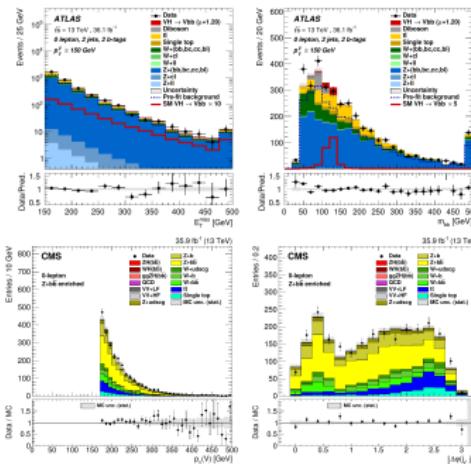
(important for  $t\bar{t}b\bar{b}$ )

- questions: kernel, scale in  $\alpha_S$

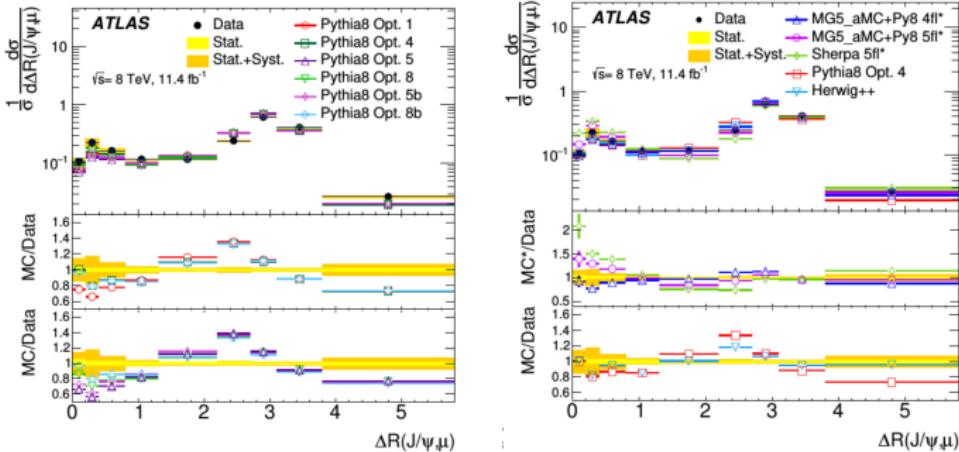
(example:  $k_\perp$  vs.  $m_{bb}$ )



- flagship measurements:  
 $VH \rightarrow b\bar{b}$ ,  $t\bar{t}H \rightarrow b\bar{b}$ , ...
- many searches with  $b$ 's
- influences  $b$ -tag rate  
 ("double"- $b$  jets = gluon jets)
- can cause problems in highly boosted regime



- ATLAS measurement in  $b\bar{b}$  production
- use decay products in  $B \rightarrow J/\Psi(\mu\mu) + X$  and  $B \rightarrow \mu + X$
- use muons as proxies, most obvious observable  $\Delta R(J\Psi, \mu)$



# matching at NLO and NNLO

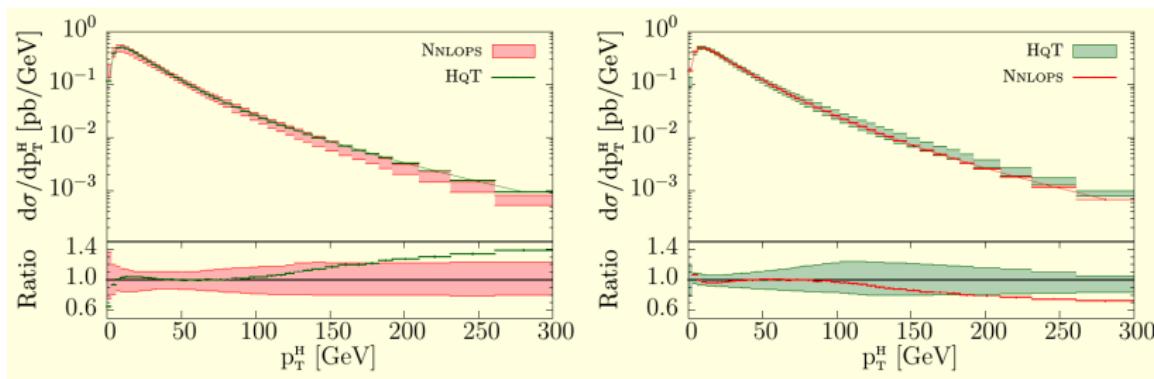
- avoid double-counting of emissions
- two schemes at NLO: Mc@NLO and POWHEG
  - mismatches of  $K$  factors in transition to hard jet region
  - Mc@NLO: → visible structures, especially in  $gg \rightarrow H$
  - POWHEG: → high tails, cured by  $h$  dampening factor
  - well-established and well-known methods

(no need to discuss them any further)

- two schemes at NNLO: MINLO & UN<sup>2</sup>LOPs (singlets  $S$  only)
  - different basic ideas
  - MINLO:  $S + j$  at NLO with  $p_T^{(S)} \rightarrow 0$  and capture divergences by reweighting internal line with analytic Sudakov, NNLO accuracy ensured by reweighting with full NNLO calculation for  $S$  production
  - UN<sup>2</sup>LOPs identifies and subtracts and adds parton shower terms at FO from  $S + j$  contributions, maintaining unitarity
  - available for two simple processes only: DY and  $gg \rightarrow H$

# NNLOPs for $H$ production: MINLO

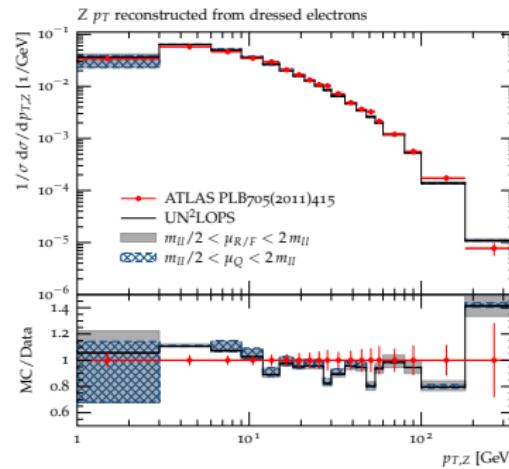
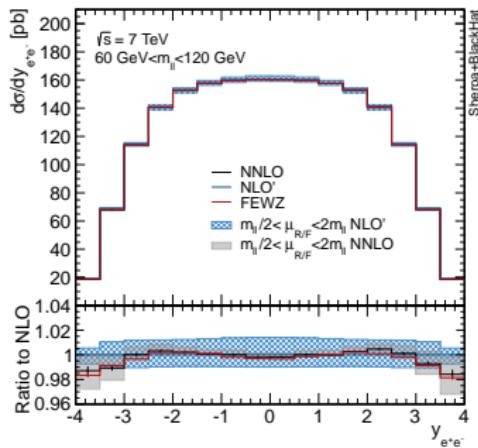
K. Hamilton, P. Nason, E. Re & G. Zanderighi, JHEP 1310



