

PDF dependence of W/Z cross sections and lepton charge asymmetry at the LHC

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Working Group on Electroweak precision measurements at the LHC
CERN, Geneva, 5th April 2011

Outline of talk

1 Preliminaries

- Heavy quarks in deep-inelastic scattering
- Current status of PDFs from different fitting groups
- Comparison of quark–antiquark luminosity functions
- Comparison of α_S values from different fitting groups

2 W and Z total cross sections

- Settings for calculations
- Comparison of W and Z total cross sections
- Comparison of W^+ and W^- total cross sections
- Two-dimensional total cross section plots
- Comments on acceptance calculations

3 Lepton charge asymmetry from W decays

- Comparison of asymmetry for different PDFs
- Comparison of $u_v \pm d_v$ for different PDFs

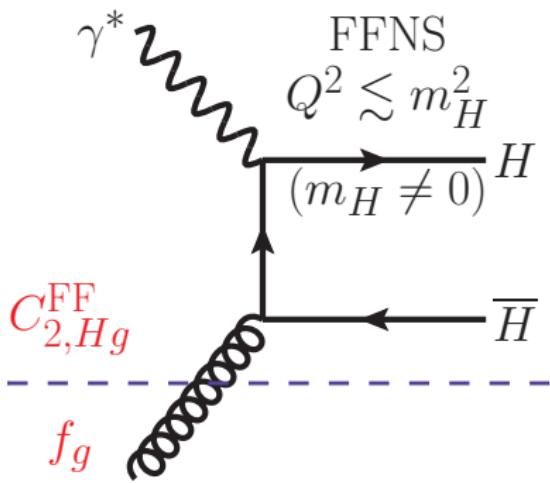
4 Use of K -factors

- Motivation and methods
- K -factors for lepton charge asymmetry
- Z/γ^* rapidity distribution at the LHC

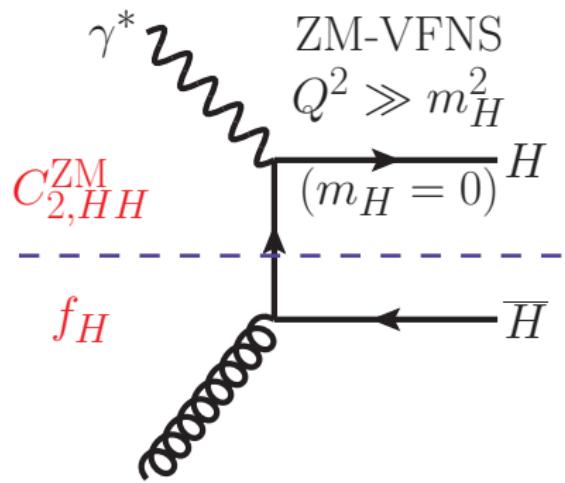
5 Summary

- Summary

Heavy quark contribution to DIS structure function F_2



Fixed flavour number scheme



Zero-mass variable flavour number scheme

- $\sigma_{W,Z}$ at LHC sensitive to light quark PDFs at $x \sim 0.01$ determined from HERA $F_2(x, Q^2)$ data with significant F_2^{charm} .
- **General-mass variable flavour number scheme (GM-VFNS)** interpolates between two well-defined regions ($H \equiv c, b$): **FFNS** for $Q^2 \leq m_H^2$, **ZM-VFNS** for $Q^2 \gg m_H^2$.
- Ambiguous up to $\mathcal{O}(m_H^2/Q^2) \Rightarrow$ theory uncertainty on $\sigma_{W,Z}$.

Impact of heavy quarks in DIS on $\sigma_{W,Z}$ at LHC

Impact of GM-VFNS variation [R. Thorne, arXiv:1006.5925]

- Uncertainty $\sim 2\%$ at NLO, but less than 1% at NNLO.

Impact of (pole-mass) $m_{c,b}$ variation [MSTW, arXiv:1007.2624]

- Vary $m_c = 1.40 \pm 0.15$ GeV \Rightarrow just over 1% change in $\sigma_{W,Z}$.
- Vary $m_b = 4.75 \pm 0.25$ GeV \Rightarrow negligible change (0.1%).

LHC, $\sqrt{s} = 7$ TeV	$B_{\ell\nu} \cdot \sigma^W$	$B_{\ell^+\ell^-} \cdot \sigma^Z$
PDF only uncertainty	+1.7% -1.6%	+1.7% -1.5%
PDF+ α_S uncertainty	+2.5% -1.9%	+2.5% -1.9%
PDF+ $\alpha_S+m_{c,b}$ uncertainty	+2.7% -2.2%	+2.9% -2.4%

- Combined HERA I data: upwards shift in $\sigma_{W,Z}$ by 1–2% [MSTW, arXiv:1006.2753]. HERA II and F_2^{charm} data to come.
- Future theoretical improvements: “optimal” GM-VFNS [R. Thorne, arXiv:1006.5925], possible use of $\overline{\text{MS}}$ mass.

Current status of proton PDFs from different groups

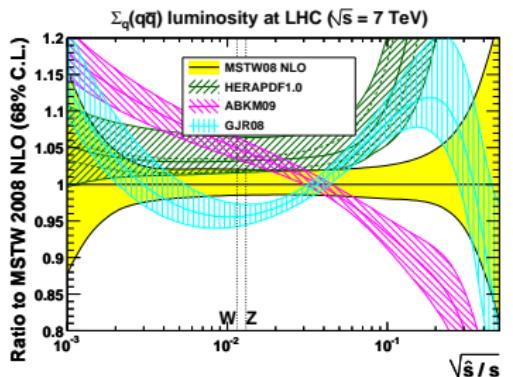
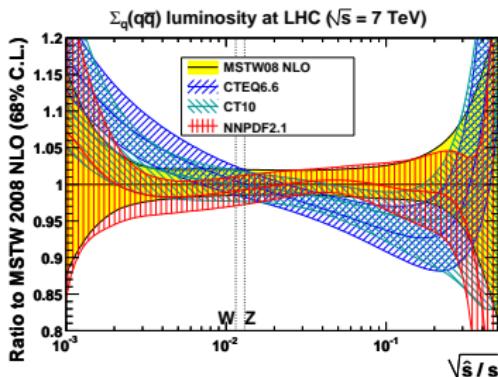
- Consider only *public* sets, where “public” \equiv available in LHAPDF.
- Highlight major differences in data and theory between groups:

	MSTW08	CTEQ6.6/CT10	NNPDF2.1	HERAPDF1.0/1.5	ABKM09	GJR08/JR09
HERA DIS	✓		✓	✓	✓	✓
Fixed-target DIS	✓		✓	✗	✓	✓
Fixed-target DY	✓		✓	✗	✓	✓
Tevatron W, Z	✓		✓	✗	✗	✗
Tevatron jets	✓		✓	✗	✗	✓
GM-VFNS	✓		✓	✓	✗	✗
NNLO	✓	✗	✗	✓	✓	✓

- “Global” \equiv includes all five main categories of data.
- Three* groups with **NLO** global fits, but only *one* at **NNLO**.
- GJR08** *almost* global but restrictive “dynamical” parameterisation.
- NNPDF2.0 (ZM-VFNS)** \rightarrow **NNPDF2.1 (GM-VFNS)**, now allowing meaningful comparison to other NLO global fits.
(Previous **NNPDF2.0** $\sigma_{W,Z}$ lower than all other groups.)
- ABKM09** and **GJR08/JR09** use **FFNS** for structure functions.

Ratio of NLO quark–antiquark luminosity functions

$$\frac{\partial \mathcal{L}_{\Sigma_q(q\bar{q})}}{\partial \hat{s}} = \frac{1}{s} \int_{\tau}^1 \frac{dx}{x} \sum_{q=d,u,s,c,b} [f_q(x, \hat{s}) f_{\bar{q}}(\tau/x, \hat{s}) + (q \leftrightarrow \bar{q})], \quad \tau \equiv \frac{\hat{s}}{s}$$



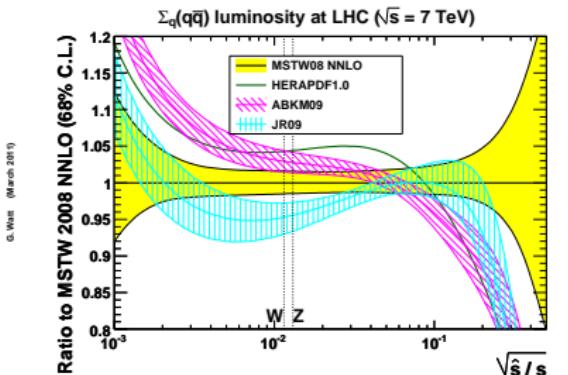
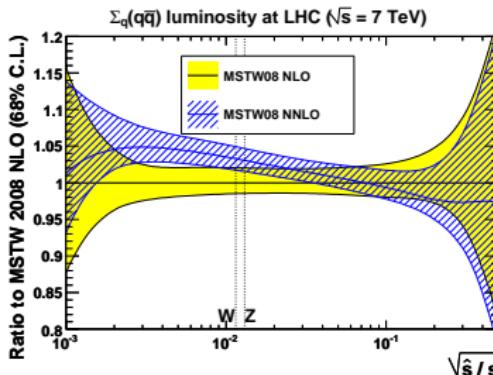
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- Relevant values of $\sqrt{\hat{s}} = M_{W,Z}$ are indicated: good agreement for global fits (*left*), but more variation for other sets (*right*).

