

# CONFRONTING DIFFERENT MASS SCALES FOR DARK MATTER

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*«Would you be willing to give a talk on the possible different mass scales for DM? Tentative/illustrative title: "Confronting different scales for DM"...*

*I know we are asking something non-trivial, a kind of deep perspective talk.»*

# WHICH MASS SCALE?

Observations tell us that  
dark matter is cold, stable ( $\tau \gg \tau_U$ )<sup>\*</sup> and invisible

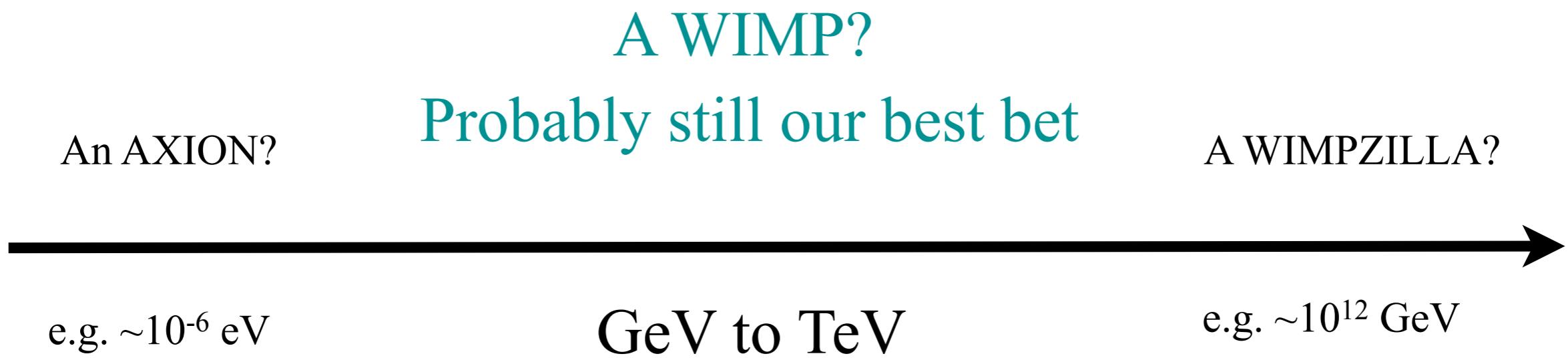
This leaves some freedom...

\* Rem:  $\tau_U \sim 10^{18}$  sec;  $\tau \gtrsim 10^{26}$  sec from constraints on flux of e+, anti-proton, gamma-ray,...

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## WHY WIMPs?

Classy theories (SUSY, Xtra DIM's, etc.) «predict» the existence of stable, weakly interacting massive particles.

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Stable, weakly interacting massive particles may be searched by:

Direct Detection, Indirect Detection and Collider Experiments

## WHY WIMPs?

This experimental program by itself largely motivates (at times much) less classy constructions.

Indeed, it is easy to implement DM.

e.g. add a singlet scalar field  $S$  with a parity

$$S \rightarrow -S$$

If  $\langle S \rangle = 0$  then  $S$  is a DM candidate.

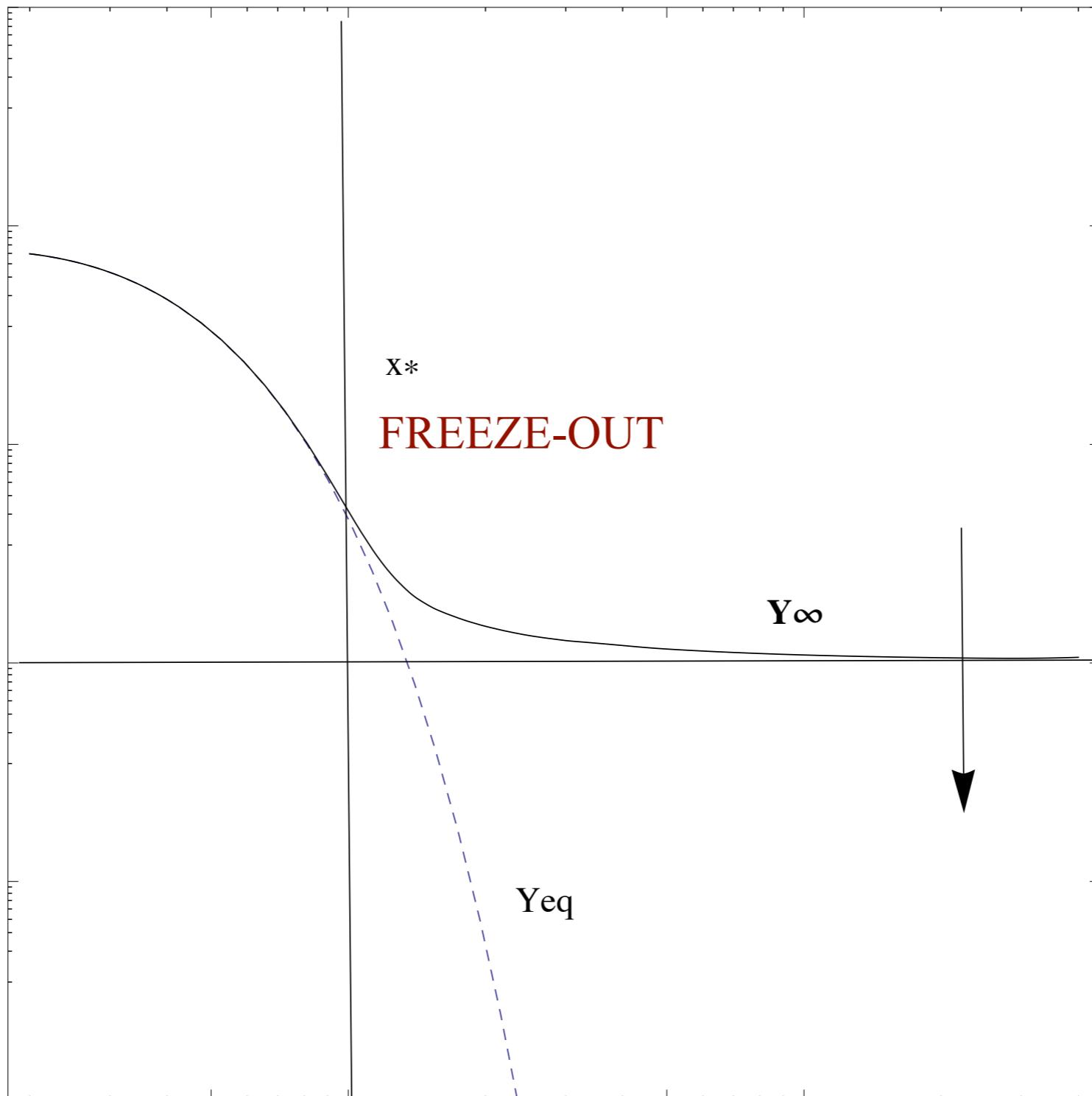
Silveira & Zee; Yndurain & Veltman; McDonald; Burgess, Pospelov & ter Veldhuis;...

THEN THERE IS THE WIMP MIRACLE



THERMAL  
ABUNDANCE

$$Y = \frac{n}{s}$$



$$x = m/T$$

RELIC  
ABUNDANCE

RELIC  
ABUNDANCE

$$\frac{\Omega_{dm}}{\Omega_b} \approx 0.2 x^* \left( \frac{\text{pbarn}}{\langle \sigma v \rangle} \right) \approx 5$$

FOR  $x^* = \mathcal{O}(25)$  NEED  $\langle \sigma v \rangle \sim 3 \cdot 10^{-26} \text{cm}^3 \cdot \text{s}^{-1}$

(FREEZE-OUT)

# SCALAR PHANTOMS

Vanda SILVEIRA<sup>1,2</sup> and A. ZEE

*Department of Physics, FM-15, University of Washington, Seattle, WA 98195, USA*

Received 17 June 1985

We show that, by a minimal modification of the standard  $SU(3) \times SU(2) \times U(1)$  theory, we can account for the dark matter of the universe. With a reasonable choice of an unknown coupling, the galactic mass scale emerges. We comment on the prospects for laboratory detection of the scalar particle involved and the possible production of anti-protons in cosmic rays.

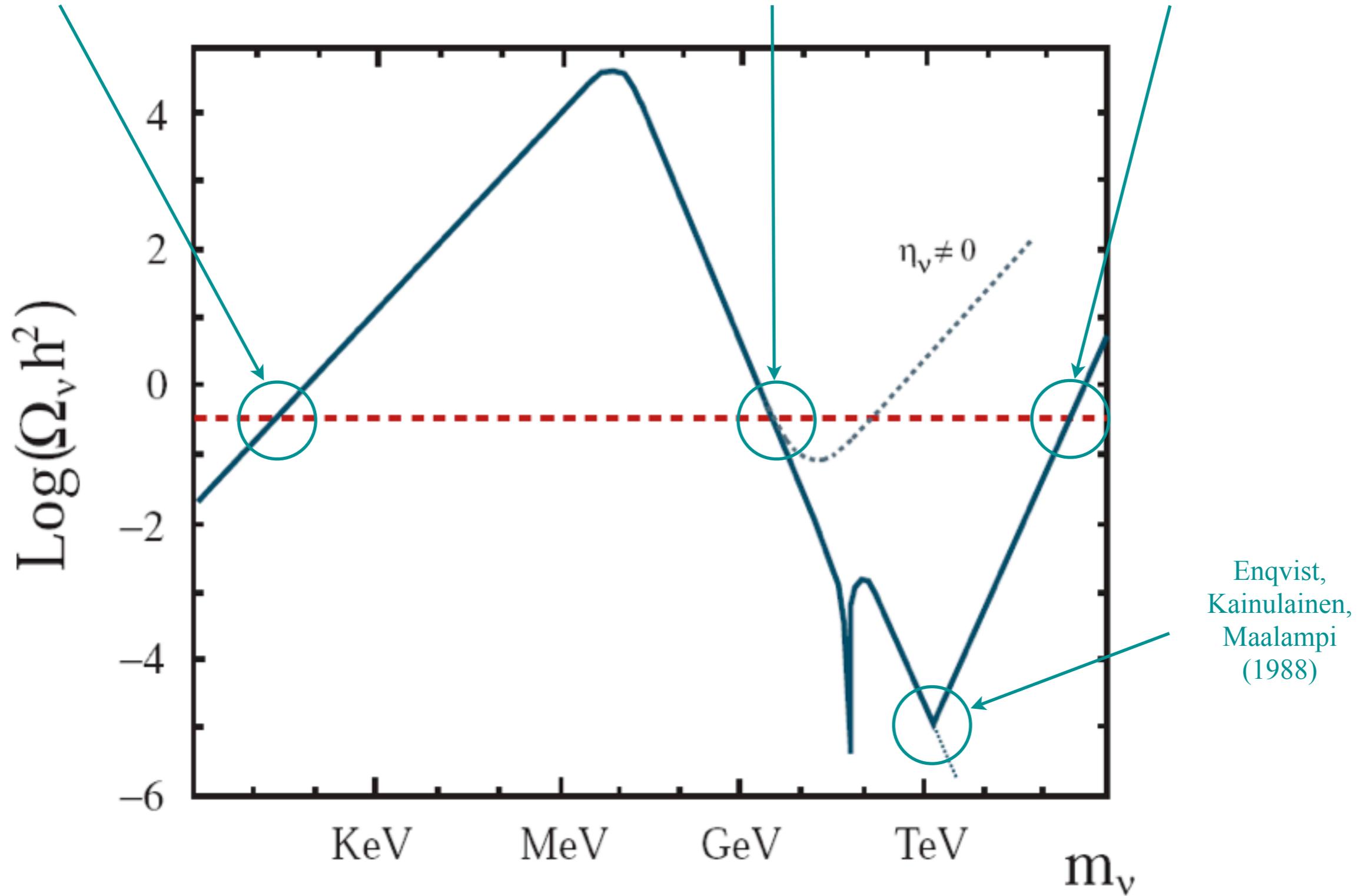
A striking prediction of the inflationary universe [5] is that  $\Omega$  is equal to 1. The X particle could saturate  $\Omega$  if  $m_X \simeq 0.75m_H$ . (Let us first take  $h$  to be 1.) Thus for  $m_H$  in the range 10–30 GeV, the condition  $\Omega_X = 1$  requires that  $m_X$  lies in the range 7.5–22 GeV and the freezing temperature  $T_f$  is in the 0.3–1 GeV range. The

## e.g. A HEAVY NEUTRINO

Cowsik-McLlland  
(1972)