- also available for  $Z/W/VH$  production

# NNLOPs for $Z$ production: UN<sup>2</sup>LOPs

S. Hoche, Y. Li, & S. Prestel, Phys.Rev.D90 & D91



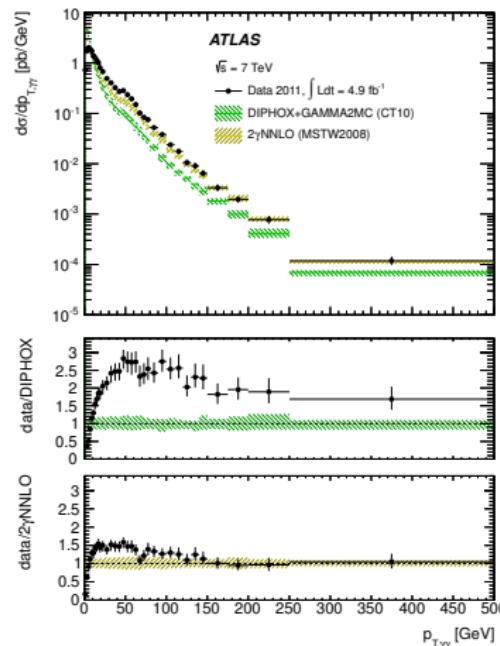
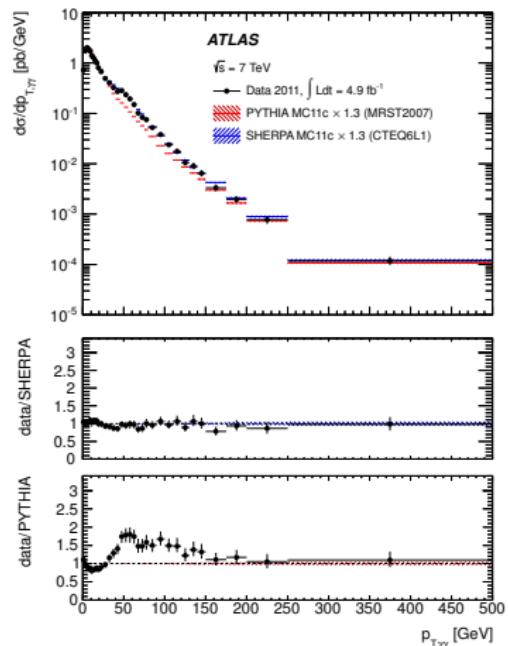
- also available for  $H$  production

# NNLOPs: shortcomings/limitations

- MINLO relies on knowledge of  $B_2$  terms from analytic resummation  
→ to date only known for colour singlet production
- MINLO relies on reweighting with full NNLO result  
→ one parameter for  $H(y_H)$ , more complicated for  $Z, \dots$
- UN<sup>2</sup>LOPs relies on integrating single- and double emission to low scales and combination of unresolved with virtual emissions  
→ potential efficiency issues, need NNLO subtraction
- UN<sup>2</sup>LOPs puts unresolved & virtuals in “zero-emission” bin  
→ no parton showering for virtuals (?)

# merging example: $p_{\perp,\gamma\gamma}$ in MEPS@LO vs. NNLO

(arXiv:1211.1913 [hep-ex])



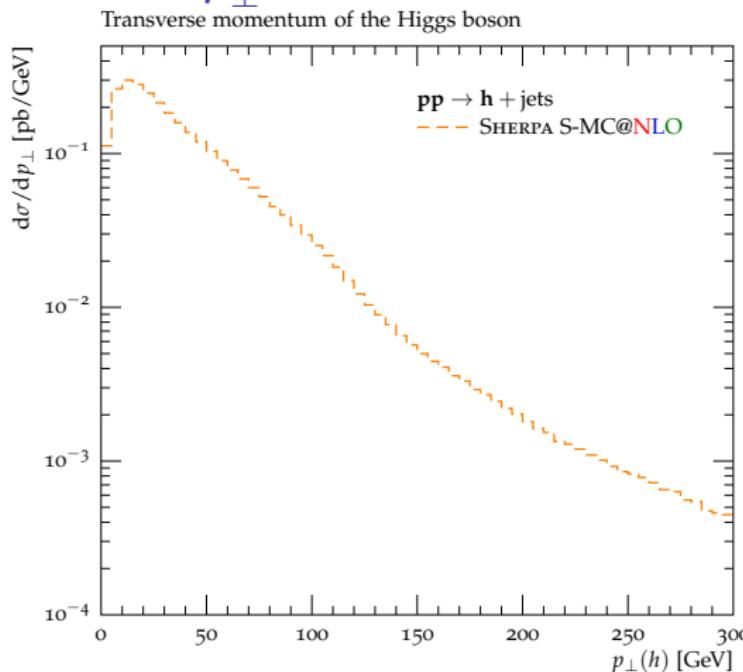
# multijet-merging at NLO

- sometimes “more legs” wins over more loops
- basic idea like at LO: towers of MEs with increasing jet multi (but this time at NLO)
- combine them into one sample, remove overlap/double-counting
- maintain NLO and LL accuracy of ME and PS
- this effectively translates into a merging of Mc@NLO simulations and can be further supplemented with LO simulations for even higher final state multiplicities
- different implementations, parametric accuracy not always clear

(MEPs@NLO, FxFx, UNLoPs)