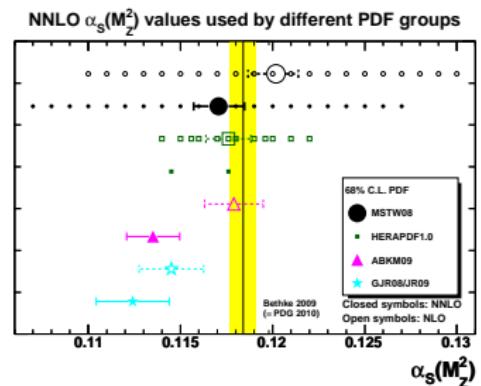
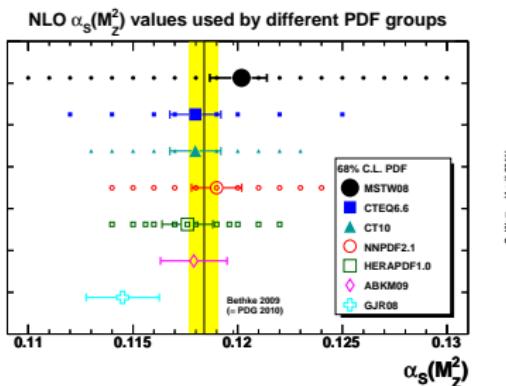
Ratio of NNLO quark–antiquark luminosity functions

$$\frac{\partial \mathcal{L}_{\Sigma_q(q\bar{q})}}{\partial \hat{s}} = \frac{1}{s} \int_{\tau}^1 \frac{dx}{x} \sum_{q=d,u,s,c,b} [f_q(x, \hat{s}) f_{\bar{q}}(\tau/x, \hat{s}) + (q \leftrightarrow \bar{q})], \quad \tau \equiv \frac{\hat{s}}{s}$$



- **Left plot:** compare MSTW NLO and NNLO luminosities.
- **Right plot:** NNLO trend between groups similar to NLO.

Values of $\alpha_s(M_Z^2)$ used by different fitting groups



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- $\alpha_s(M_Z^2)$ for MSTW08, ABKM09 and GJR08/JR09 fitted.
- $\alpha_s(M_Z^2)$ for other groups applied as an external constraint.
- Smaller symbols indicate alternative $\alpha_s(M_Z^2)$ values provided.
- Fitted NLO $\alpha_s(M_Z^2)$ always larger than NNLO $\alpha_s(M_Z^2)$: attempt to mimic missing higher-order corrections.
- Plot cross sections versus $\alpha_s(M_Z^2)$ to show dependence (more important for $t\bar{t}$ and $gg \rightarrow H$ than W/Z production).

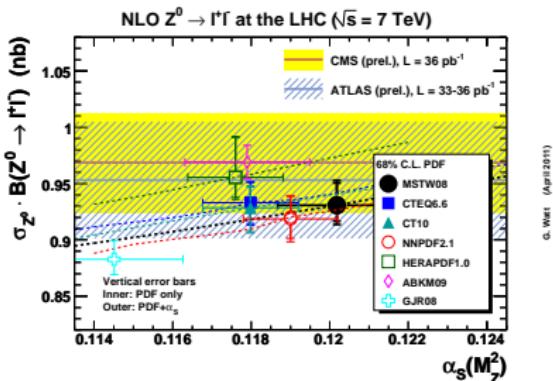
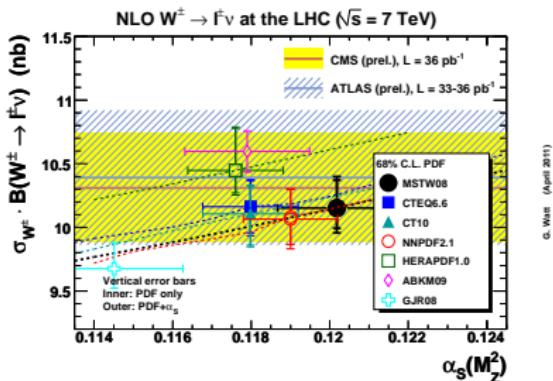
Settings for NLO/NNLO W and Z total cross sections

- Aim to isolate PDF (and α_S) dependence.
⇒ Use **same** code for all PDF sets with common settings.
- “PDF+ α_S ” uncertainties (at 68% and 90% C.L.) computed using recommended prescription of each fitting group.
- No attempt made to evaluate other theoretical uncertainties.
Single scale choice, $\mu_R = \mu_F = M_W, M_Z$. (Scale uncertainties less than 1% at NNLO.) No electroweak corrections included.
- Treatment of heavy quarks in 5-flavour ZM-VFNS.
- Use PDG 2008 electroweak parameters, no virtual photon (γ^*).
- On-shell W and Z production times leptonic branching ratios.
- Apply correction factors to ATLAS and CMS data calculated using VRAP at NNLO with MSTW08 PDFs (but same at NLO).

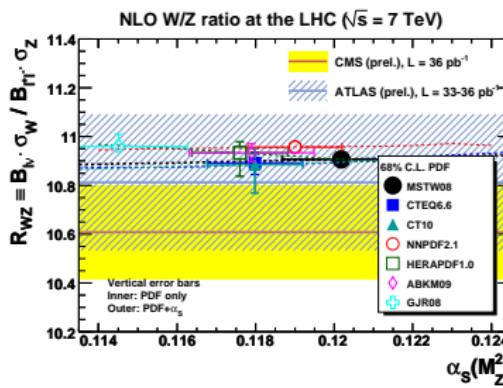
ATLAS: $\sigma(Z/\gamma^*, 66 < M_{\ell\ell} < 116 \text{ GeV}) / \sigma(\text{Z-only}, M_{\ell\ell} = M_Z) = 0.991$

CMS: $\sigma(Z/\gamma^*, 60 < M_{\ell\ell} < 120 \text{ GeV}) / \sigma(\text{Z-only}, M_{\ell\ell} = M_Z) = 1.006$

NLO W^\pm and Z^0 total cross sections versus $\alpha_S(M_Z^2)$

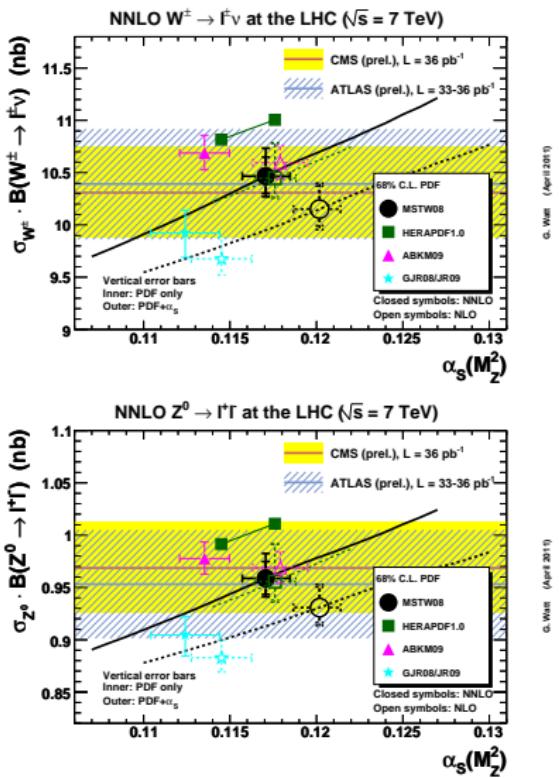


- Global fits in good agreement for σ_{W^\pm} and σ_{Z^0} (left plots).
- Small uncertainties in predictions for W/Z ratio:

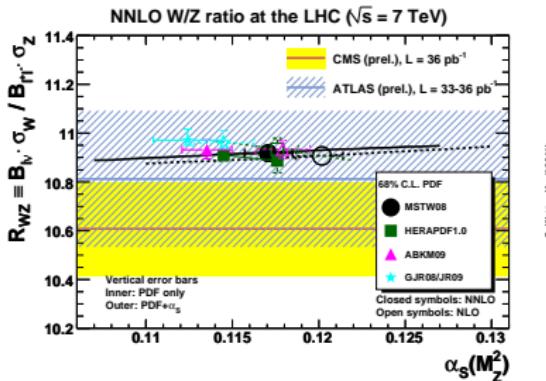


- **Preliminary LHC data**
[ATLAS-CONF-2011-041,
CMS PAS EWK-10-005].