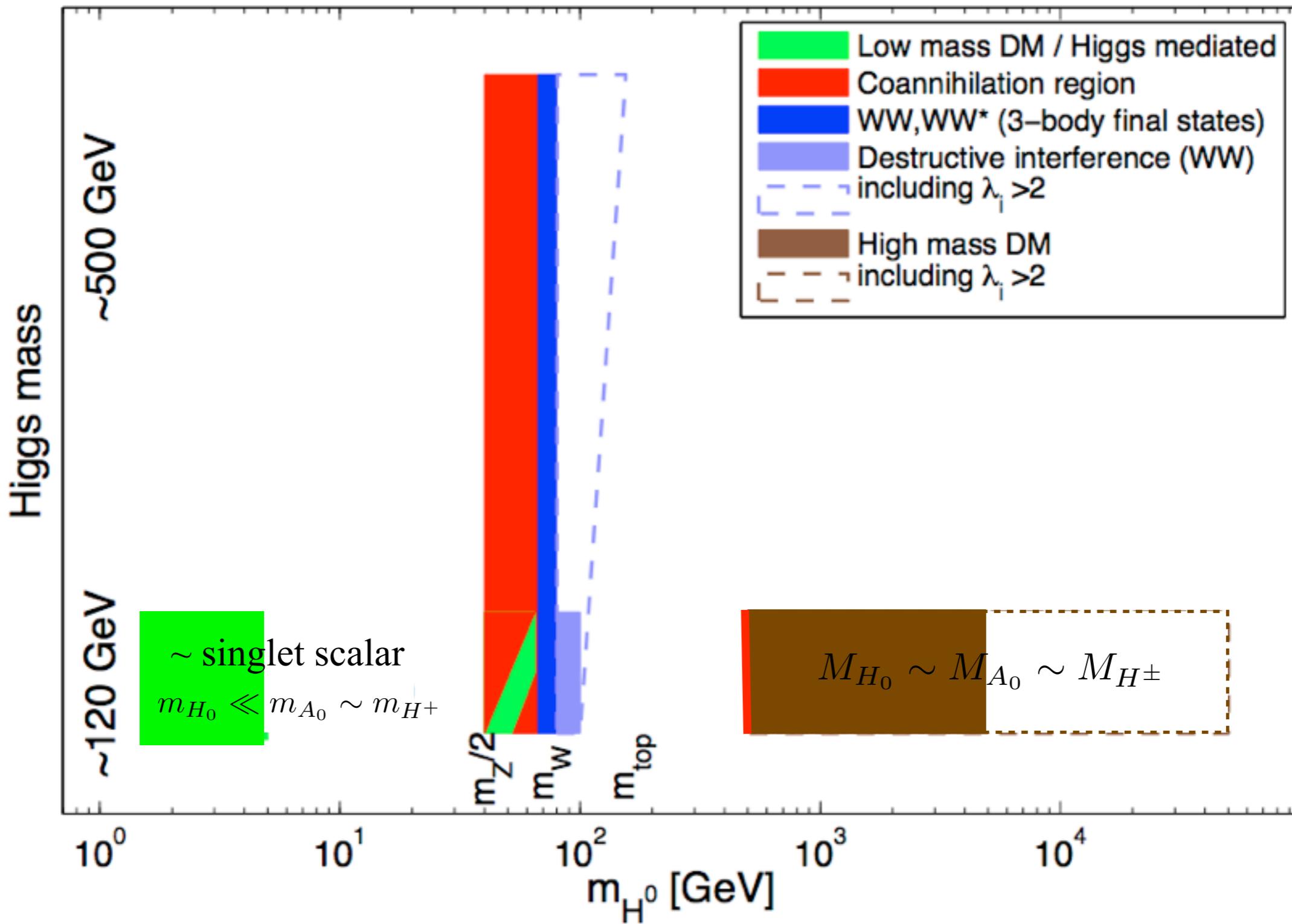
Lee-Weinberg  
(1977)

Griest-Kamionkowski  
(1989)



(Figure by Kimmo Kainulainen)

## e.g. THE INERT DOUBLET



(Fig. by Michael Gustafsson)

ONLY EXPERIMENTS CAN TELL

SMS  
Singlet Scalar through the ~~Higgs~~ Portal

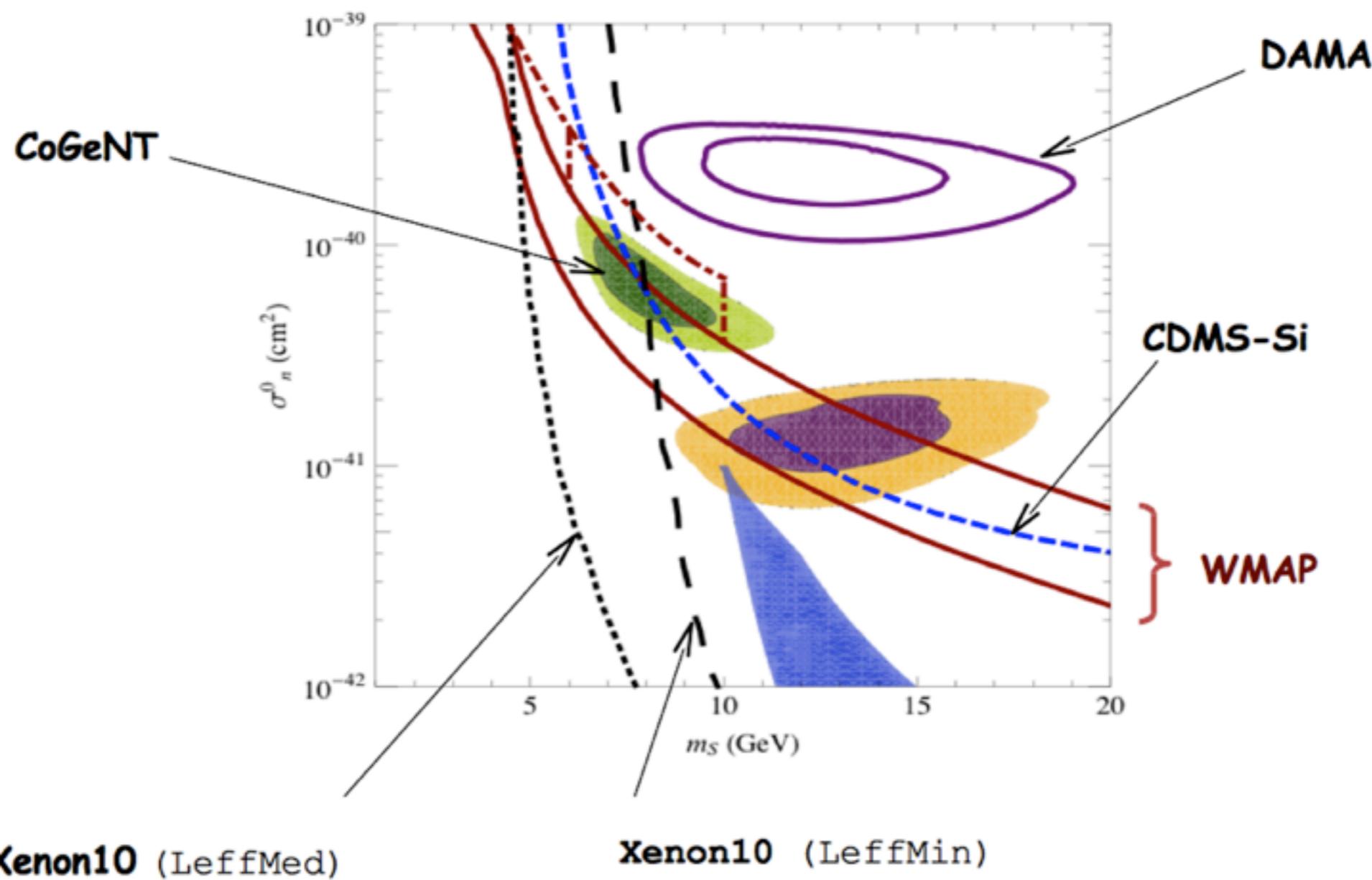
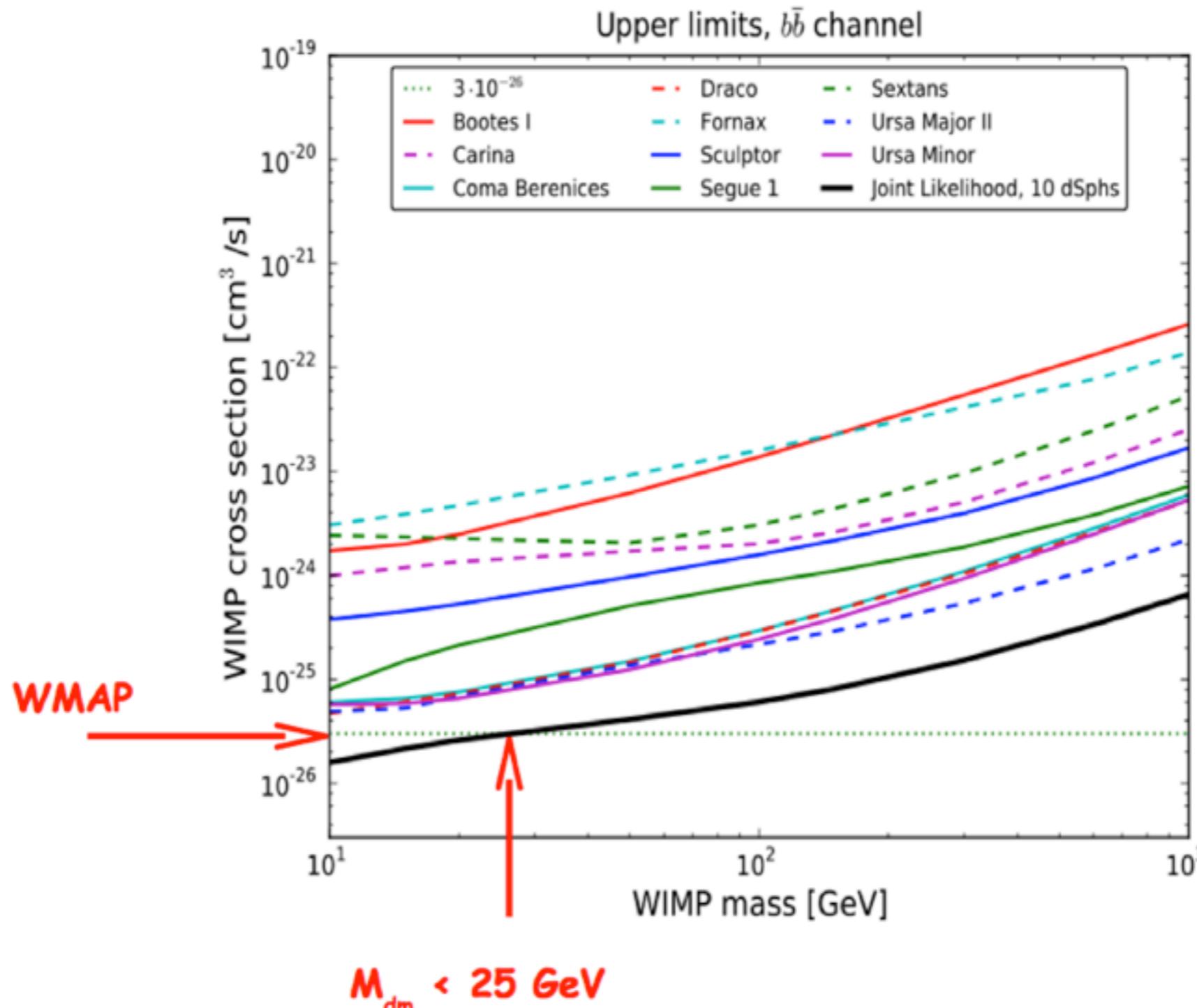