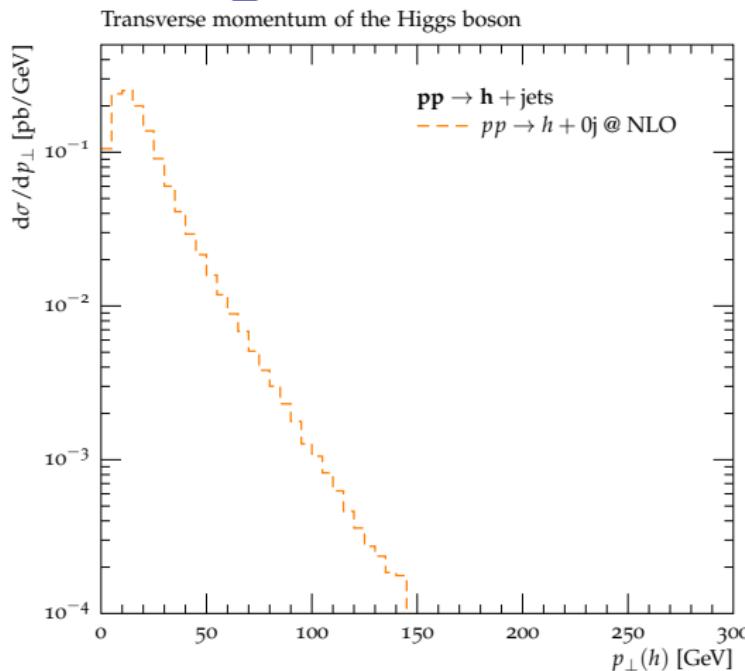
- starts being used, still lacks careful cross-validation

# illustration: $p_T^H$ in MEPS@NLO



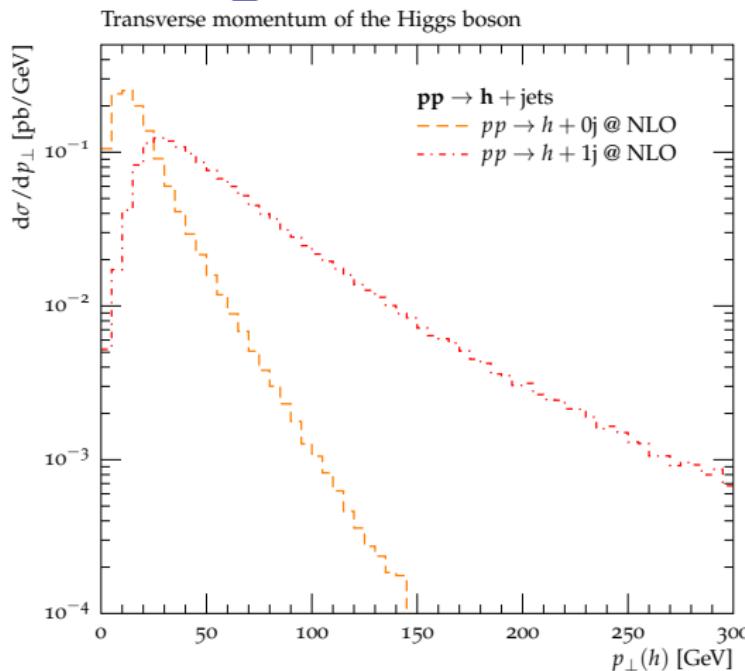
- first emission by MC@NLO

# illustration: $p_\perp^H$ in MEPS@NLO



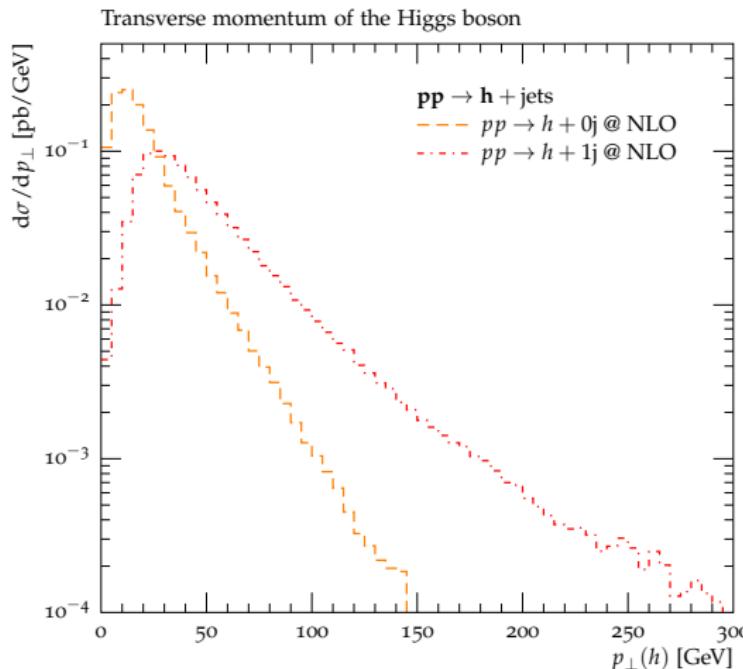
- first emission by MC@NLO , restrict to  $Q_{n+1} < Q_{\text{cut}}$

# illustration: $p_T^H$ in MEPS@NLO



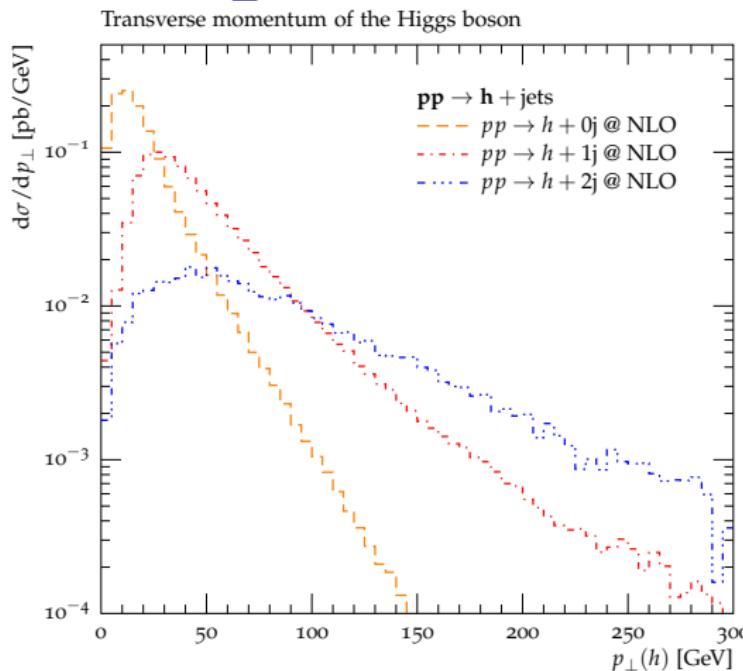
- first emission by MC@NLO , restrict to  $Q_{n+1} < Q_{\text{cut}}$
- MC@NLO  $\text{pp} \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$