NNLO W^\pm and Z^0 total cross sections versus $\alpha_S(M_Z^2)$

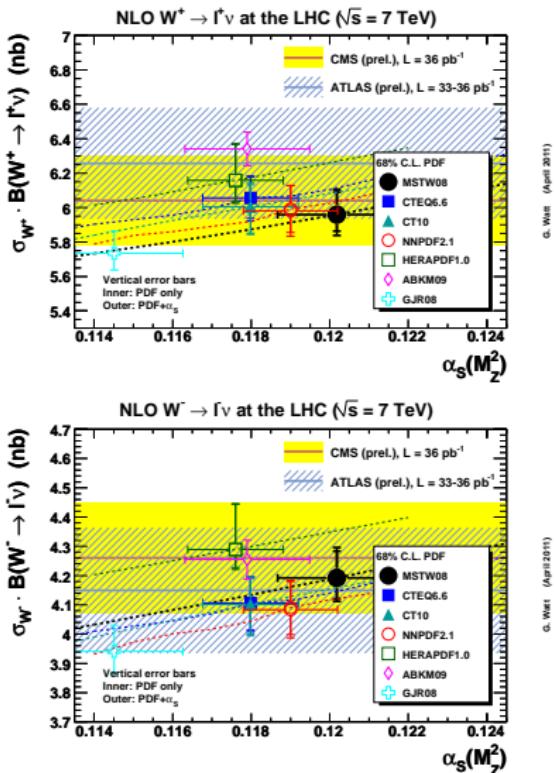


- NNLO corrections reduced by taking different $\alpha_S(M_Z^2)$ values at different orders.
- W/Z ratio insensitive to NNLO corrections (and α_S):

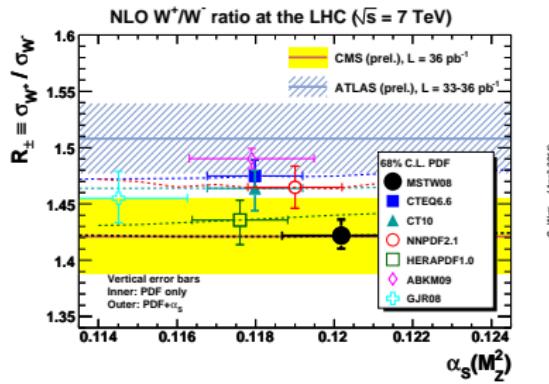


- Luminosity uncertainty 3–4%, comparable with PDF spread.

NLO W^+ and W^- total cross sections versus $\alpha_S(M_Z^2)$

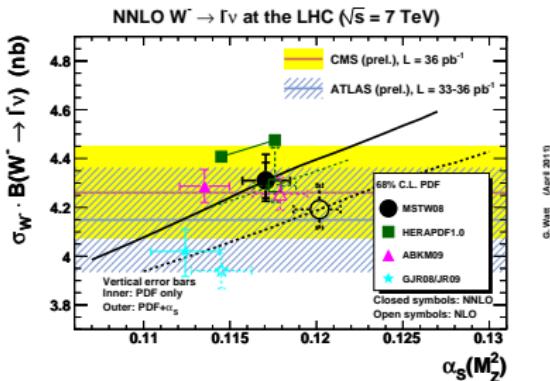
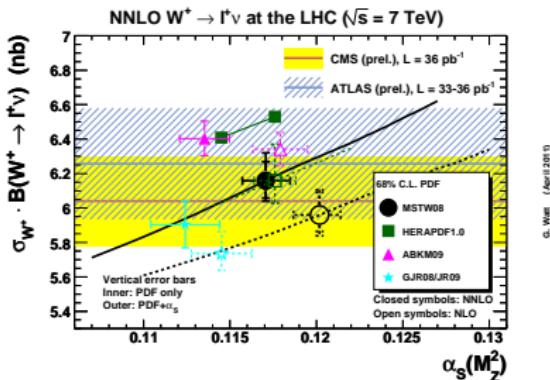


- Slightly more spread in separate σ_{W^+} and σ_{W^-} .
- Reflected in W^+/W^- ratio (sensitive to u/d ratio):

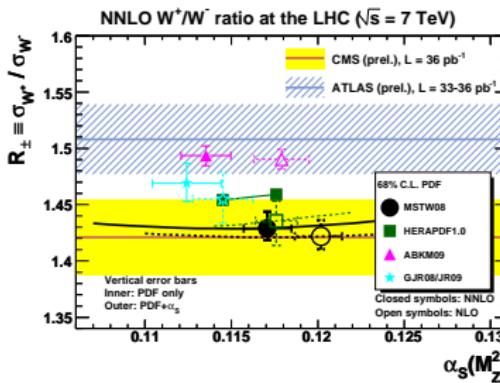


- ATLAS W^+/W^- ratio derived from ATLAS ellipse [ATLAS-CONF-2011-041].

NNLO W^+ and W^- total cross sections versus $\alpha_s(M_Z^2)$



- W^+/W^- ratio insensitive to NNLO corrections (and α_s):

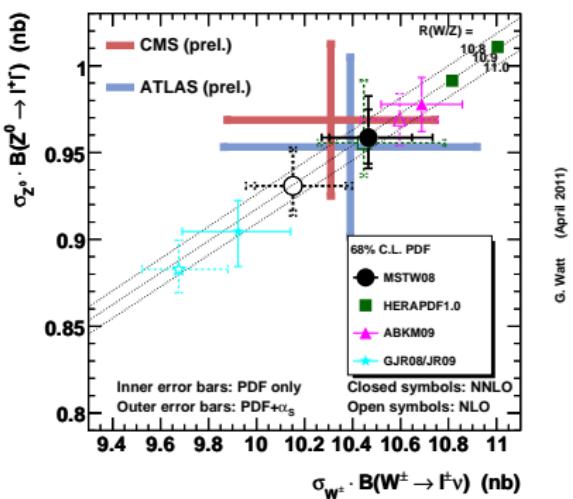


- Apparent discrepancy between CMS and ATLAS for ratio.
- CMS ratio favours **MSTW08**, ATLAS favours **ABKM09** (?).

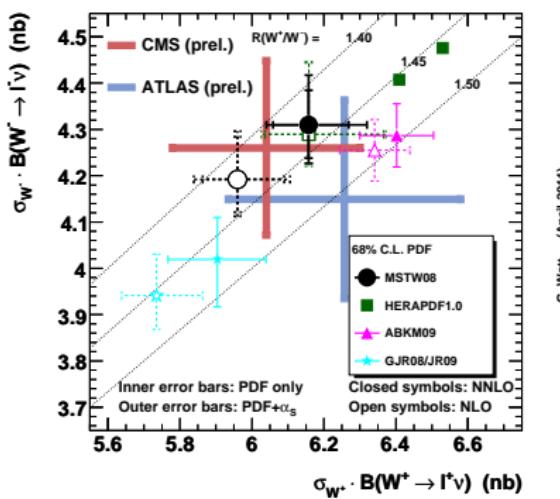
NNLO W^\pm vs. Z^0 and W^+ vs. W^- total cross sections

- Consolidate two cross section measurements (and their ratio).

NNLO W and Z cross sections at the LHC ($\sqrt{s} = 7$ TeV)



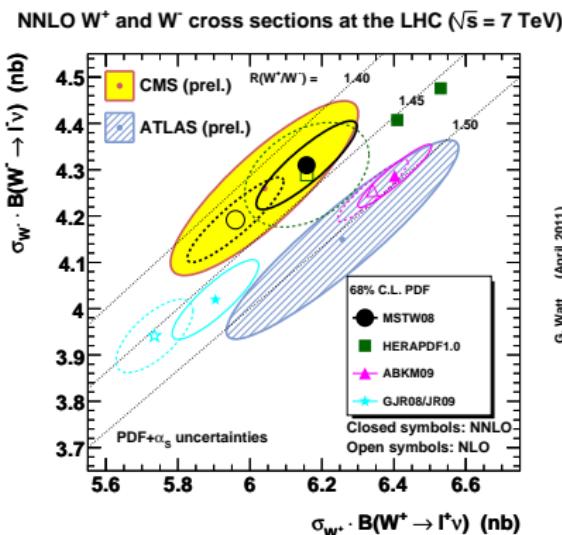
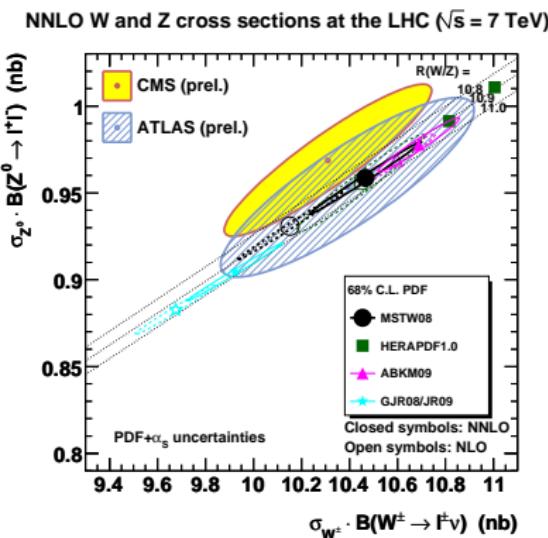
NNLO W^+ and W^- cross sections at the LHC ($\sqrt{s} = 7$ TeV)



- Know correlation of both data and theory (from eigenvector PDFs).