Figure from Andreas, Arina, Hambye, Ling & M.T. arXiv:1003.2595

ONLY EXPERIMENTS CAN TELL

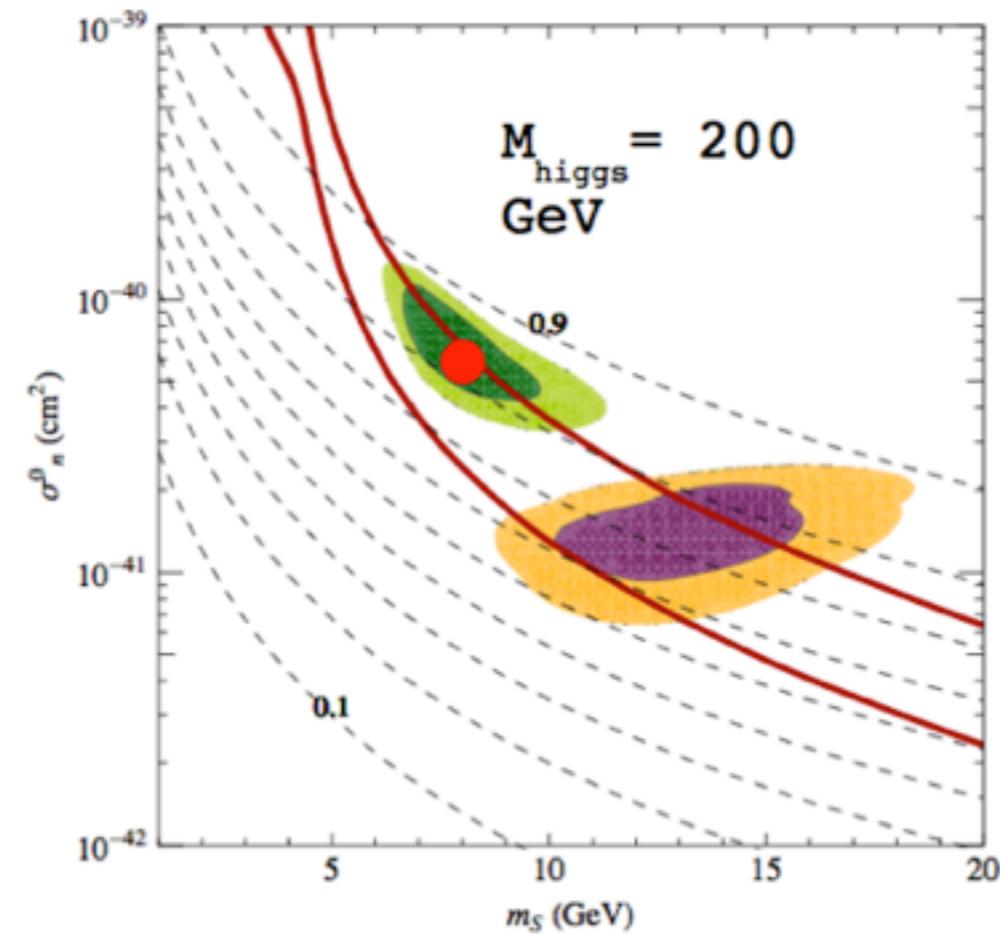
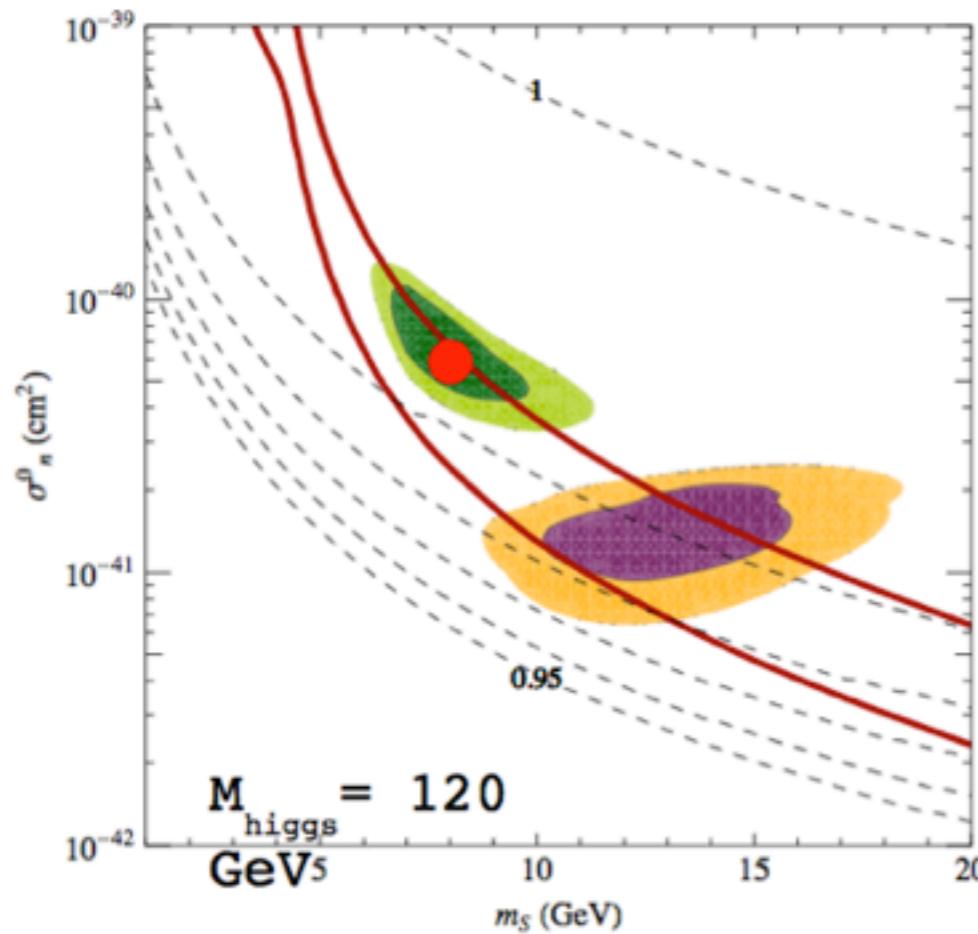
## Limits from nearby dwarf spheroidal galaxies (Fermi-LAT)



ONLY EXPERIMENTS CAN TELL

## Light Scalar = Very Invisible Higgs Scenario

SMS



For  $M_{\text{DM}} = 8$  GeV

$M_{\text{higgs}} = 120$  GeV

$M_{\text{higgs}} = 200$  GeV

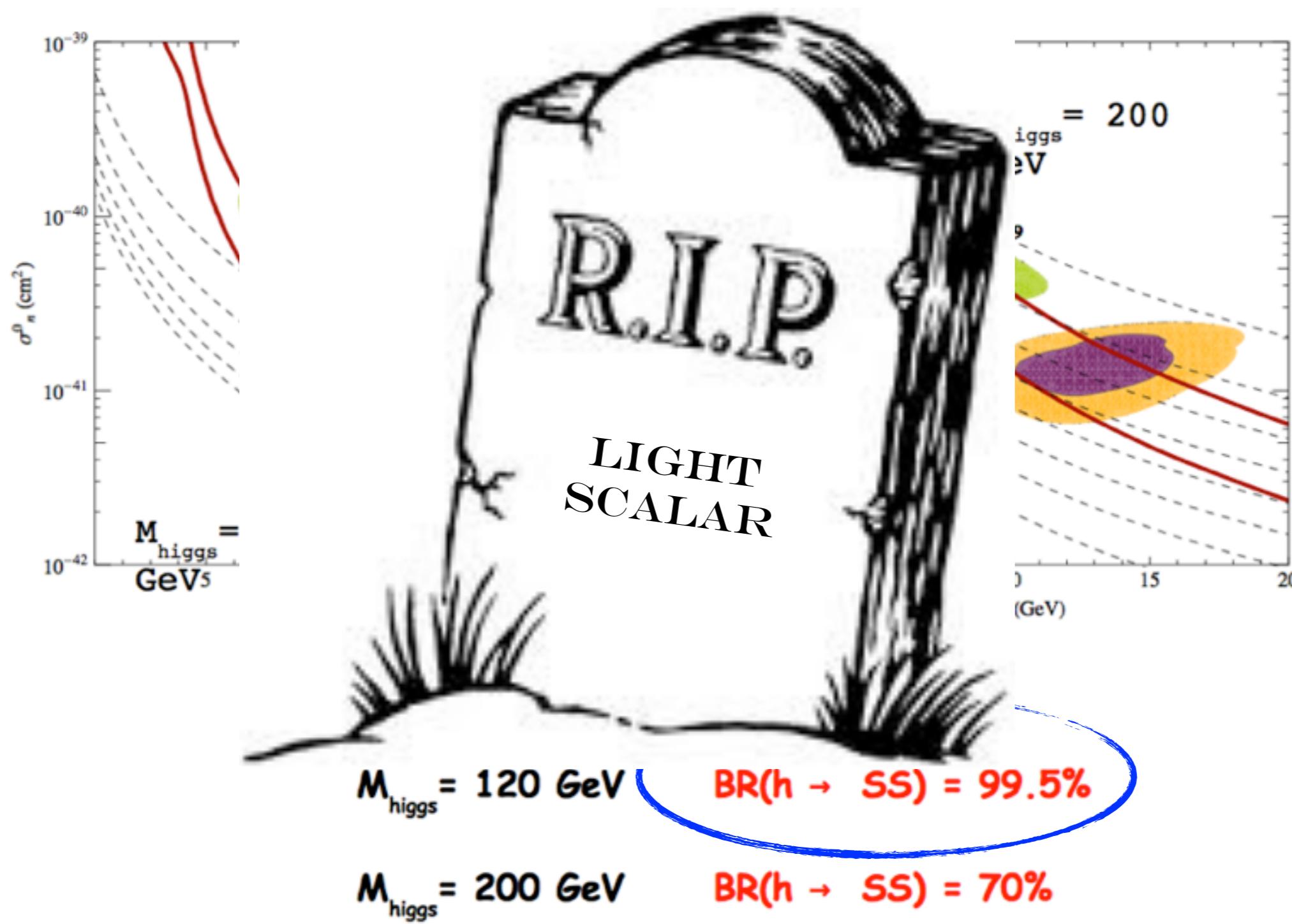
$\text{BR}(h \rightarrow SS) = 99.5\%$

$\text{BR}(h \rightarrow SS) = 70\%$

Andreas, Arina, Ling, Hambye, MT (2010)

ONLY EXPERIMENTS CAN TELL

## Light Scalar = Very Invisible Higgs Scenario



Andreas, Arina, Ling, Hambye, MT (2010)

# SO, WHICH MASS SCALE?

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## The Baryon-Dark Matter Coincidence

Low Mass WIMP,  $M_{\text{DM}} \sim \text{few GeV?}$

## Dark Matter and Electroweak Symmetry Breaking

Medium Mass WIMP,  $M_{\text{DM}} \sim M_H?$

## Minimal Dark Matter & Siblings

Large Mass WIMP,  $M_{\text{DM}} \sim \text{few TeV?}$

# SO, WHICH MASS SCALE?

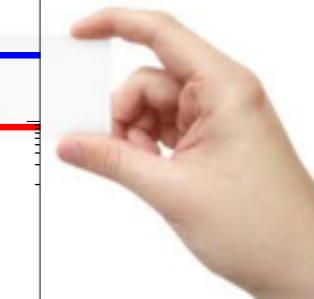
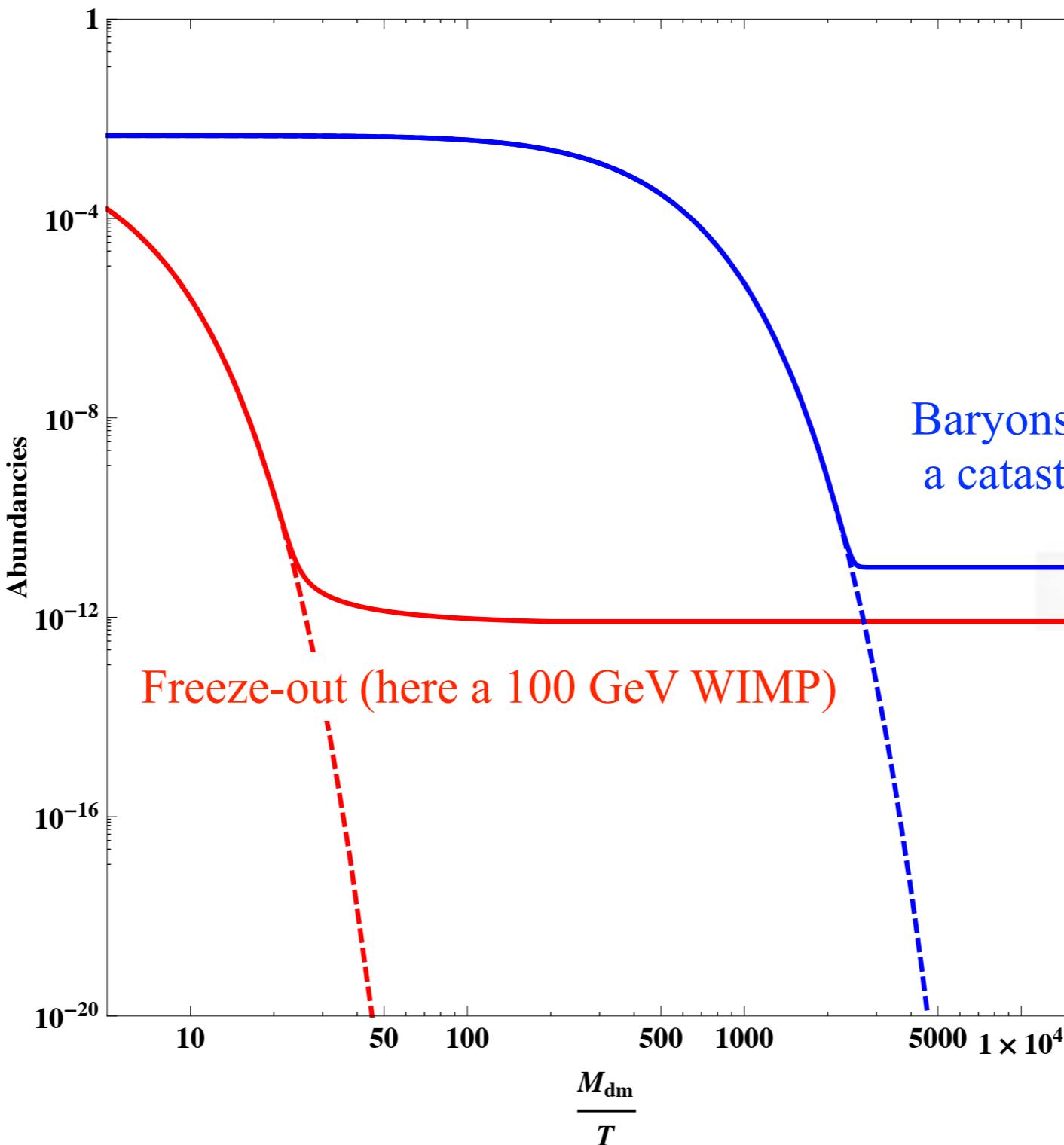


Standard  
~ 100 GeV

Heavy  
~ TeV

Light  
~1-10 GeV

# 1. BARYON - DARK MATTER COINCIDENCE



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$$\frac{\Omega_{DM}}{\Omega_B} = \frac{M_{DM}}{M_p} \times \frac{Y_{DM}}{Y_B} = \mathcal{O}(5)$$



## 1. BARYON - DARK MATTER COINCIDENCE

BARYON ASYMMETRY  $\longrightarrow$  ASYMMETRIC DM?

$$\frac{\Omega_{DM}}{\Omega_B} = \frac{M_{DM}}{M_p} \times \frac{\cancel{Y_{DM}}}{\cancel{Y_B}} = \mathcal{O}(5)$$

A LIGHT WIMP?

Nussinov (1985); Barr; Kaplan; Gudnasson *et al*; Dodelson *et al*; Kitano *et al*; Farrar & Zaharijas; Lopez Honorez *et al*; Zurek *et al*; etc...