# illustration: $p_T^H$ in MEPS@NLO



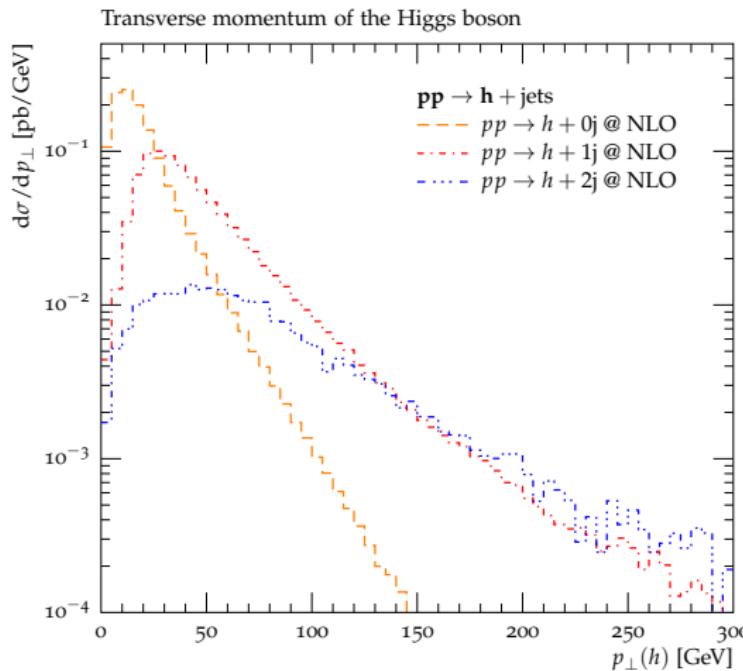
- first emission by MC@NLO , restrict to  $Q_{n+1} < Q_{\text{cut}}$
- MC@NLO  $\text{pp} \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $\text{pp} \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$

# illustration: $p_T^H$ in MEPS@NLO



- first emission by MC@NLO , restrict to  $Q_{n+1} < Q_{\text{cut}}$
- MC@NLO  $\text{pp} \rightarrow \text{h} + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $\text{pp} \rightarrow \text{h} + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
- MC@NLO  $\text{pp} \rightarrow \text{h} + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$

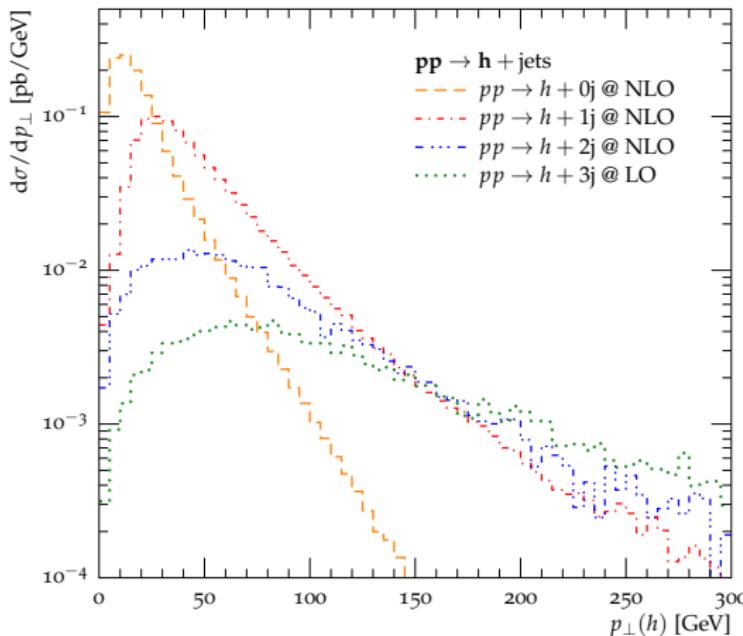
# illustration: $p_\perp^H$ in MEPS@NLO



- first emission by MC@NLO , restrict to  $Q_{n+1} < Q_{\text{cut}}$
- MC@NLO  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off  $pp \rightarrow h + \text{jet}$  to  $Q_{n+2} < Q_{\text{cut}}$
- MC@NLO  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate

# illustration: $p_T^H$ in MEPS@NLO

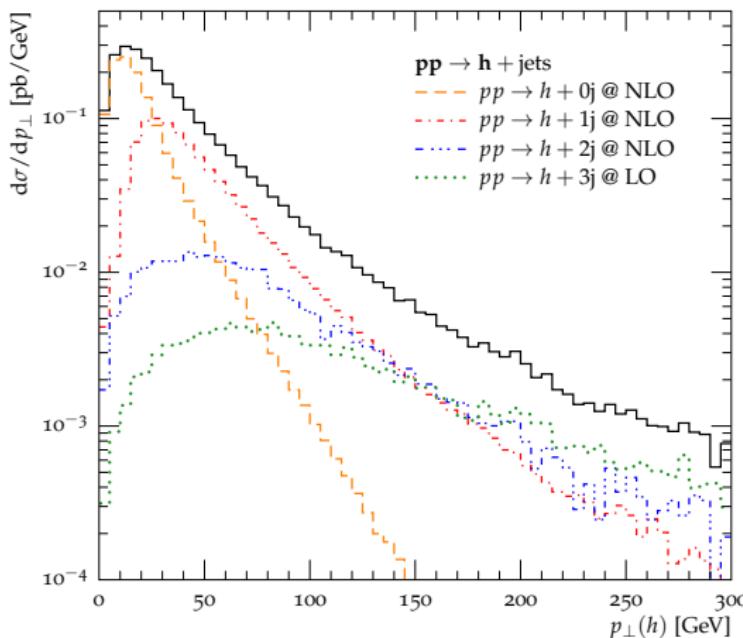
Transverse momentum of the Higgs boson



- first emission by MC@NLO , restrict to  $Q_{n+1} < Q_{cut}$
- MC@NLO  $pp \rightarrow h + jet$  for  $Q_{n+1} > Q_{cut}$
- restrict emission off  $pp \rightarrow h + jet$  to  $Q_{n+2} < Q_{cut}$
- MC@NLO  $pp \rightarrow h + 2jets$  for  $Q_{n+2} > Q_{cut}$
- iterate