NNLO W^\pm vs. Z^0 and W^+ vs. W^- total cross sections

- Correlation of ellipse \Leftrightarrow uncertainty in ratio of cross sections.



- Apparent discrepancy between CMS and ATLAS for W^+/W^- . CMS ratio favours **MSTW08**, ATLAS favours **ABKM09** (?)

Acceptance for W^+/W^- total cross section ratio

- CMS [arXiv:1012.2466, CMS PAS EWK-10-005] use POWHEG (with CTEQ6.6/CT10, MSTW08NLO, NNPDF2.0), check with FEWZ.

$$\Rightarrow \frac{\sigma_{W^+}^{\text{tot}}}{\sigma_{W^-}^{\text{tot}}} = \begin{cases} 1.418 \pm 0.008(\text{stat.}) \pm 0.022(\text{syst.}) \pm 0.029(\text{th.}) & (e) \\ 1.423 \pm 0.008(\text{stat.}) \pm 0.019(\text{syst.}) \pm 0.031(\text{th.}) & (\mu) \\ 1.421 \pm 0.006(\text{stat.}) \pm 0.014(\text{syst.}) \pm 0.030(\text{th.}) & (e + \mu) \end{cases}$$

- ATLAS [arXiv:1010.2130, ATLAS-CONF-2011-041] use PYTHIA (with MRSTLO*) $\Rightarrow \sigma_{W^+}^{\text{tot}}/\sigma_{W^-}^{\text{tot}} = 1.51 \pm 0.03 (e + \mu)$ [from ATLAS ellipse].

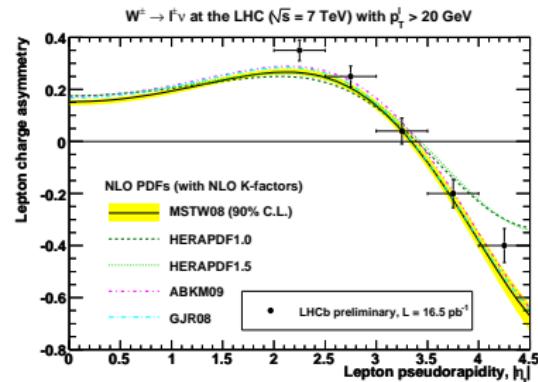
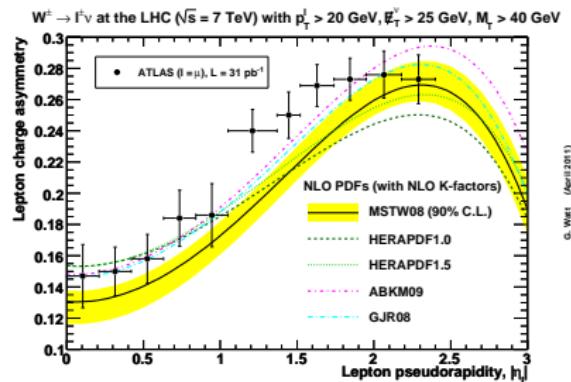
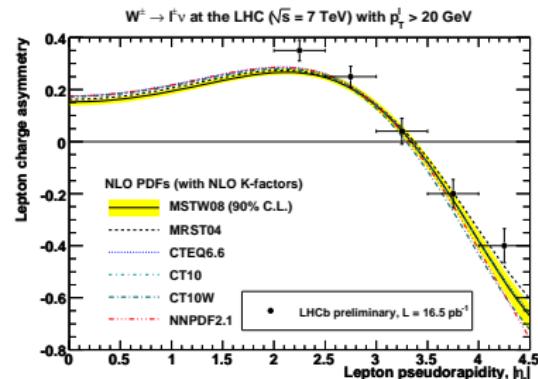
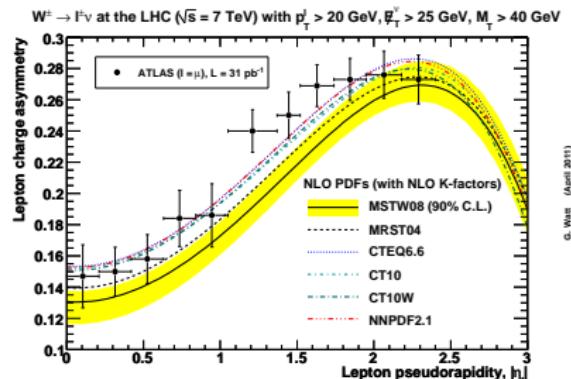
	A_{W^+}/A_{W^-}		$\sigma_{W^+}^{\text{tot}}/\sigma_{W^-}^{\text{tot}}$	
	e	μ	e	μ
MC+PDF				
PYTHIA+MRSTLO*	1.02	1.02	1.50	1.51
PYTHIA+CTEQ6.6	1.05	1.05	1.46	1.47
PYTHIA+HERAPDF1.0	1.03	1.04	1.48	1.49
MC@NLO+HERAPDF1.0	1.05	1.05	1.46	1.47
MC@NLO+CTEQ6.6	1.06	1.06	1.45	1.46

$$\frac{\sigma_{W^+}^{\text{tot}}}{\sigma_{W^-}^{\text{tot}}} = \frac{\sigma_{W^+}^{\text{fid}}}{\sigma_{W^-}^{\text{fid}}} \cdot \frac{A_{W^-}}{A_{W^+}}$$

Alternative acceptance calculations move ATLAS $\sigma_{W^+}^{\text{tot}}/\sigma_{W^-}^{\text{tot}}$ much closer to CMS.

- Precision requires better acceptance calculations and/or data to theory comparisons at level of fiducial cross section.

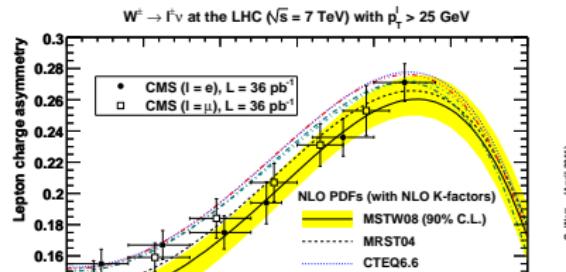
$W^\pm \rightarrow \ell^\pm \nu$ charge asymmetry from ATLAS and LHCb



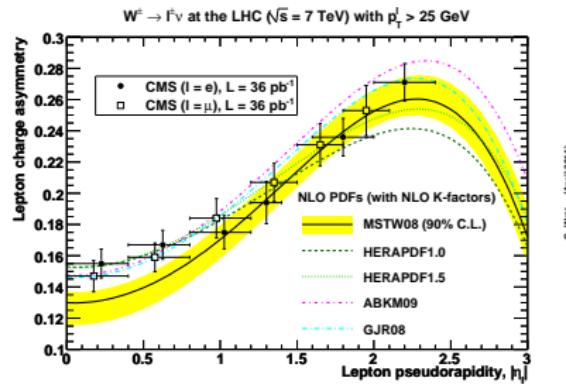
Data: ATLAS [arXiv:1103.2929]

Data: LHCb preliminary

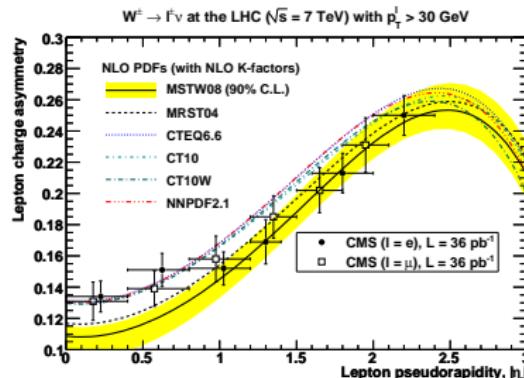
$W^\pm \rightarrow \ell^\pm \nu$ charge asymmetry from CMS [arXiv:1103.3470]