Some recent models: aidogenesis, cogenesis, xogenesis, baryomorphosis, darkogenesis,... (I personally prefer «Matter Genesis»)

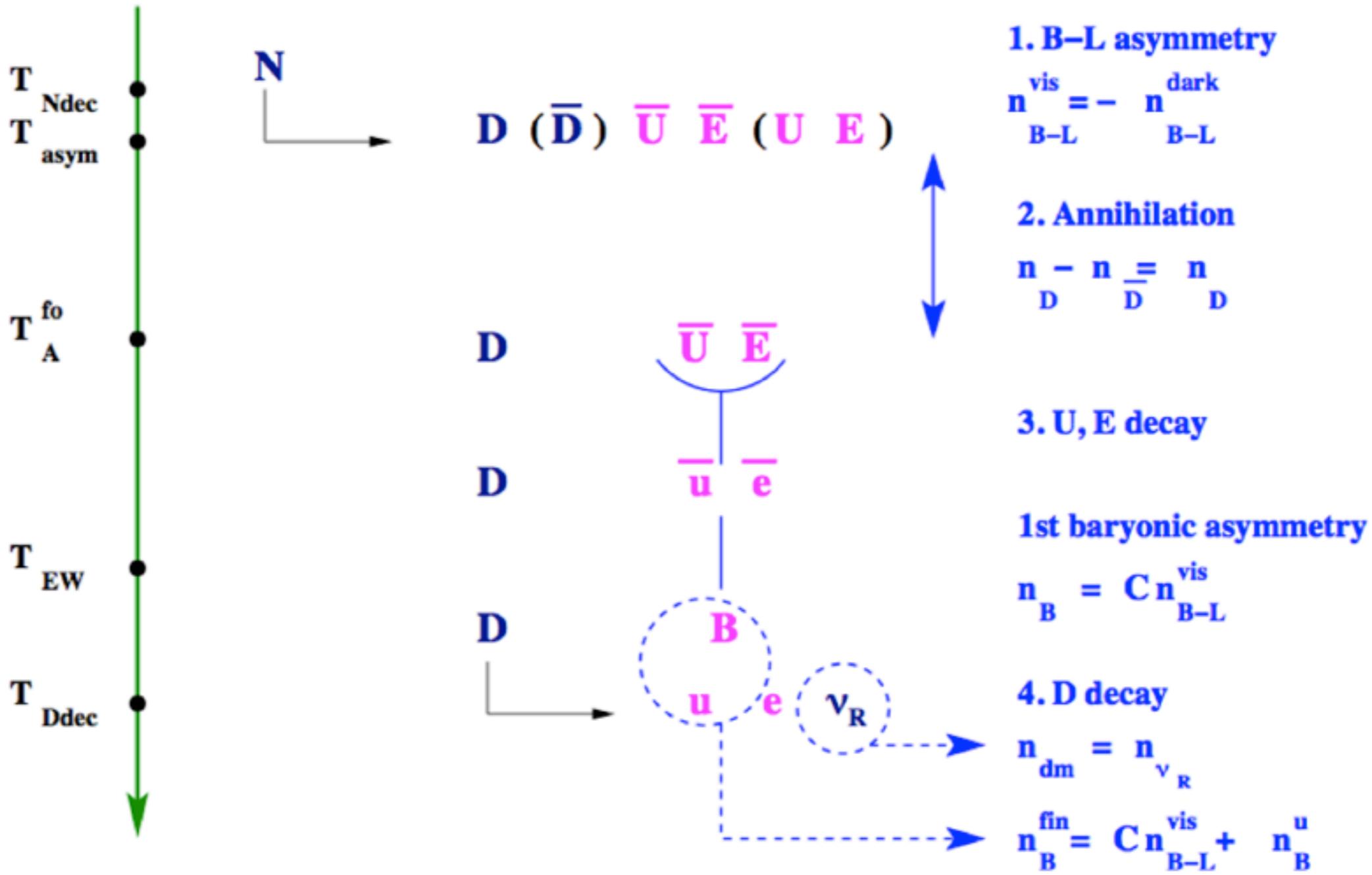


Figure 1: Steps of Matter Genesis

Figure from Lopez Honorez, Cosme and M.T. (2005)

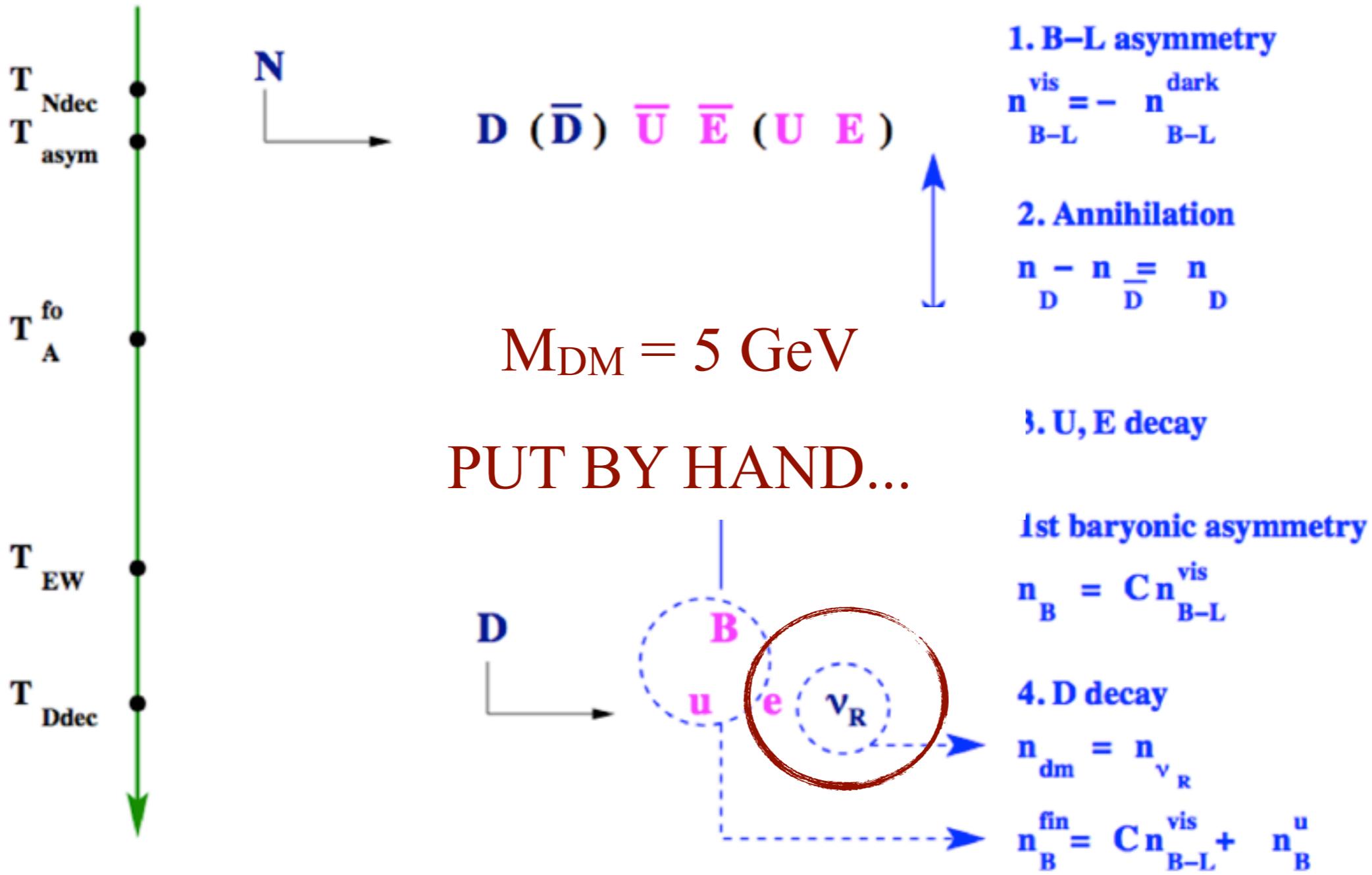


Figure 1: Steps of Matter Genesis

Figure from Lopez Honorez, Cosme and M.T. (2005)



# NEED A REALLY GREAT WATCHMAKER

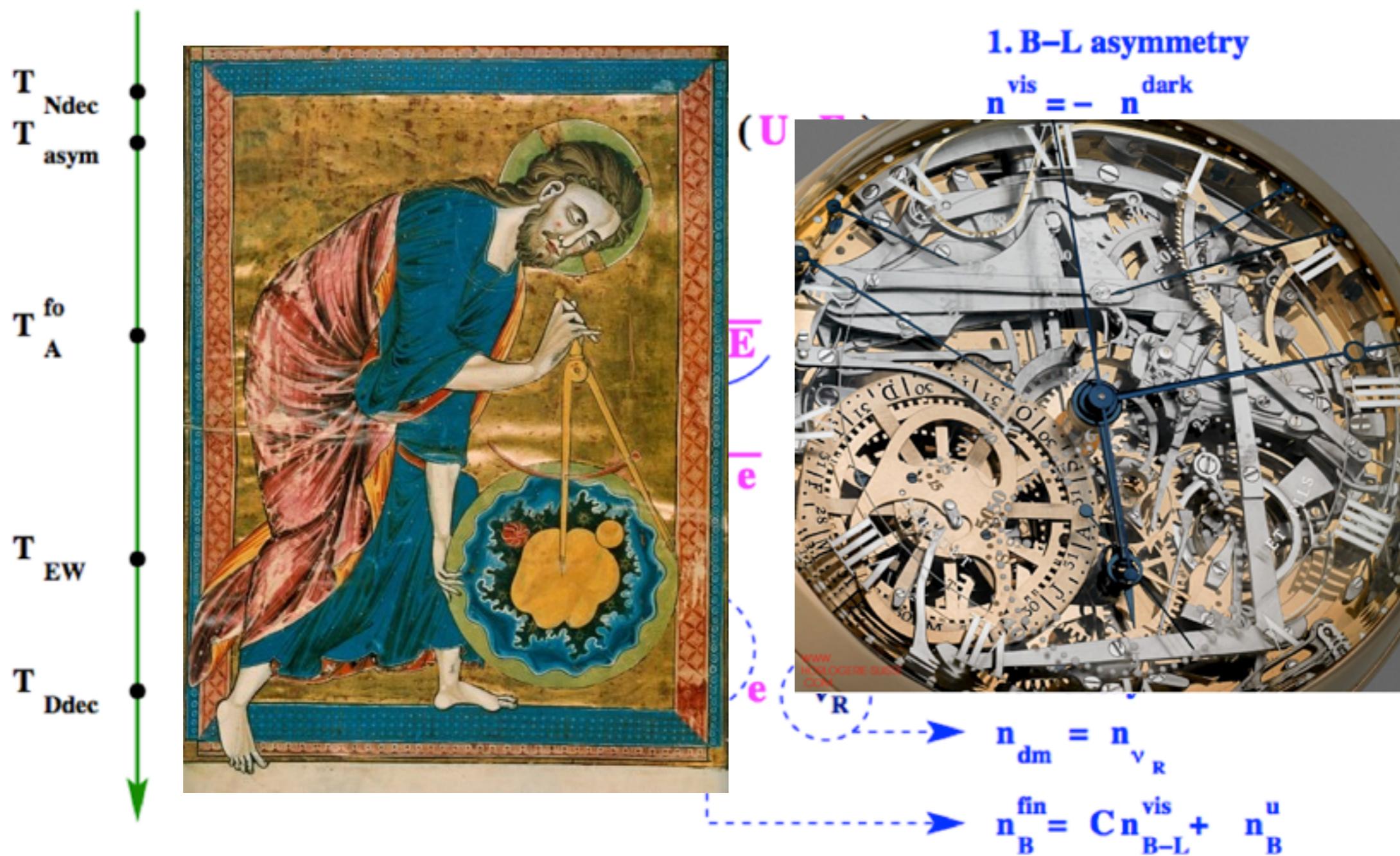
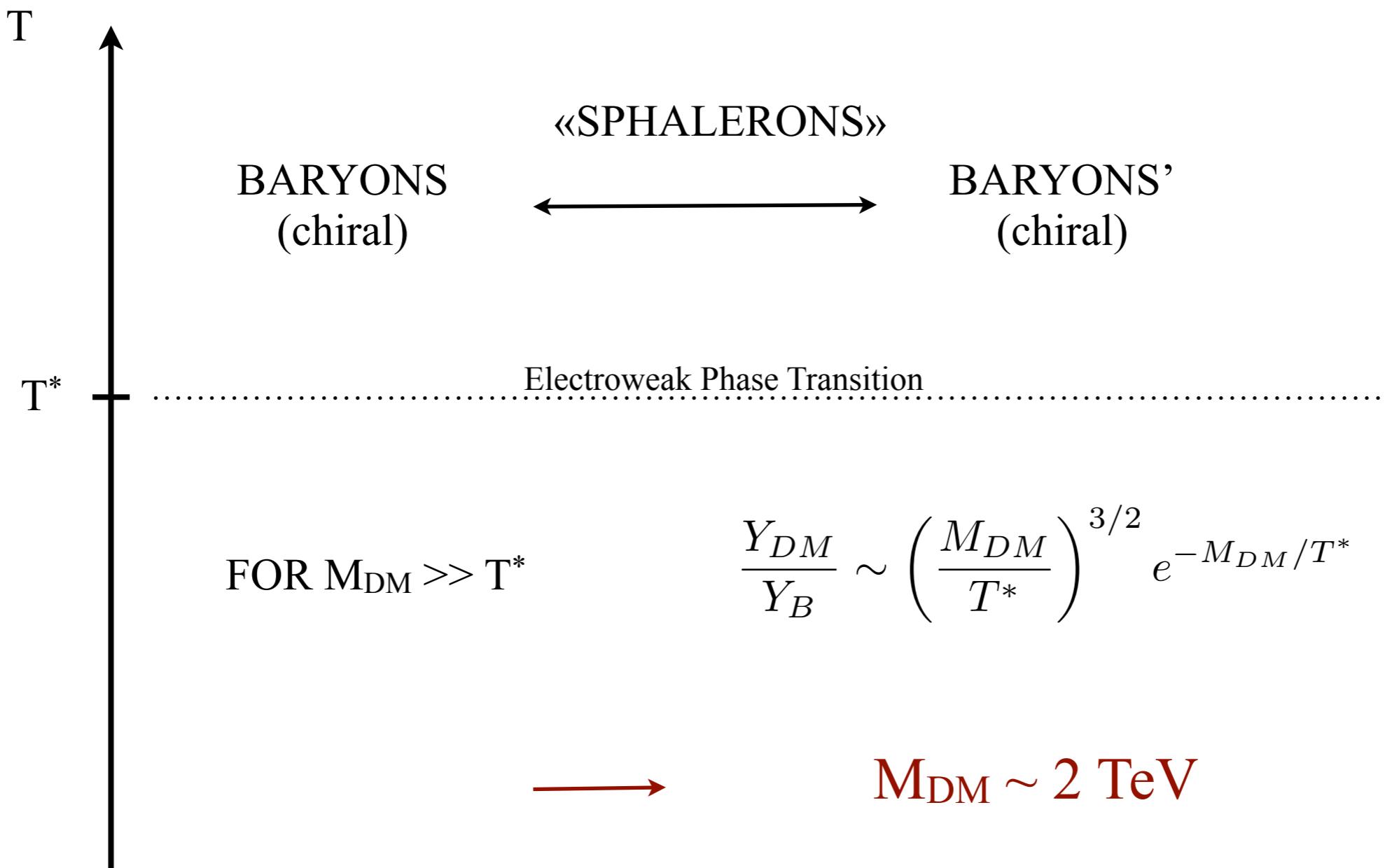