# illustration: $p_T^H$ in MEPS@NLO

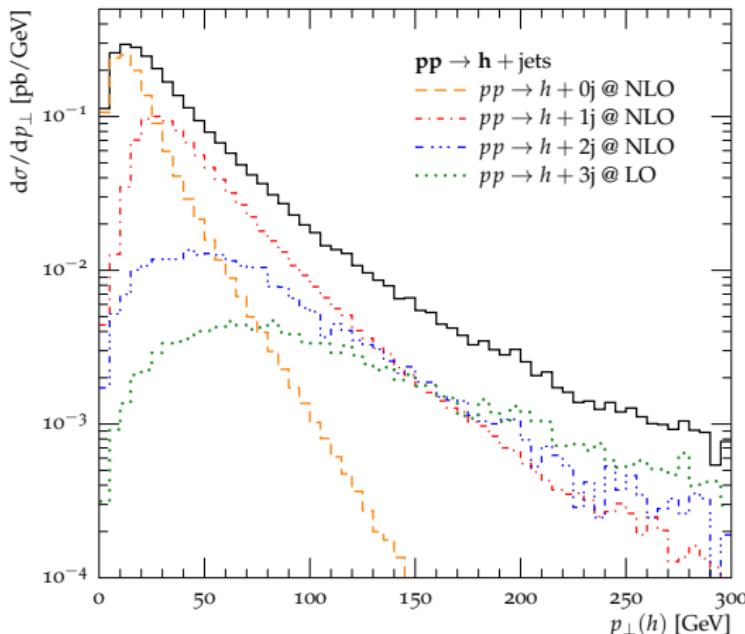
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- iterate
- sum all contributions

# illustration: $p_\perp^H$ in MEPS@NLO

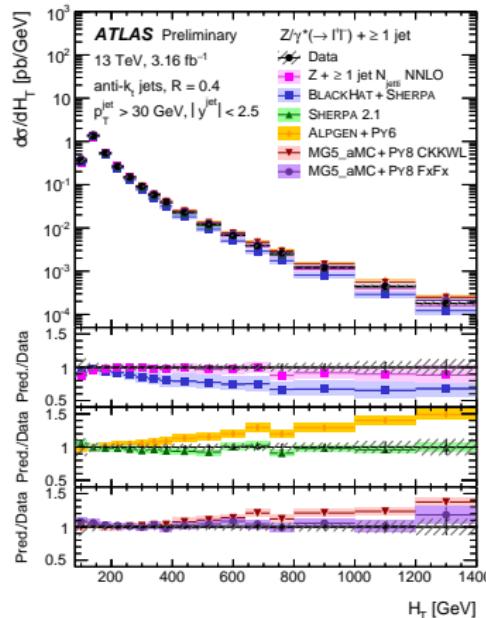
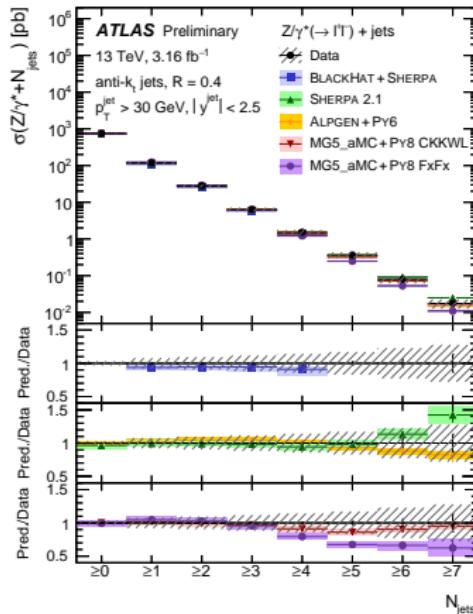
Transverse momentum of the Higgs boson



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- MC@NLO  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$
- iterate
- sum all contributions
- eg.  $p_\perp(h) > 200$  GeV has contributions fr. multiple topologies

# Z+jets at 13 Tev: comparison with ATLAS data

- various merging codes at LO and NLO



# pushing the envelope: showering at NLO accuracy

# Including NLO splitting kernels

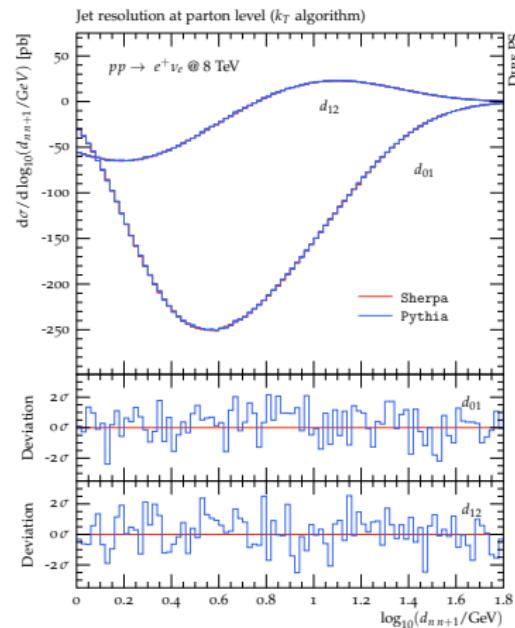
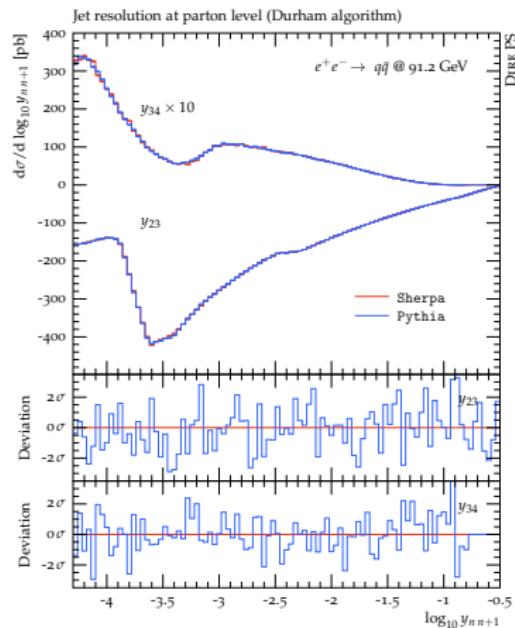
( Hoeche, FK & Prestel, 1705.00982, and Hoeche & Prestel, 1705.00742)