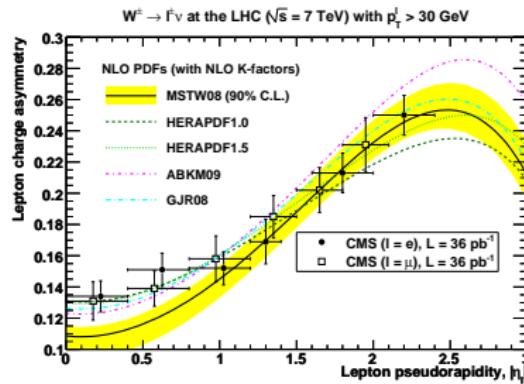
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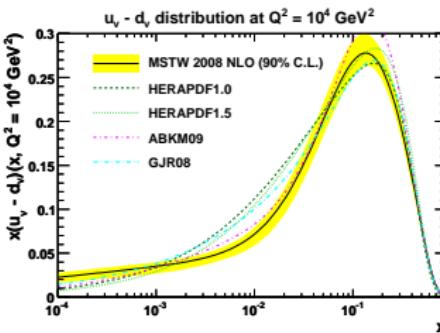
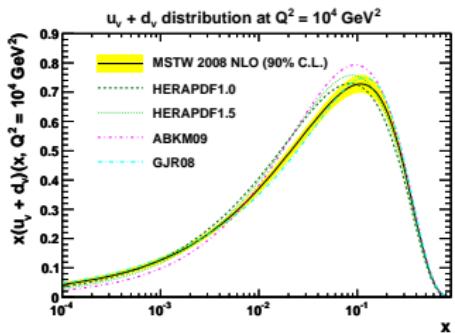
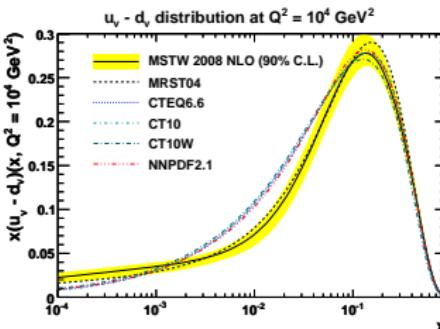
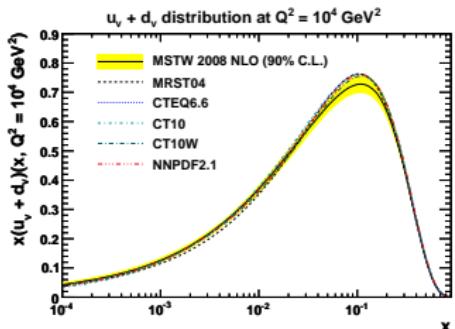
Data: CMS for $p_T^\ell > 25$ GeV

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Data: CMS for $p_T^\ell > 30$ GeV

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Comparison of $u_v \pm d_v$ for different NLO PDFs



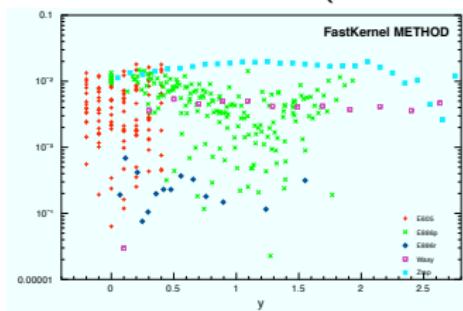
- MSTW08 has input $xu_v \propto x^{0.29 \pm 0.02}$ and $xd_v \propto x^{0.97 \pm 0.11}$.
Many other groups assume equal powers \Rightarrow parameterisation bias.
(NNPDF: restricted range of small- x preprocessing exponents.)

Methods for including hadron collider data in PDF fits

Problem: need fast NLO/NNLO calculation to allow PDF fitting.

Solutions:

- ① Avoid explicit PDF refitting. **Reweighting** existing Monte Carlo replica PDF sets (\rightarrow M. Ubiali) or Hessian eigenvector PDF sets (\rightarrow R. McNulty). Useful method, but short-term solution.
- ② Grid **interpolation** methods: FASTNLO (NLOJET++), APPLGRID (NLOJET++, MCFM), FASTKERNEL (DY w/o ℓ cuts).



Methods used by three global fit groups:

	MSTW	CTEQ	NNPDF
Tevatron jets	FASTNLO	K -factors	FASTNLO
Tevatron W, Z	K -factors	K -factors	FASTKERNEL
Fixed-target DY	K -factors	K -factors	FASTKERNEL

- ③ Parameterised **K -factors** calculated for exact kinematic cuts.
More traditional method, but often (unjustly?) criticised.

Practical implementation of K -factors in PDF fits

- **Example:** Z rapidity distribution in PDF fit calculated as

$$\frac{d\sigma^{\text{NNLO}}}{dy} = \frac{d\sigma^{\text{LO}}}{dy} K(y), \quad K(y) \equiv \left. \frac{d\sigma^{\text{NNLO}}/dy}{d\sigma^{\text{LO}}/dy} \right|_{\text{fixed NNLO PDF}},$$

where $K(y)$ calculated beforehand for a fixed NNLO PDF (and α_S) choice in **both** numerator and denominator.

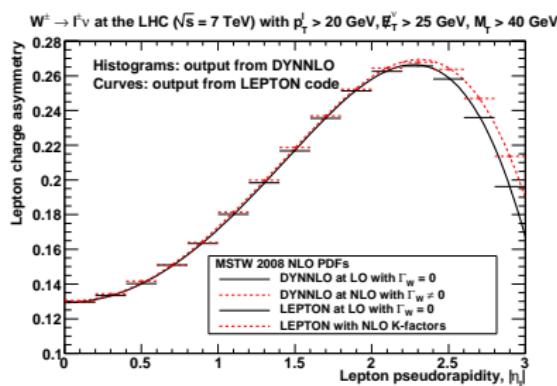
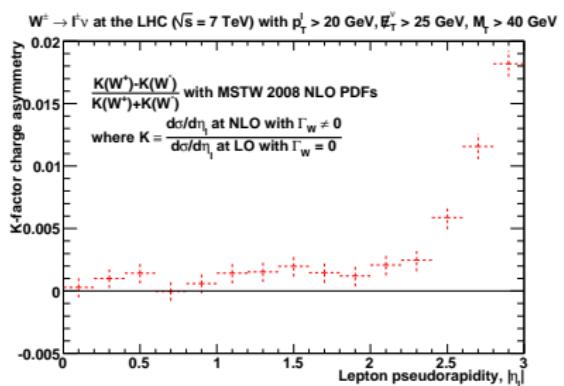
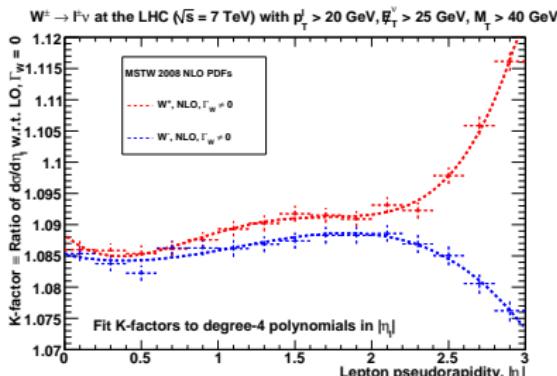
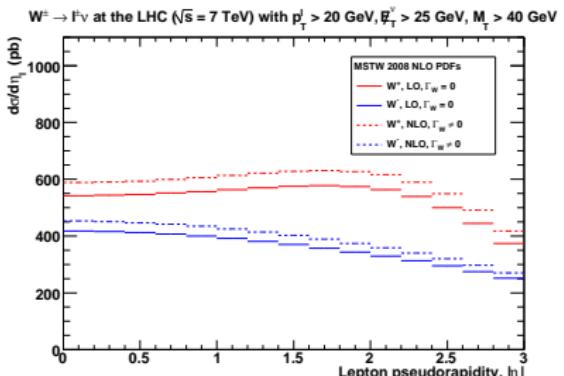
- Approximation made is that $K(y)$ is independent of PDF choice: can iterate or use a different PDF choice to check this assumption.
- Possible to go further and isolate α_S dependence from K -factor:

$$K(y) = 1 + \alpha_S D(y) + \alpha_S^2 E(y),$$

where coefficients $D(y)$ and $E(y)$ are calculated for a fixed PDF choice. Method used for Drell–Yan data in MSTW08 fit.