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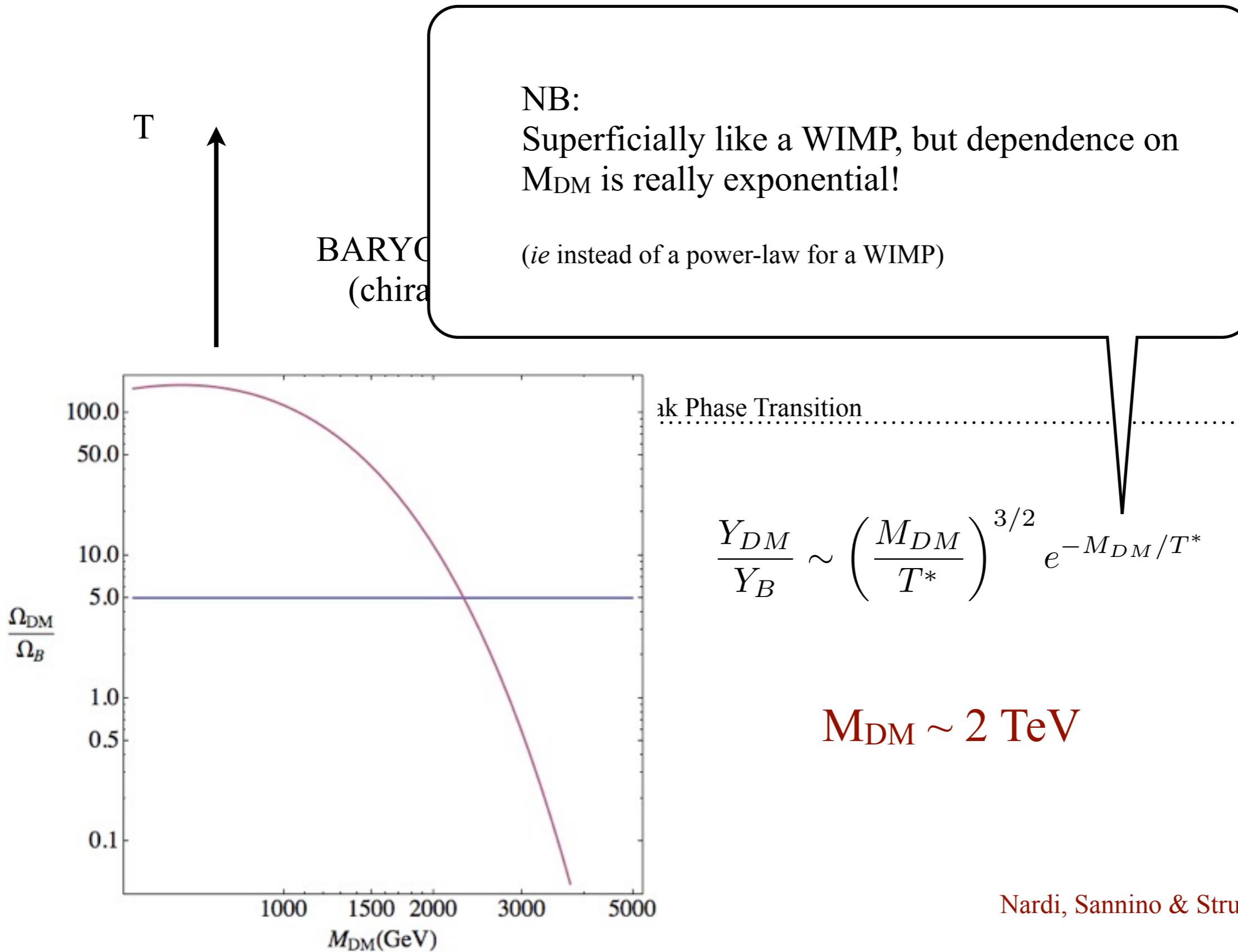
## ANYWAY, ASYMMETRIC DM DOES NOT MEAN LIGHT DM



Nardi, Sannino & Strumia (2008)



## ANYWAY, ASYMMETRIC DM DOES NOT MEAN LIGHT DM



## 2. DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING?

$$\mathcal{L}_{SM} \supset \mu^2 |H|^2$$

Unique!

- ☞ Origin of Electroweak Symmetry Breaking
- ☞ Portal to renormalizable couplings to New Physics!

## 2. DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING?

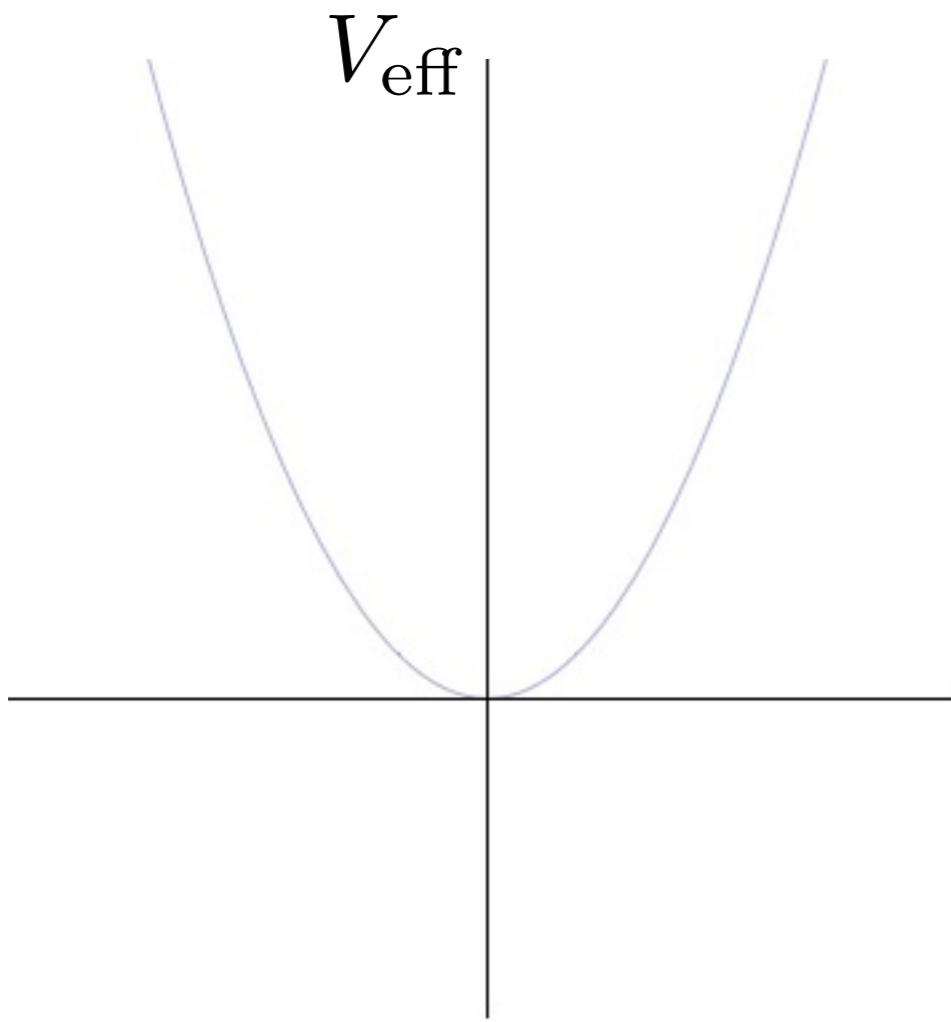
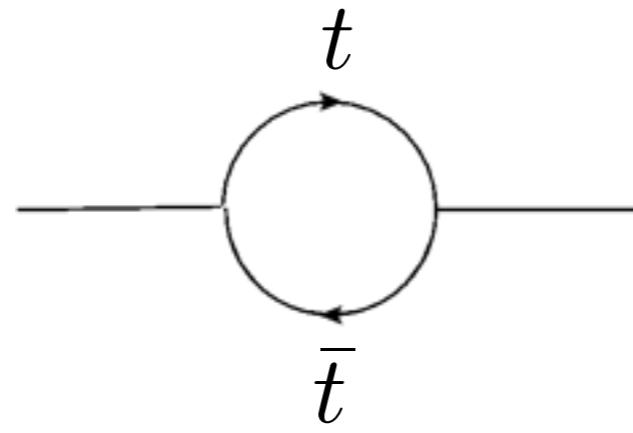
$$\mathcal{L} \supset S^2 |H|^2$$

- ☞ Origin of Electroweak Symmetry Breaking
- ☞ Portal to renormalizable couplings to New Physics!
- ☞ All of the above?

(Patt & Wilczek; Quiros & Espinosa; Hambye & MT;...)

## 2. DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING?

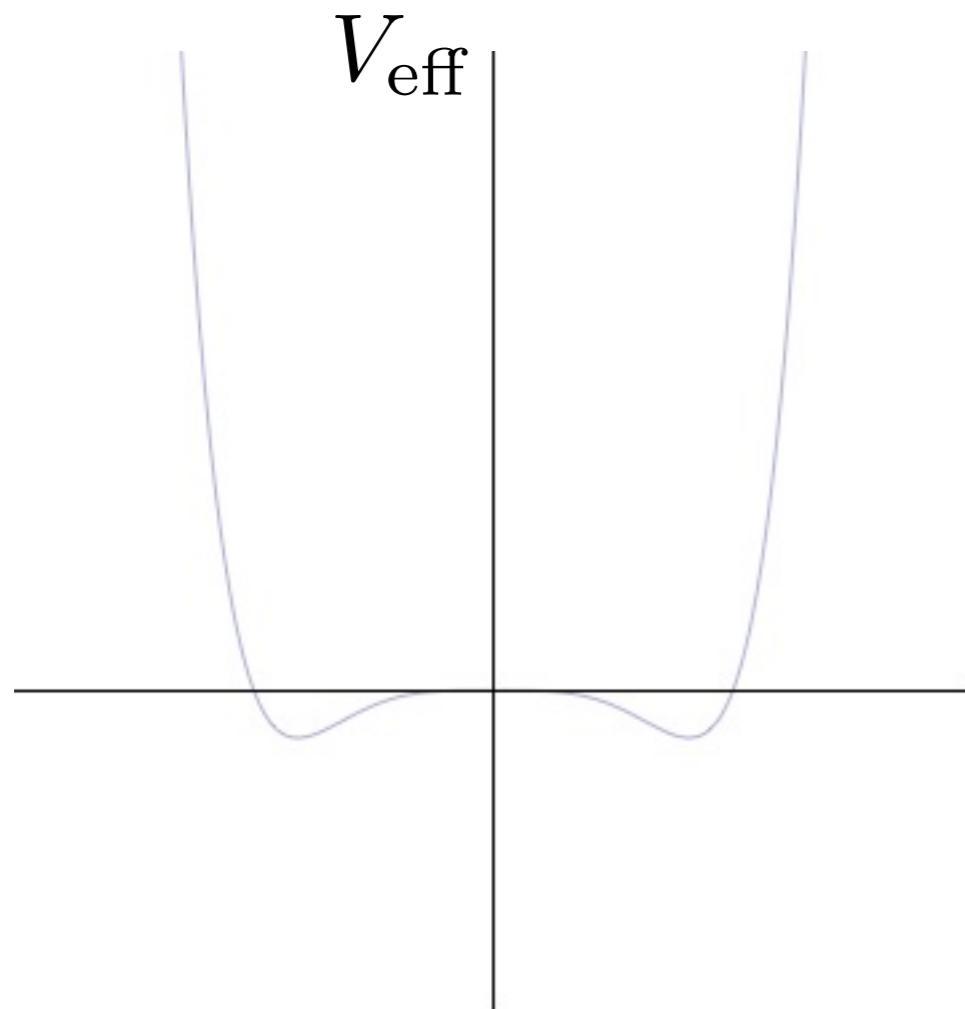
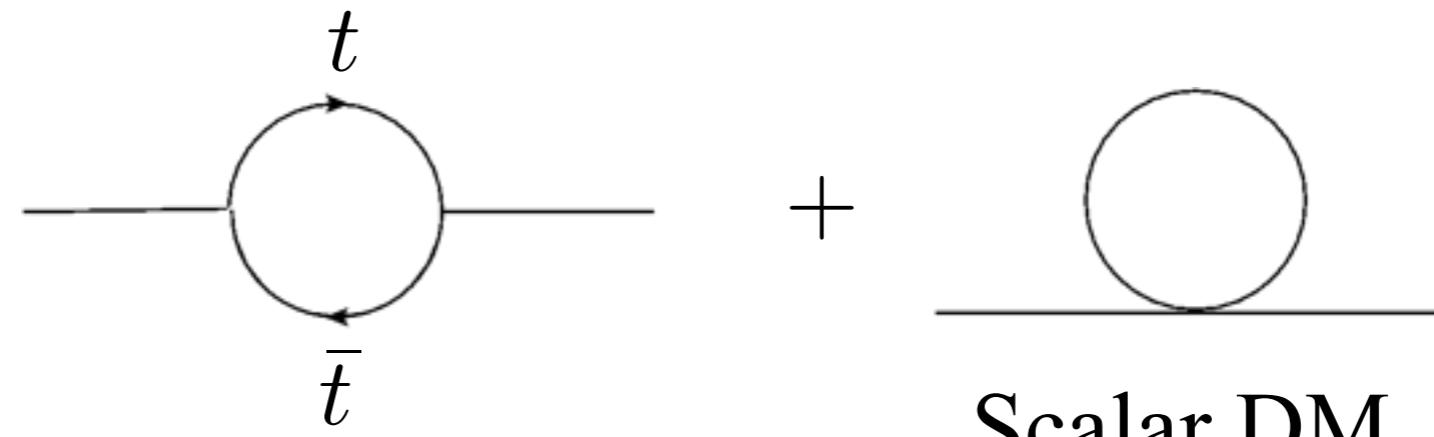
$$\Delta V_{\text{eff}}(H) \supset$$





# DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING?

$$\Delta V_{\text{eff}}(H) \supset$$

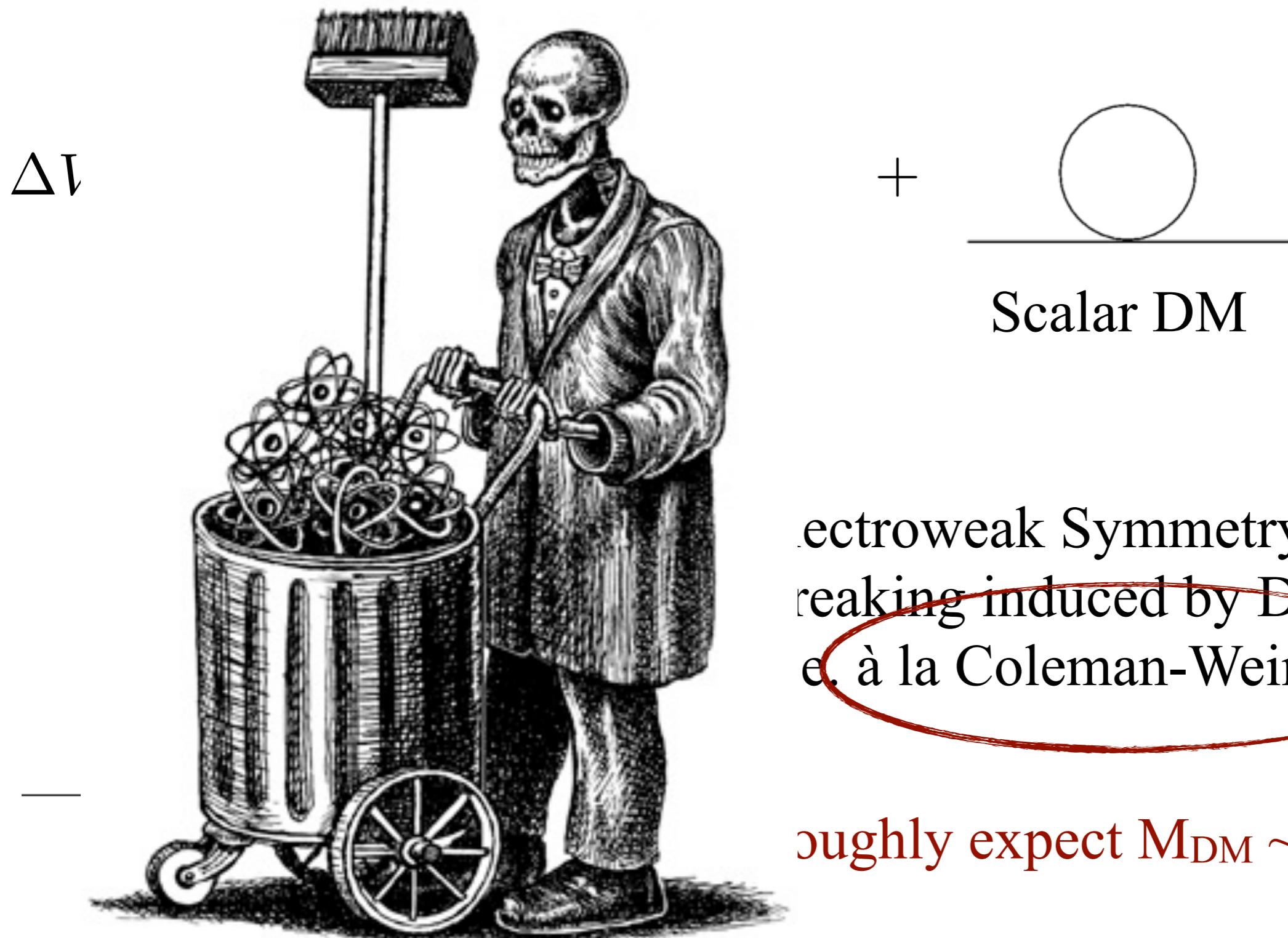


Electroweak Symmetry  
Breaking induced by DM  
(i.e. à la Coleman-Weinberg)

Roughly expect  $M_{\text{DM}} \sim M_H$

(Quiros & Espinosa; Hambye & MT)

## 2. DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING?



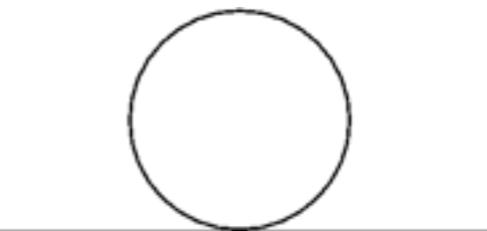
**The Dustbin of History**

(Quiros & Espinosa; Hambye & MT)

## 2. DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING?



$$+ \quad - +$$



Scalar DM

Electroweak Symmetry  
Breaking induced by DM  
(i.e. à la Coleman-Weinberg)

Roughly expect  $M_{DM} \sim M_H$

(Quiros & Espinosa; Hambye & MT)



# DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING

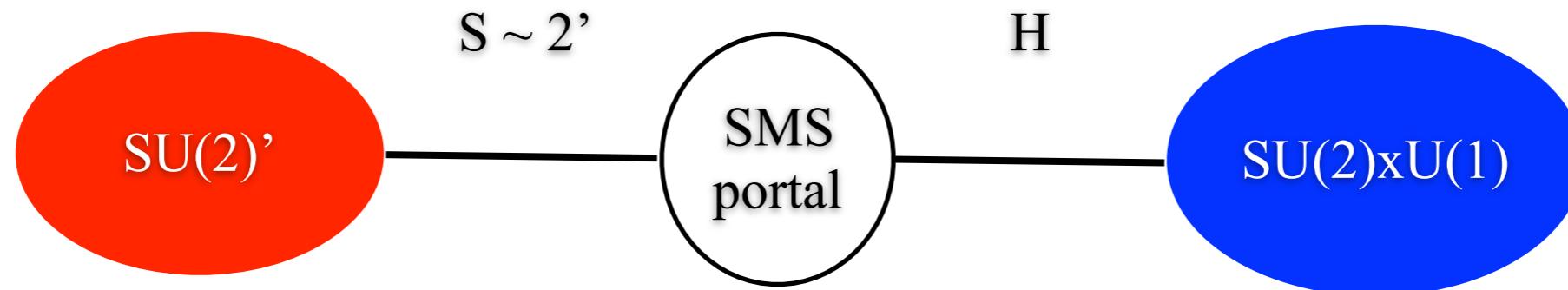
	$\lambda_1$	$\lambda_2$	$\lambda_3$	$\lambda_4$	$\lambda_5$	$M_h$	$M_{H_0}$	$M_{A_0}$	$M_{H^\pm}$	$h_{BR}$	$W_{BR}$
I	-0.11	0	5.4	-2.8	-2.8	120	12	405	405	100%	0%
I	-0.11	-2	5.4	-2.7	-2.7	120	43	395	395	100%	0%
I	-0.11	-3	5.4	-2.6	-2.6	120	72	390	390	94%	6 %
I	-0.30	0	7.6	-4.1	-4.1	180	12	495	495	100%	0 %
I	-0.30	-2.5	7.6	-3.8	-3.8	180	64	470	470	100%	0 %
II	-0.18	-3	-0.003	4.6	-4.7	120	39	500	55	100%	0 %
II	-0.29	-5	-0.07	5.5	-5.53	150	54	535	63	0%	100 %

VANILLA WIMPs,  
BUT (EMBARRISINGLY) LARGE  
COUPLINGS  
(MAINLY DUE TO  $\langle S \rangle = 0$ )

ers with WMAP DM abundance.  
bution of Higgs mediated annihi-  
 $[W_{BR}]$ .

*Hambye & M.T. (2007); ...*

## 2. DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING



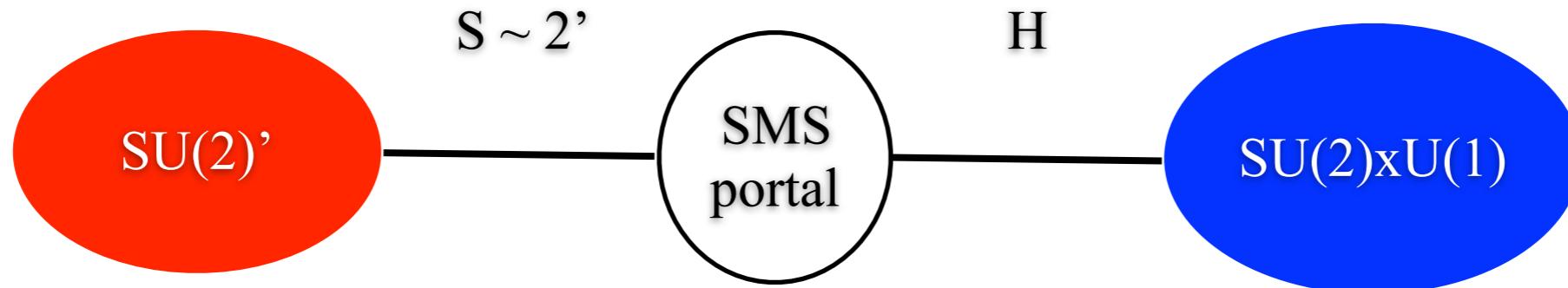
DM = Hidden Gauge Bosons  
(Stability from a global  
custodial  $SO(3)$  symmetry)

IF NO FURTHER ASSUMPTION,  $M_{DM} \sim 1$  MeV to 120 TeV

Hambye (2009); Hambye, M.T. (2009)



## DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING



DM = Hidden Gauge Bosons  
(Stability from a global  
custodial SO(3) symmetry)

$$\lambda_{HS}|S|^2|H|^2 \rightarrow \lambda_{HS}\Lambda_{HS}^2|H|^2$$

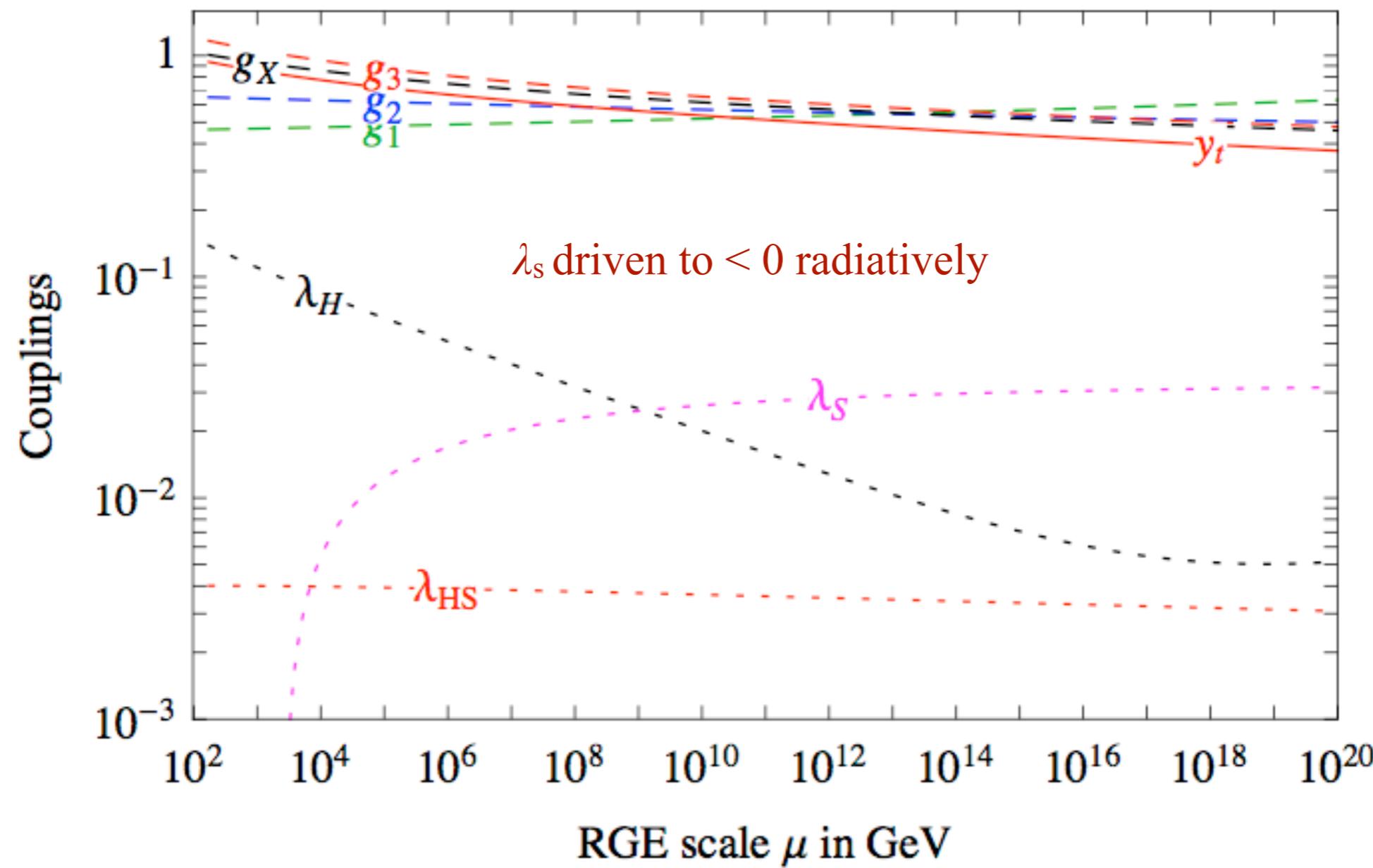
Coleman-Weinberg  
SU(2)' in confined phase