- expand splitting kernels as

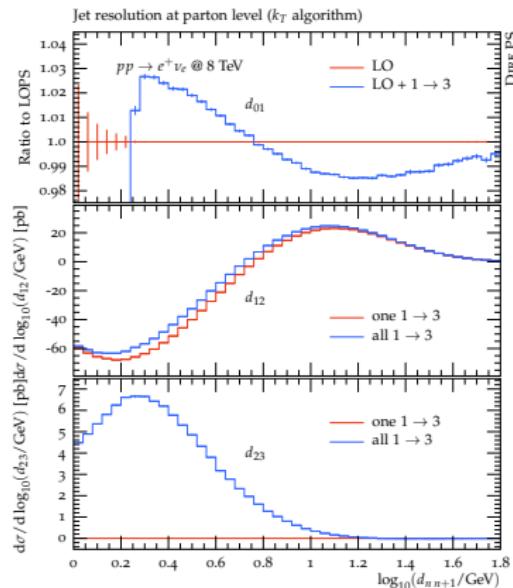
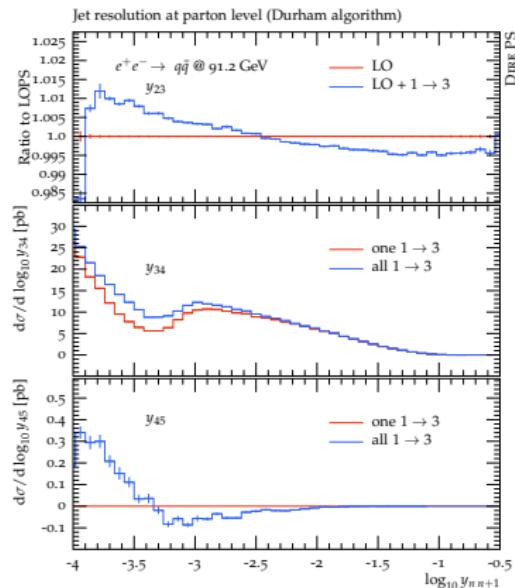
$$P(z, \kappa^2) = P^{(0)}(z, \kappa^2) + \frac{\alpha_S}{2\pi} P^{(1)}(z, \kappa^2)$$

- aim: reproduce DGLAP evolution at NLO
  - include all NLO splitting kernels
- three categories of terms in  $P^{(1)}$ :
  - cusp (universal soft-enhanced correction)  
(already included in original showers)
  - corrections to  $1 \rightarrow 2$
  - new flavour structures (e.g.  $q \rightarrow q'$ ), identified as  $1 \rightarrow 3$
- new paradigm: **two independent implementations**

# validation of $1 \rightarrow 3$ splittings

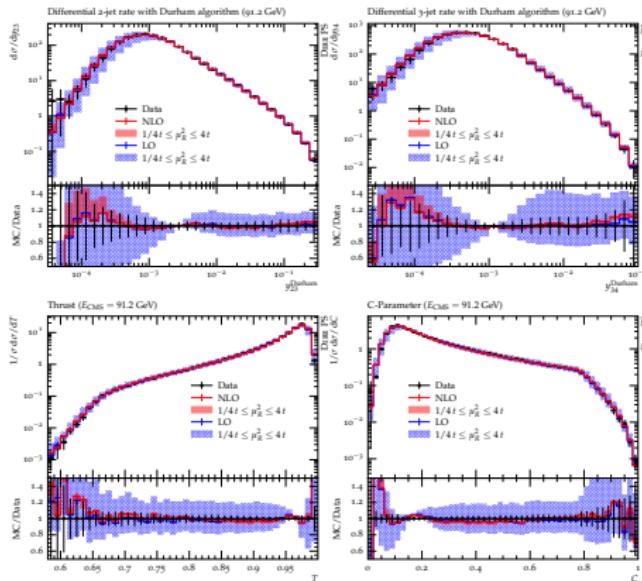


# impact of $1 \rightarrow 3$ splittings



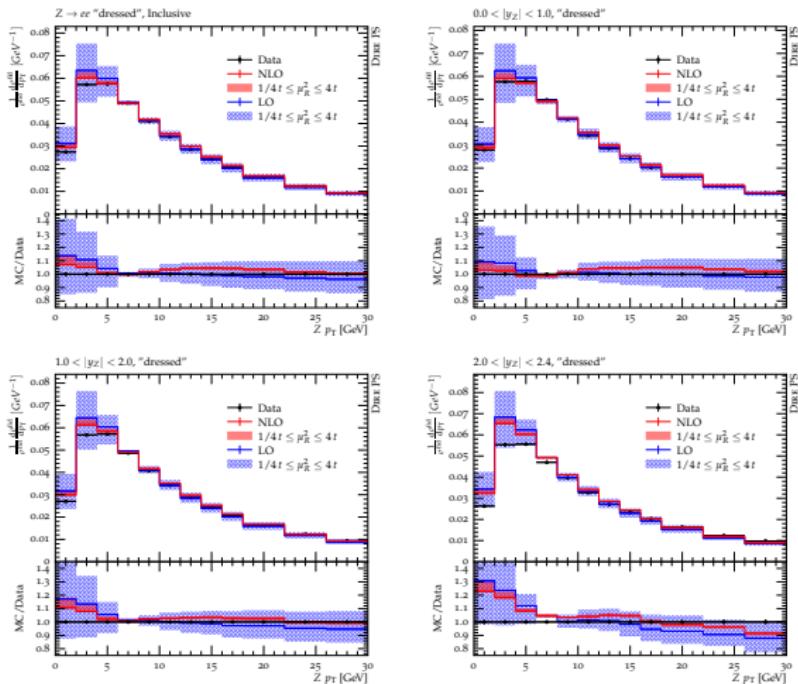
# physical results: $e^- e^+ \rightarrow \text{hadrons}$

(Hoeche, FK & Prestel, 1705.00982)

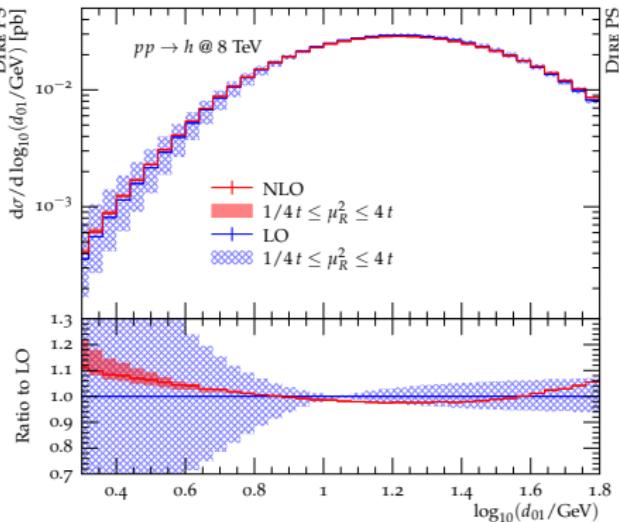
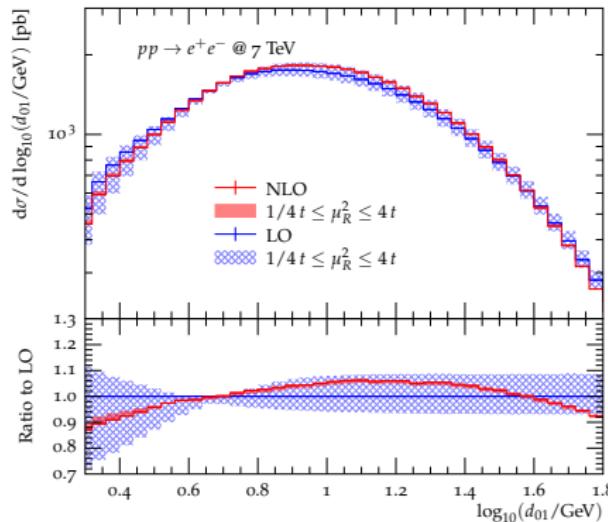