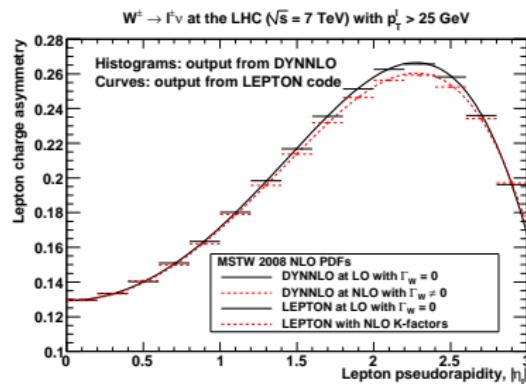
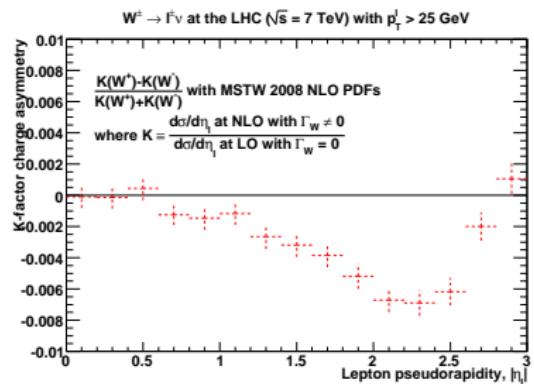
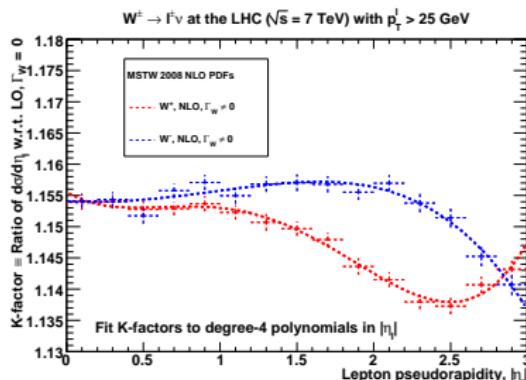
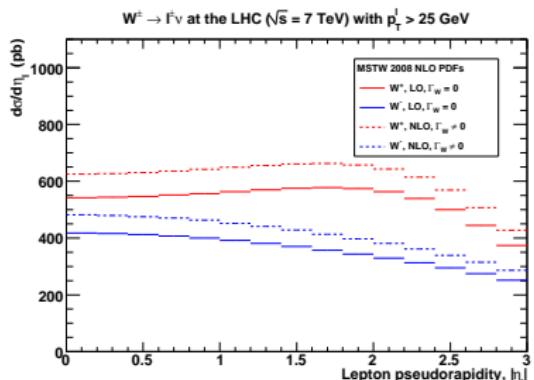
- Illustrate method by looking at K -factors for LHC W/Z data.

NLO K -factors for ATLAS cuts [arXiv:1103.2929]



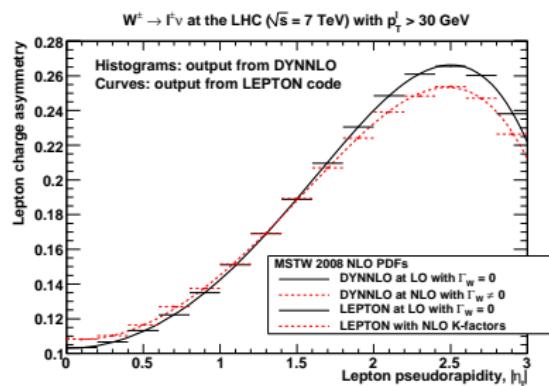
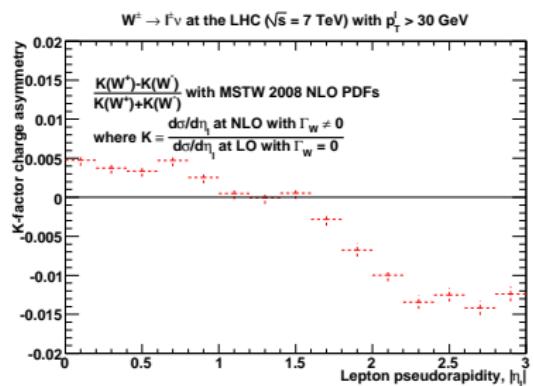
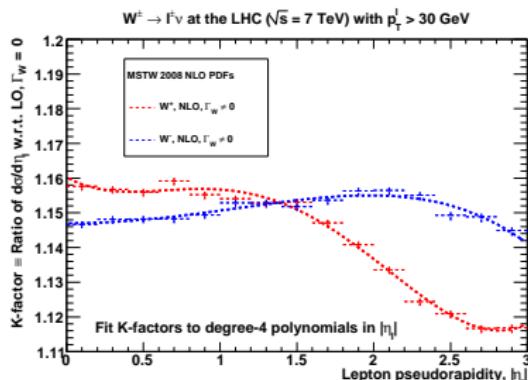
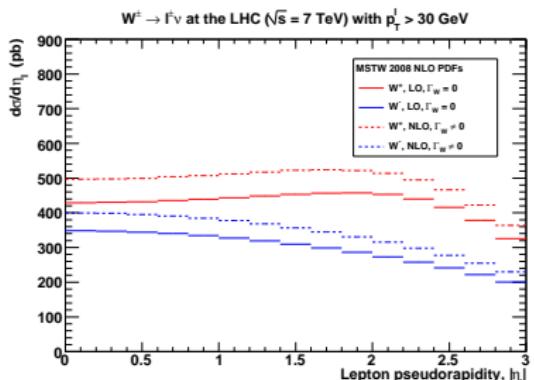
- PDF dependence of K -factor charge asymmetry should be negligible.

NLO K -factors for CMS cuts ($p_T^l > 25$ GeV) [arXiv:1103.3470]



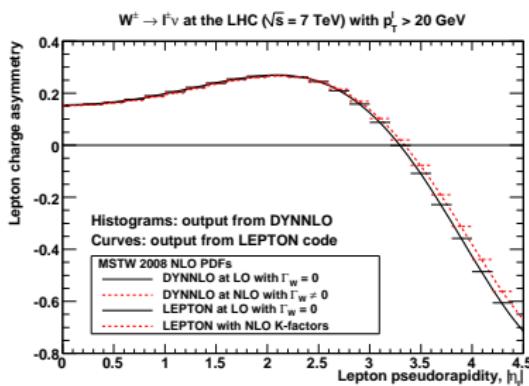
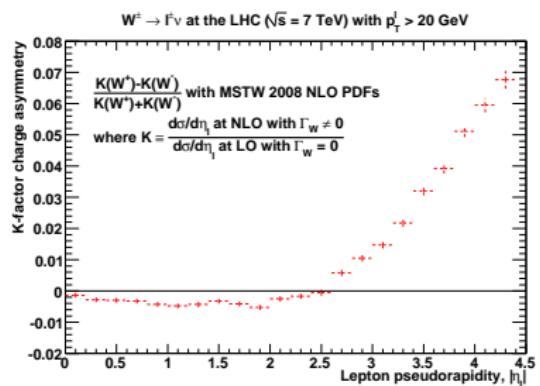
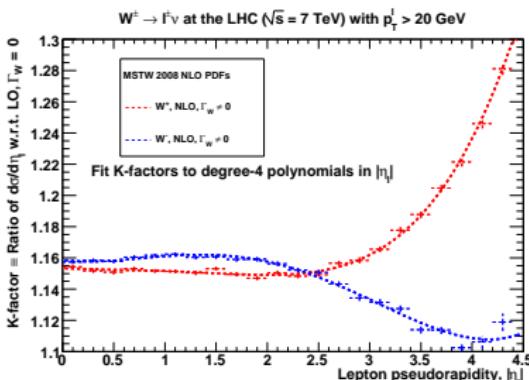
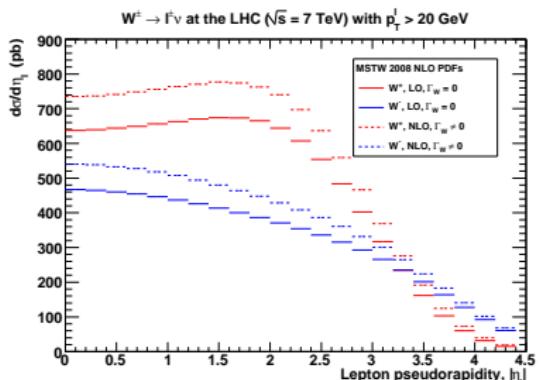
- CMS cuts slightly different from ATLAS, but equal at LO with $\Gamma_W = 0$.

NLO K -factors for CMS cuts ($p_T^\ell > 30$ GeV) [arXiv:1103.3470]



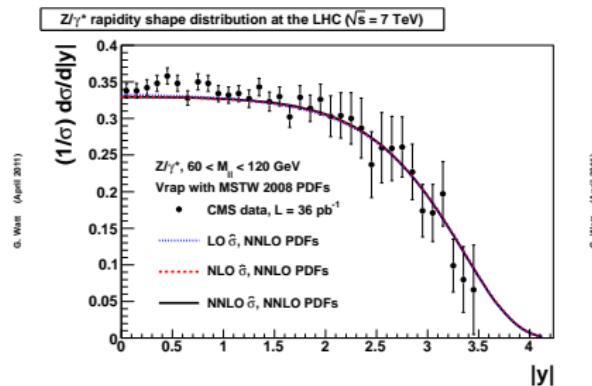
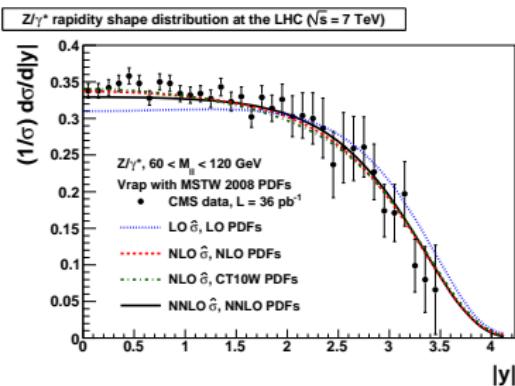
- K -factor charge asymmetry larger for $p_T^\ell > 30$ GeV than $p_T^\ell > 25$ GeV.