M<sub>DM</sub> ~ FEW TeV

Hambye, M.T. (2009)

## 2. DARK MATTER AND ELECTROWEAK SYMMETRY BREAKING

$$V = \lambda_H |H|^4 - \lambda_{HS} |SH|^2 + \lambda_S |S|^4$$



Hambye, Strumia (2013)



4 parameters = 4 couplings

3 fixed by  $M_h$ ,  $v_{ev}$  and relic abundance

Only 1 free parameter e.g.  $M_{DM}$

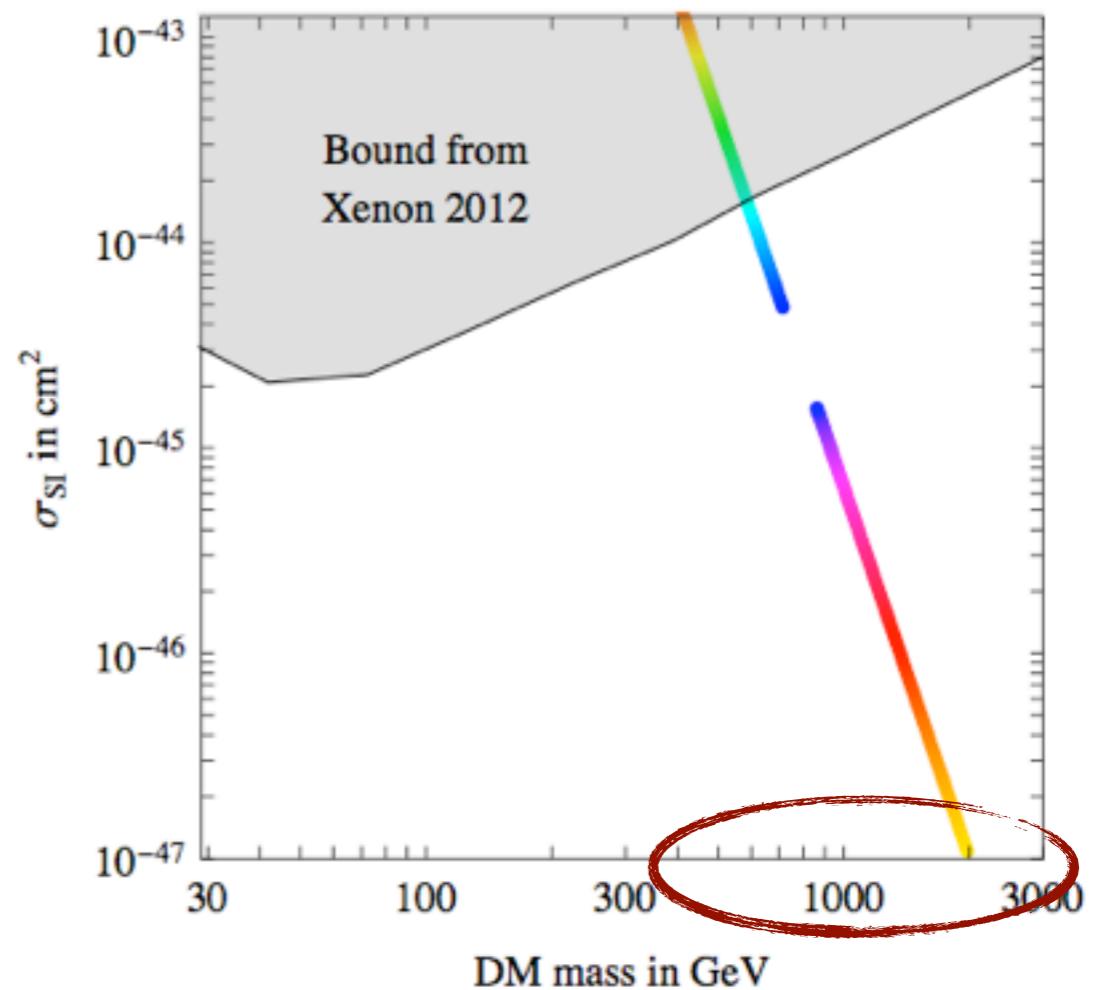
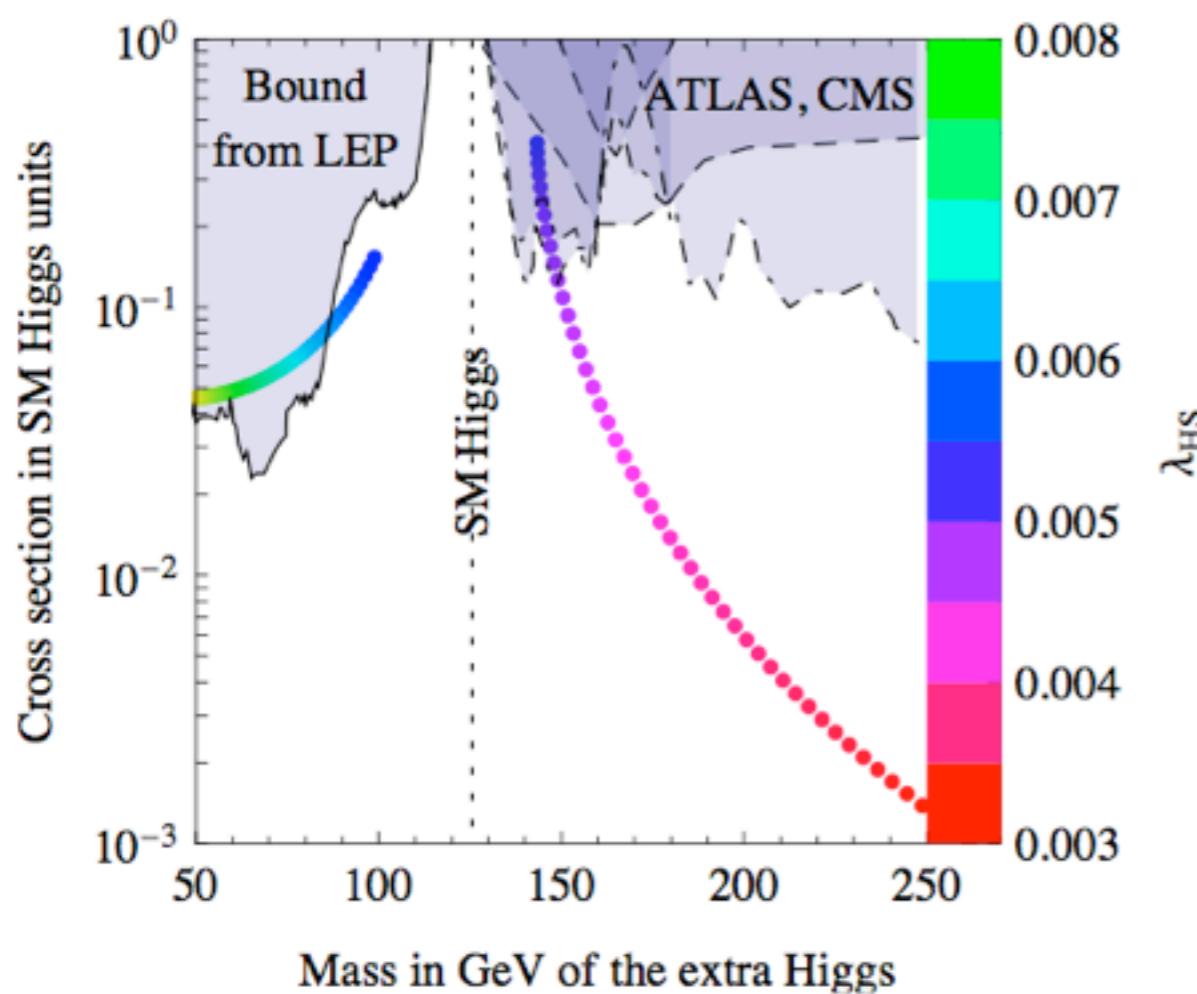


Figure 1: Predicted cross sections for the extra scalar boson (left) and for DM direct detection (right) as function of the only free parameter of the model  $\lambda_{HS}$ , varied as shown in the colour legend.

Hambye, Strumia (2013)

### 3. MINIMAL DARK MATTER & SIBLINGS

(Cirreli, Fornengo & Strumia)



### 3. MINIMAL DARK MATTER & SIBLINGS

MAIN MOTTO:

GAUGE  
INTERACTIONS  
ONLY


$$\langle \sigma v \rangle \sim \frac{\alpha^2}{M_{DM}^2}$$

DM IN THE TEV RANGE

(Cirigliano, Fornengo & Strumia)



Quantum numbers			DM can decay into	DM mass in TeV	$m_{\text{DM}^\pm} - m_{\text{DM}}$ in MeV	Events at LHC $\int \mathcal{L} dt = 100/\text{fb}$	$\sigma_{\text{SI}}$ in $10^{-45} \text{ cm}^2$
SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	Spin					
2	1/2	0	<i>EL</i>	$0.54 \pm 0.01$	350	$320 \div 510$	0.2
2	1/2	1/2	<i>EH</i>	$1.1 \pm 0.03$	341	$160 \div 330$	0.2
3	0	0	<i>HH*</i>	$2.0 \pm 0.05$	166	$0.2 \div 1.0$	1.3
3	0	1/2	<i>LH</i>	$2.4 \pm 0.06$	166	$0.8 \div 4.0$	1.3
3	1	0	<i>HH, LL</i>	$1.6 \pm 0.04$	540	$3.0 \div 10$	1.7
3	1	1/2	<i>LH</i>	$1.8 \pm 0.05$	525	$27 \div 90$	1.7
4	1/2	0	<i>HHH*</i>	$2.4 \pm 0.06$	353	$0.10 \div 0.6$	1.6
4	1/2	1/2	( <i>LHH*</i> )	$2.4 \pm 0.06$	347	$5.3 \div 25$	1.6
4	3/2	0	<i>HHH</i>	$2.9 \pm 0.07$	729	$0.01 \div 0.10$	7.5
4	3/2	1/2	( <i>LHH</i> )	$2.6 \pm 0.07$	712	$1.7 \div 9.5$	7.5
5	0	0	( <i>HHH*H*</i> )	$5.0 \pm 0.1$	166	$\ll 1$	12
5	0	1/2	—	$4.4 \pm 0.1$	166	$\ll 1$	12
7	0	0	—	$8.5 \pm 0.2$	166	$\ll 1$	46

Table 1: **Summary of the main properties of Minimal DM candidates.** Quantum numbers are listed in the first 3 columns; candidates with  $Y \neq 0$  are allowed by direct DM searches only if appropriate non-minimalities are introduced. The 4th column indicates dangerous decay modes, that need to be suppressed (see sec. 2 for discussion). The 5th column gives the DM mass such that the thermal relic abundance equals the observed DM abundance (section 4). The 6th column gives the loop-induced mass splitting between neutral and charged DM components (section 3); for scalar candidates a coupling with the Higgs can give a small extra contribution, that we neglect. The 7th column gives the  $3\sigma$  range for the number of events expected at LHC (section 6). The last column gives the spin-independent cross section, assuming a sample value  $f = 1/3$  for the uncertain nuclear matrix elements (section 5).

(Cirigli, Fornengo & Strumia)



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## STABILITY IS AUTOMATIC (NO NEED FOR AD HOC PARITY)

Properties of Minimal DM candidates. Quantum number candidates with  $Y \neq 0$  are allowed by direct DM searches only if appropriate non-minimalities are introduced. The 4th column indicates dangerous decay modes, that need to be suppressed (see sec. 2 for discussion). The 5th column gives the DM mass such that the thermal relic abundance equals the observed DM abundance (section 4). The 6th column gives the loop-induced mass splitting between neutral and charged DM components (section 3); for scalar candidates a coupling with the Higgs can give a small extra contribution, that we neglect. The 7th column gives the  $3\sigma$  range for the number of events expected at LHC (section 6). The last column gives the spin-independent cross section, assuming a sample value  $f = 1/3$  for the uncertain nuclear matrix elements (section 5).