# physical results: DY at LHC

(untuned showers vs. 7 TeV ATLAS data)



# physical results: differential jet rates at LHC



limitations

and

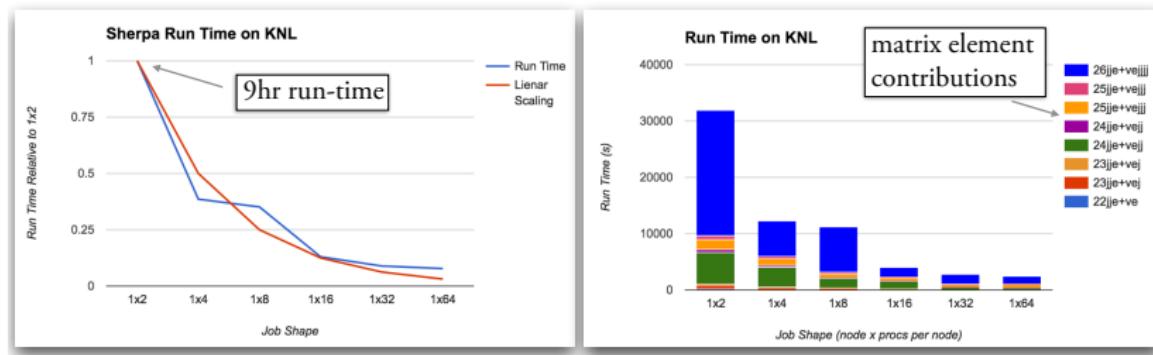
future challenges

# theory challenges

# limitation: computing short-distance cross sections – LO

(Childers, Uram, LeCompte, Benjamin, Hoeche, CHEP 2016)

- challenge of efficiency on tomorrow's (& today's) computers
- 2000's paradigm: memory free, flops expensive  
(example: 16-core Xeon, 20MB L2 Cache, 64GB RAM)
- 2020's paradigm: flops free, memory expensive & must be managed  
(example: 68-core Xeon KNL, 34MB L2 Cache, 16GB HBM, 96GB RAM)
- may trigger rewrites of code to account for changing paradigm



(figures stolen from Taylor Childers' talk at CHEP)

# theory limitations/questions

- we have constructed lots of tools for precision physics at LHC
  - but we did not cross-validate them careful enough (yet)
  - but we did not compare their theoretical foundations (yet)
- we also need unglamorous improvements on existing tools:
  - account for new computer architectures and HPC paradigms
  - systematically check advanced scale-setting schemes (MINLO)
  - automatic (re-)weighting for PDFs & scales
  - scale compensation in PS is simple (implement and check)
- 4 vs. 5 flavour scheme → really?
- how about  $\alpha_S$ : range from 0.113 to 0.118

(yes, I know, but still - it bugs me)

→ is there any way to settle this once and for all (measurements?)

# achievable goals (I believe we know how to do this)

- NLO for loop-induced processes:
  - fixed-order starting, MC@NLO tedious but straightforward
- EW NLO corrections with tricky/time-consuming calculation setup
  - but important at large scales: effect often  $\sim$  QCD, but opposite sign
  - need maybe faster approximation for high-scales (EW Sudakovs)
  - work out full matching/merging instead of approximations
- improve parton shower:
  - beyond (next-to) leading log, leading colour, spin-averaged
  - HO effects in shower and scale uncertainties
  - start including next-to leading colour
  - include spin-correlations → important for EW emissions

# more theory uncertainties/issues?

- with NNLOPS approaching 5% accuracy or better:
  - non-perturbative uncertainties start to matter:  
→ PDFs, MPIs, hadronization, etc.
  - question (example): with hadronization tuned to quark jets (LEP)  
→ how important is the “chemistry” of jets for JES?  
→ can we fix this with measurements?
  - example PDFs: to date based on FO vs. data  
→ will we have to move to resummed/parton showered?

(reminder: LO\* was not a big hit, though)

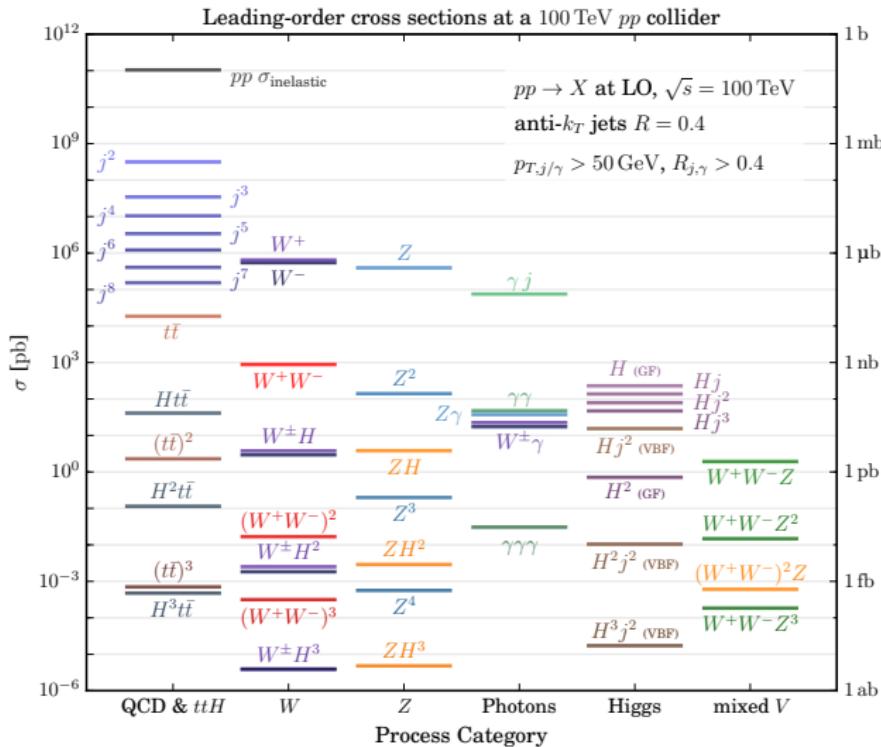
- $g \rightarrow q\bar{q}$  at accuracy limit of current parton showers:
  - how bad are  $\sim 25\%$  uncertainty on  $g \rightarrow b\bar{b}$ ?
  - can we fix this with measurements?