NLO K -factors for LHCb cuts [LHCb-CONF-2011-012]



- K -factor charge asymmetry still small at large $|\eta_\ell|$ relevant for LHCb.

Z/γ^* rapidity distribution at the LHC [CMS PAS EWK-10-010]



- **Left plot:** change PDF with order of $\hat{\sigma}$ calculation. NLO and NNLO clearly favoured over LO. CT10W close to MSTW08NLO.
- **Right plot:** same MSTW08NNLO PDF with varying $\hat{\sigma}$ order.
 \Rightarrow PDF dependence of K -factor should be negligible.
- Could quantify accuracy by propagating PDF uncertainties:

$$\frac{d\sigma_i^{\text{NNLO}}}{dy} = \frac{d\sigma_0^{\text{LO}}}{dy} K_i(y), \quad K_i(y) \equiv \frac{d\sigma_i^{\text{NNLO}}/dy}{d\sigma_i^{\text{LO}}/dy},$$

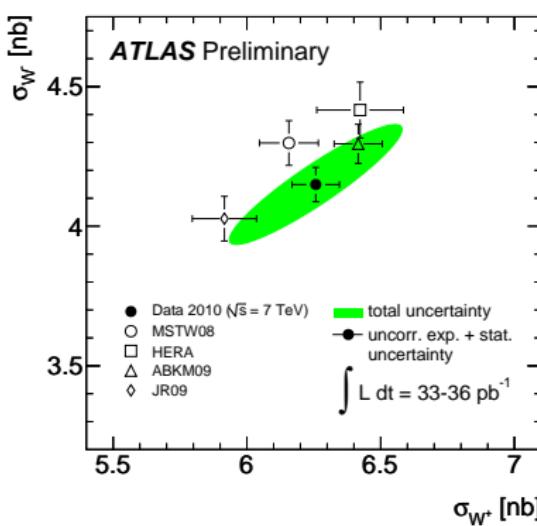
for eigenvector NNLO PDF set “ i ”, where “ 0 ” is the central set.

Summary

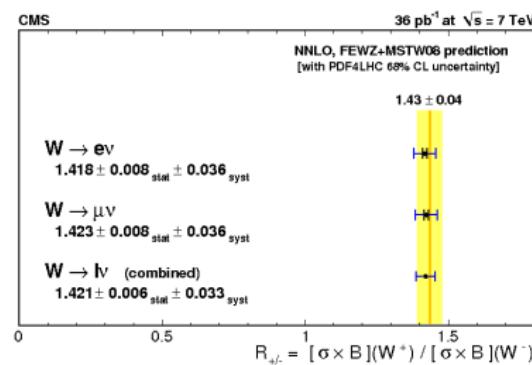
- Apparent discrepancy between ATLAS and CMS W^+/W^- total cross section ratio due to **inadequate acceptance calculations**. Data precision requires proper acceptance corrections and/or comparison of data and theory for fiducial cross section.
- LHC $W^\pm \rightarrow \ell^\pm \nu$ charge asymmetry data an important input to future fits (but still outstanding issues to be resolved concerning Tevatron data and nuclear effects in deuteron structure functions [**MSTW, arXiv:1006.2753**]).
- **K -factor methods** should be sufficiently accurate for inclusion in PDF fits of LHC data on $W^\pm \rightarrow \ell^\pm \nu$ charge asymmetry and Z/γ^* rapidity shape distribution (but not jets etc.).

ATLAS and CMS W^+/W^- total cross section ratios

[ATLAS-CONF-2011-041]



[CMS PAS EWK-10-005]



- PDF4LHC recipe **inappropriate** for PDF-sensitive measurement.

- ATLAS ellipse $\Rightarrow \sigma_{W^+}^{\text{tot}} / \sigma_{W^-}^{\text{tot}} = 1.51 \pm 0.03$ (total uncertainty).
- CMS $\sigma_{W^+}^{\text{tot}} / \sigma_{W^-}^{\text{tot}} = 1.421 \pm 0.034 \Rightarrow$ correlation for ellipse.

What is α_S from only DIS in the MSTW08 NNLO fit?

[Studies prompted by question from G. Altarelli, December 2010]

- Global fit: $\alpha_S(M_Z^2) = 0.1171 \pm 0.0014$ [[arXiv:0905.3531](#)].
- DIS-only fit gives $\alpha_S(M_Z^2) = 0.1104$ (BCDMS-dominated)¹, but **input $xg < 0$ for $x > 0.4$** due to lack of data constraint.
 $\Rightarrow F_2^{\text{charm}} < 0$ and $\chi^2/N_{\text{pts.}} \sim 10$ for Tevatron jets.
- DIS-only fit fixing high- x gluon parameters gives $\alpha_S(M_Z^2) = 0.1172$.
- DIS-only fit without BCDMS gives $\alpha_S(M_Z^2) = 0.1193$.
- Global fit without BCDMS gives $\alpha_S(M_Z^2) = 0.1181$.
- **Conclusion:** Tevatron jet data vital to pin down **high- x gluon**, giving smaller **low- x gluon** and therefore larger α_S in the global fit compared to a DIS-only fit, at the expense of some deterioration in the fit quality of the BCDMS data.

¹Some analyses cut $y > 0.3$ on BCDMS data to reduce energy scale uncertainty of scattered muon: increases $\alpha_S(M_Z^2)$ by 0.004 in BCDMS-only fit.

Non-singlet QCD analysis of DIS data [BBG06, hep-ph/0607200]

Order	$\alpha_S(M_Z^2)$ (expt.)
NLO	$0.1148^{+0.0019}_{-0.0019}$
NNLO	$0.1134^{+0.0019}_{-0.0021}$
NNNLO	$0.1141^{+0.0020}_{-0.0022}$

- Fit F_2^P and F_2^d for $x > 0.3$ (neglect singlet contribution), and F_2^{NS} .
- But singlet makes up about 10% (2%) of F_2^P at $x = 0.3$ ($x = 0.5$).

- **Exercise:** perform MSTW08 NNLO DIS-only fit to F_2^P and F_2^d for $x > 0.3$ (282 points, 160 from BCDMS).
 $\Rightarrow \alpha_S(M_Z^2) = 0.1103$ (0.1130) without (with) singlet included.
 (Lower than BBG06 due to lack of $y > 0.3$ cut on BCDMS.)
- **Conclusion:** low value of $\alpha_S(M_Z^2)$ found by BBG06 due to (i) dominance of BCDMS data and (ii) neglect of singlet.
- Closest possible to reliable extraction of $\alpha_S(M_Z^2)$ from DIS is MSTW08 NNLO combined analysis of DIS, DY and jet data:

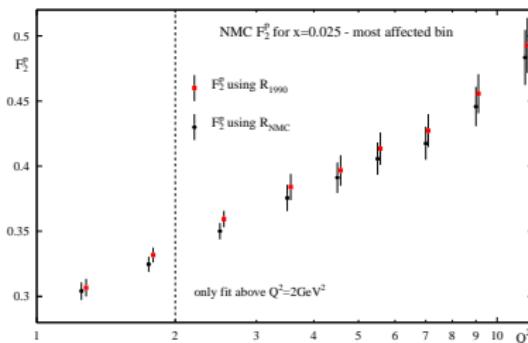
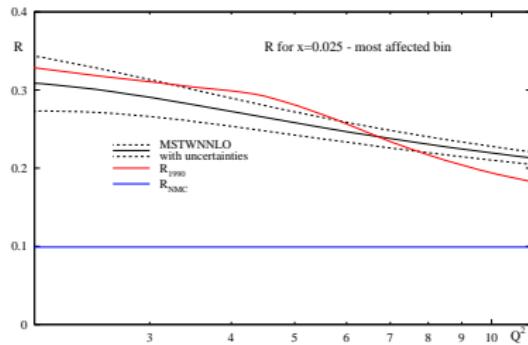
$$\alpha_S(M_Z^2) = 0.1171 \pm 0.0014 \text{ (68\% C.L.)} \quad \pm 0.0034 \text{ (90\% C.L.)}$$

Treatment of F_L correction for NMC data [Studies by R. Thorne]