# opportunities at 100 TeV

## some general observations

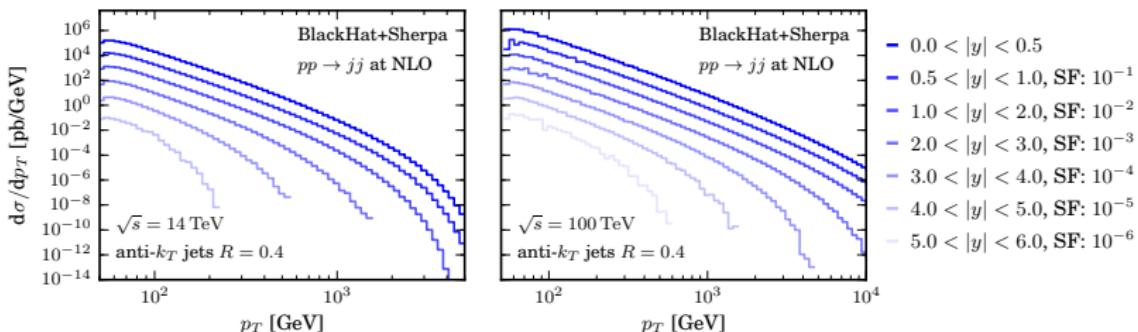
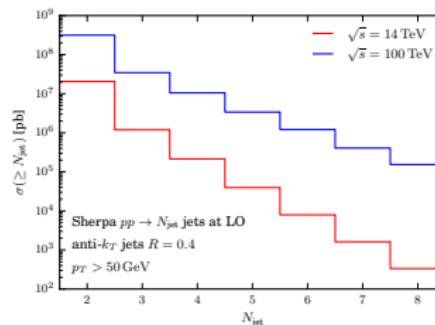
- (sea-) parton luminosities go with  $x^{-\lambda}$ 
  - steep increase in soft jet production
  - “soft @ LHC”  $\neq$  “soft @ 100 TeV”
- interesting opportunities for double-parton scattering
- ridge with 10 GeV  $p_{\perp}$  hadrons?
  - ↔ interface perturbative – non-perturbative?
- jets will be more collimated – challenges for sub-jet measurements

# cross sections potpourri

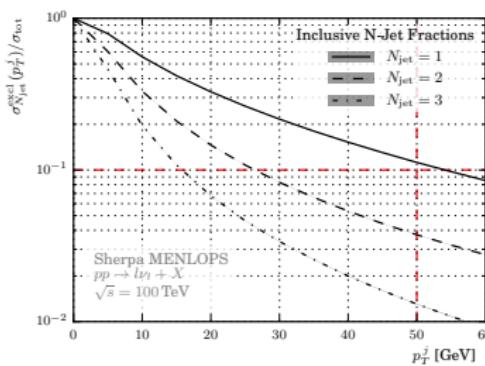
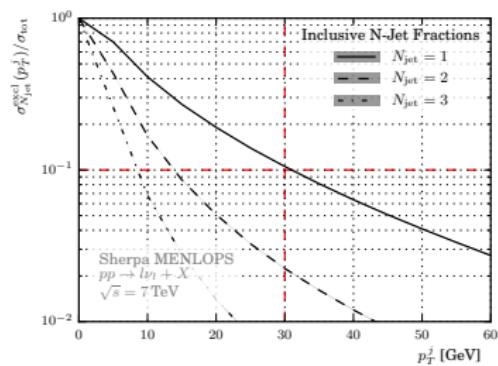


# scaling of jet rates with c.m. energy

- more jets
- higher transverse momenta
- jets more collimated
- $\sigma(p_T \geq 10\text{ TeV}) \approx 100 \text{ ab}$
- different scaling patterns

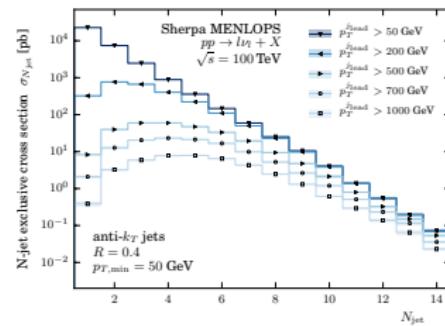


# “typical” jet- $p_T$ in $W + \text{jets}$

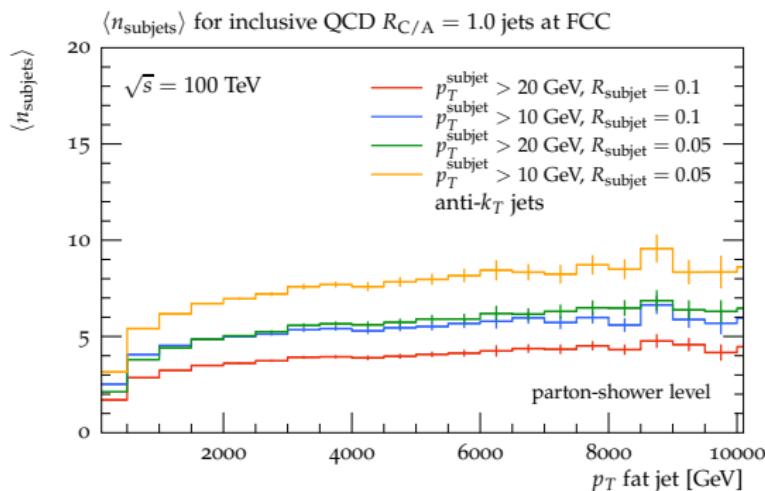


# staircase to Poisson

- scaling patterns in multijet production
- may provide insight where precise calculations fail
- two extreme cases:  
staircase vs. Poissonian



# jet substructure



# summary

# summary

- QCD at energy frontier full of challenges & surprises
- increasing accuracy and precision of LHC drives
  - rapid development of calculational techniques  
(with a lot of exciting mathematical developments)
  - rapid development of ever more detailed simulations  
(stress-testing computational abilities in soft- and hardware)
- first measurements with boosted topologies  
→ jet substructures become analysis tool
- not covered, but: novel analysis methods (ML & friends)