- Recent claim that bulk of **MSTW/ABKM** difference explained by F_L for NMC data [Alekhin, Blümlein, Moch, arXiv:1101.5261].
- ABKM** fit NMC cross sections, **MSTW** fit NMC F_2 corrected for $R = \sigma_L/\sigma_T \simeq F_L/(F_2 - F_L)$, where [NMC, hep-ph/9610231]:

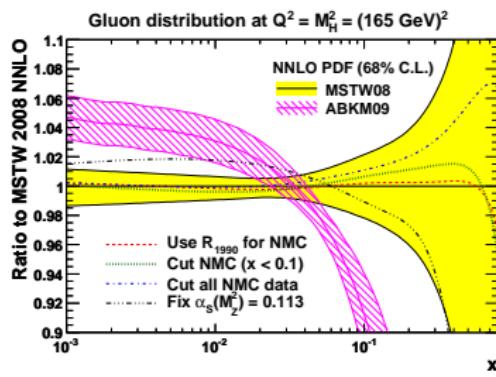
$$R(x, Q^2) = \begin{cases} R_{\text{NMC}}(x) & \text{if } x < 0.12 \\ R_{1990}(x, Q^2) & \text{if } x > 0.12 \end{cases}.$$

- Alternative NMC F_2 data using $R = R_{1990}$ ($\forall x$) close to R_{MSTW} .



Effect of NMC F_L treatment on Higgs cross sections

NNLO PDF	$\alpha_S(M_Z^2)$	σ_H at Tevatron	σ_H at 7 TeV LHC
MSTW08	0.1171	0.342 pb	7.91 pb
Use R_{1990} for NMC	0.1167	-0.7%	-0.9%
Cut NMC ($x < 0.1$)	0.1162	-1.2%	-2.1%
Cut all NMC data	0.1158	-0.7%	-2.1%
Fix $\alpha_S(M_Z^2)$	0.1130	-11%	-7.6%
ABKM09	0.1135	-26%	-11%



- Greater sensitivity found by ABM [[arXiv:1101.5261](#)] perhaps due to inclusion of higher-twist and/or lack of Tevatron jets.

- Higgs cross section insensitive to treatment of NMC F_L .
- Similar stability found by NNPDF [[arXiv:1102.3182](#)] (but at NLO with fixed α_S).
- Gluon and σ_H still far from ABKM with $\alpha_S(M_Z^2) = 0.113$.

Description of CDF II inclusive jet (k_T) data [hep-ex/0701051]

- Values of $\chi^2/N_{\text{pts.}}$ with (without) accounting for correlations:

NLO PDF (with NLO $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	0.75 (0.30)	0.68 (0.28)	0.91 (0.84)
CTEQ6.6	1.25 (0.14)	1.66 (0.20)	2.38 (0.84)
CT10	1.03 (0.13)	1.20 (0.19)	1.81 (0.84)
NNPDF2.1	0.74 (0.29)	0.82 (0.25)	1.23 (0.69)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.43 (0.39)	3.26 (0.66)	4.03 (1.67)
ABKM09	1.62 (0.52)	2.21 (0.85)	3.26 (2.10)
GJR08	1.36 (0.23)	0.94 (0.13)	0.79 (0.36)

NNLO PDF (with NLO+2-loop $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	1.39 (0.42)	0.69 (0.44)	0.97 (0.48)
HERAPDF1.0 ($\alpha_S = 0.1145$)	2.64 (0.36)	2.15 (0.36)	2.20 (0.46)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.24 (0.35)	1.17 (0.32)	1.23 (0.31)
ABKM09	2.55 (0.82)	2.76 (0.89)	3.41 (1.17)
JR09	0.75 (0.37)	1.26 (0.41)	2.21 (0.49)

- $N_{\text{pts.}} = 76$, $N_{\text{corr.}} = 17$. 90% C.L. region for **MSTW08** ($\mu = p_T$) given by $\chi^2/N_{\text{pts.}} < 0.83$ (NLO) or $\chi^2/N_{\text{pts.}} < 0.85$ (NNLO).

Description of CDF II inclusive jet (cone) data [arXiv:0807.2204]

- Values of $\chi^2/N_{\text{pts.}}$ with (without) accounting for correlations:

NLO PDF (with NLO $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	1.52 (0.61)	1.40 (0.27)	1.16 (0.73)
CTEQ6.6	1.93 (0.41)	1.98 (0.21)	1.78 (0.78)
CT10	1.75 (0.38)	1.69 (0.19)	1.50 (0.76)
NNPDF2.1	1.69 (0.60)	1.56 (0.25)	1.44 (0.60)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.61 (0.23)	2.73 (0.49)	2.53 (1.58)
ABKM09	1.56 (0.26)	1.68 (0.65)	1.69 (2.01)
GJR08	2.11 (0.71)	1.75 (0.24)	1.52 (0.31)

NNLO PDF (with NLO+2-loop $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	1.67 (0.62)	1.39 (0.43)	1.62 (0.37)
HERAPDF1.0 ($\alpha_S = 0.1145$)	2.20 (0.25)	2.06 (0.27)	2.19 (0.40)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.08 (0.55)	1.76 (0.33)	1.99 (0.23)
ABKM09	1.70 (0.50)	1.94 (0.71)	2.26 (1.12)
JR09	1.57 (0.41)	2.05 (0.36)	2.82 (0.39)

- $N_{\text{pts.}} = 72$, $N_{\text{corr.}} = 25$. 90% C.L. region for **MSTW08** ($\mu = p_T$) given by $\chi^2/N_{\text{pts.}} < 1.73$ (NLO) or $\chi^2/N_{\text{pts.}} < 1.71$ (NNLO).

Description of DØ II inclusive jet (cone) data [arXiv:0802.2400]

- Values of $\chi^2/N_{\text{pts.}}$ with (without) accounting for correlations:

NLO PDF (with NLO $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	1.45 (0.89)	1.08 (0.20)	1.05 (1.22)
CTEQ6.6	1.62 (1.15)	1.56 (0.59)	1.61 (1.35)
CT10	1.39 (0.88)	1.26 (0.37)	1.32 (1.29)
NNPDF2.1	1.41 (0.87)	1.29 (0.20)	1.22 (0.96)
HERAPDF1.0 ($\alpha_S = 0.1145$)	1.73 (0.27)	1.84 (0.74)	1.83 (2.79)
ABKM09	1.39 (0.35)	1.43 (1.07)	1.63 (3.66)
GJR08	1.90 (1.46)	1.34 (0.45)	1.03 (0.51)

NNLO PDF (with NLO+2-loop $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	1.95 (0.90)	1.23 (0.44)	1.08 (0.35)
HERAPDF1.0 ($\alpha_S = 0.1145$)	2.11 (0.37)	1.68 (0.35)	1.41 (0.63)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.28 (0.95)	1.50 (0.40)	1.17 (0.21)
ABKM09	1.68 (0.79)	1.55 (1.21)	1.63 (2.04)
JR09	1.84 (0.47)	1.61 (0.36)	1.58 (0.50)

- $N_{\text{pts.}} = 110$, $N_{\text{corr.}} = 23$. 90% C.L. region for **MSTW08** ($\mu = p_T$) given by $\chi^2/N_{\text{pts.}} < 1.28$ (NLO) or $\chi^2/N_{\text{pts.}} < 1.46$ (NNLO).

Description of DØ II dijet invariant mass data [arXiv:1002.4594]

- Values of $\chi^2/N_{\text{pts.}}$ with (without) accounting for correlations:

NLO PDF (with NLO $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	3.15 (1.63)	2.25 (0.70)	1.56 (0.70)
CTEQ6.6	5.41 (2.22)	4.85 (1.79)	3.36 (1.52)
CT10	4.74 (1.87)	4.06 (1.32)	2.70 (1.21)
NNPDF2.1	2.67 (1.56)	1.93 (0.66)	1.47 (0.55)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.05 (0.38)	2.21 (0.77)	2.11 (2.28)
ABKM09	1.49 (0.33)	1.41 (0.80)	1.34 (2.78)
GJR08	10.7 (3.92)	7.91 (2.36)	5.30 (0.66)

NNLO PDF (with NLO $\hat{\sigma}$)	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	2.38 (0.63)	1.80 (0.33)	1.31 (1.24)
HERAPDF1.0 ($\alpha_S = 0.1145$)	2.61 (0.48)	2.55 (0.89)	2.40 (2.40)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.72 (0.83)	2.31 (0.50)	1.96 (1.08)
ABKM09	1.36 (0.98)	1.49 (1.93)	1.57 (4.53)
JR09	3.29 (0.42)	2.55 (0.24)	1.88 (1.26)

- $N_{\text{pts.}} = 71$, $N_{\text{corr.}} = 70$. Scale $\mu \propto p_T \equiv (p_{T1} + p_{T2})/2$.