(Cirigliano, Fornengo & Strumia)



### 3. MINIMAL DARK MATTER & SIBLINGS

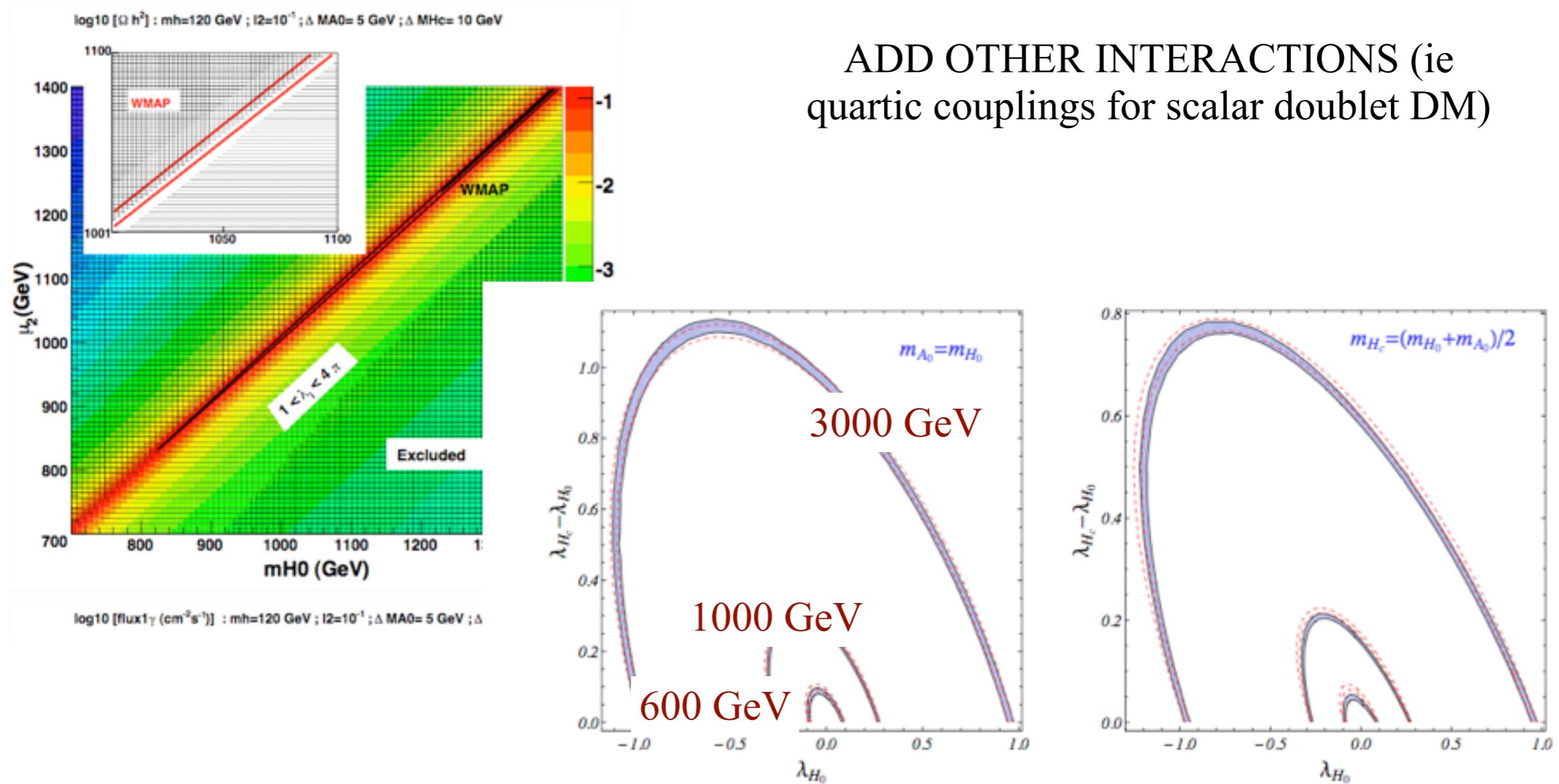


Figure 3: *Contours of  $\lambda$  for the WMAP value  $\Omega_{\text{DM}}h^2 = 0.1131 \pm 0.0034$  for  $m_{H_0} = 600$  (interior), 1000, 3000 (exterior) GeV, with  $m_{A_0} = m_{H_0}$  (left panel) and  $m_{H_c} = (m_{H_0} + m_{A_0})/2$  (right panel). Dashed curve corresponds to the approximate ellipsoid.*

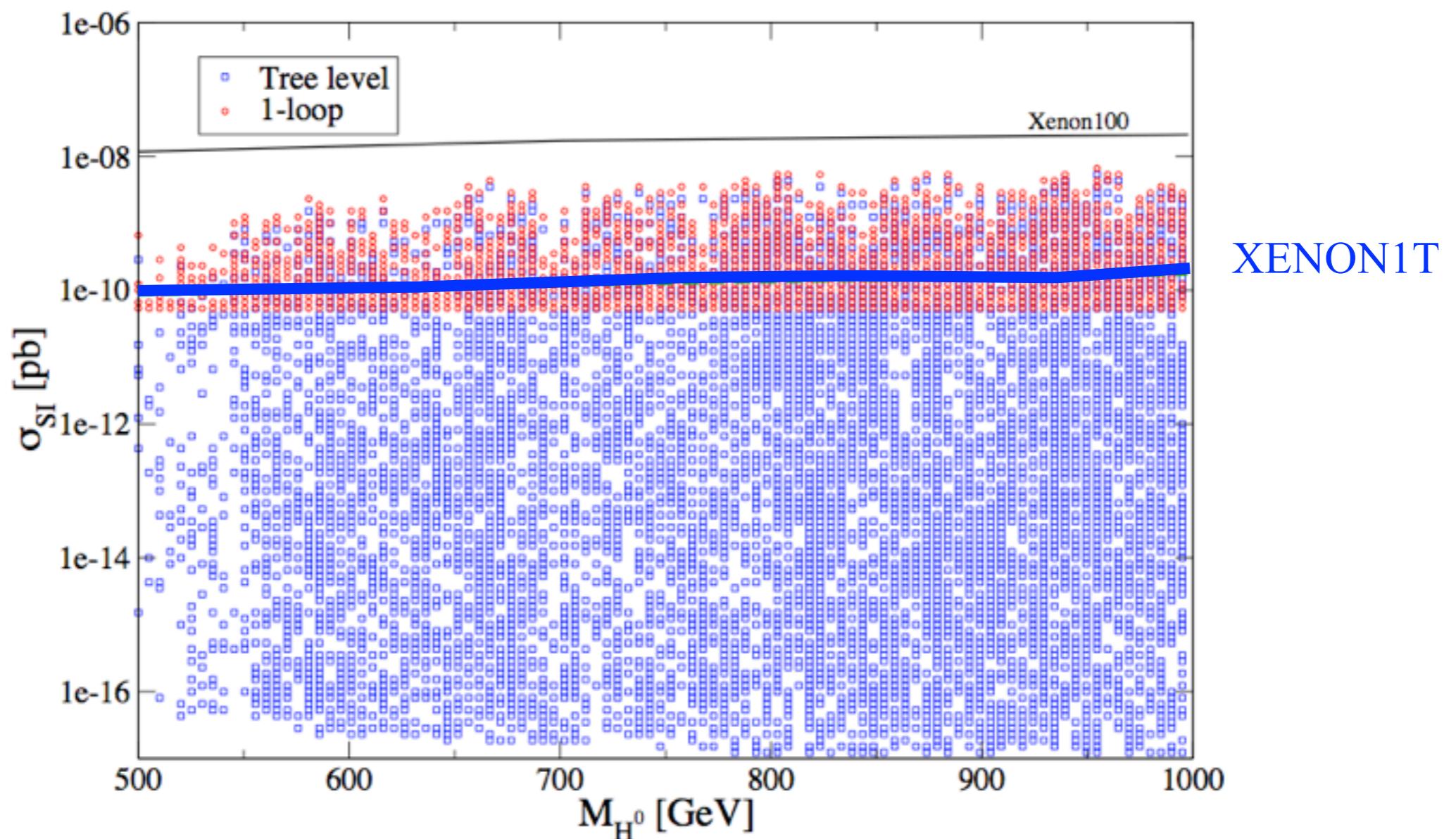
(Lopez Honorez, Nezri, Oliver & M.T.)

(Hambye, Ling, Lopez Honorez & Rocher)



### 3. MINIMAL DARK MATTER & SIBLINGS

TOO HEAVY FOR LHC BUT WITHIN REACH OF  
FUTURE DIRECT DETECTION EXPERIMENTS



(Klasen, Yaguna & Ruiz-Alvarez: arXiv:1302.1657)



## TENTATIVE CONCLUSION

DIFFICULT TO MAKE DEFINITIVE STATEMENTS REGARDING DM MASS SCALE.  
(IE COULD BE ANYTHING...)

YET, SIMPLE MODELS POINT TO THE **TEV SCALE**  
(NO SURPRISE HERE)

PERHAPS BAD FOR LHC, BUT NOT DESPERATE FOR DIRECT DETECTION.



$$\tau_p \sim \frac{M_{\text{GUT}}^4}{m_p^5} \sim 10^{41} \text{ sec} \quad p \rightarrow \pi^0 e^+$$



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$$\tau_p \sim \frac{M_{\text{GUT}}^4}{M_{\text{DM}}^5} \sim 10^{26} \text{ sec}$$

IN THE BALL PARK OF INDIRECT SEARCHES  
(antimatter, gamma rays, ...)

# BACKUP SLIDES

## MORE ON HIDDEN SECTORS

The hypothesis of thermal equilibrium basically fixes  
the moment (time/temperature) of decoupling

$$x = x^*$$

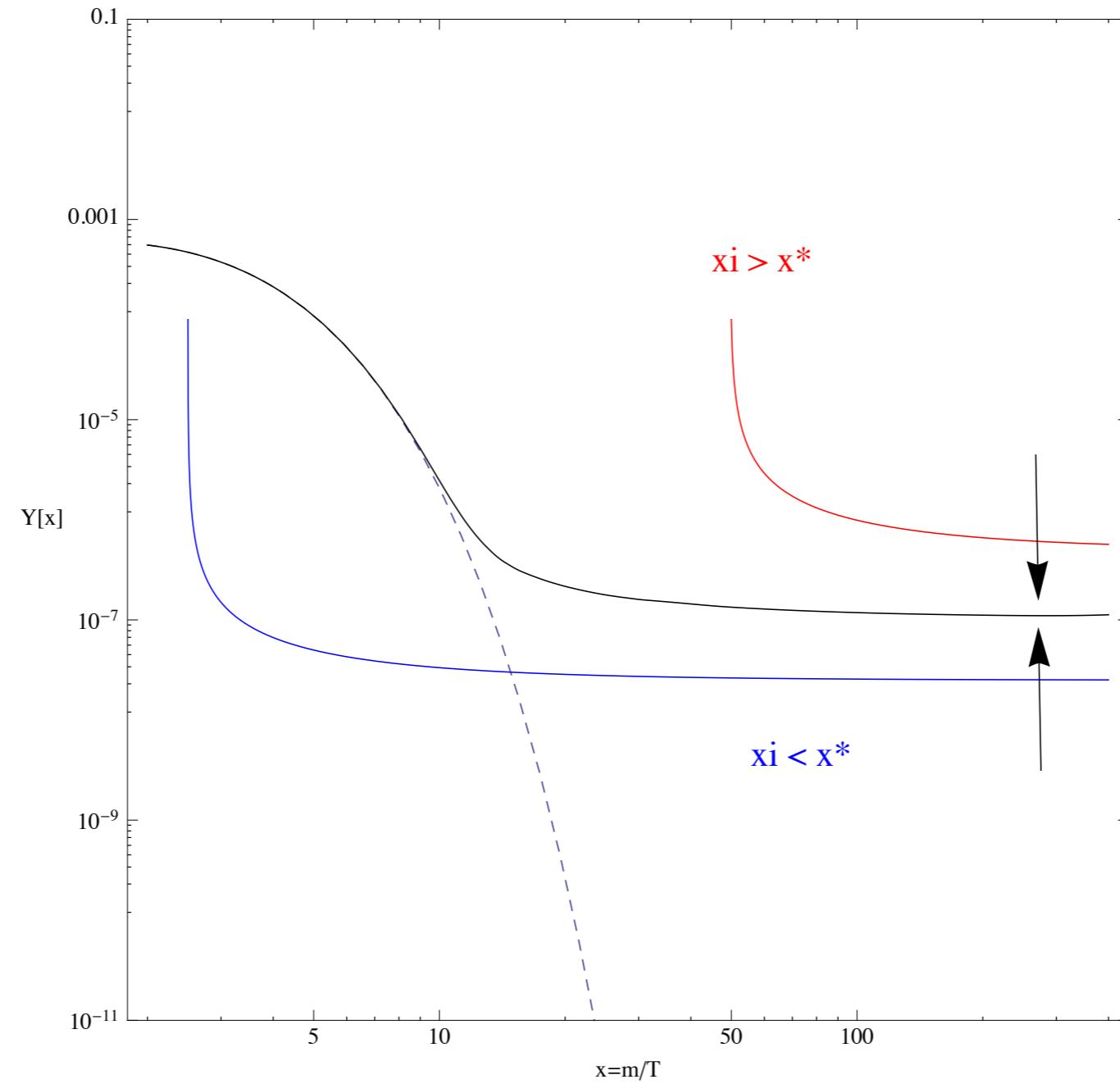
A WIMP-like behaviour may occur in more generic scenarios\*

$$Y_\infty|_{\text{non-thermal}} = \frac{x_i}{x^*} Y_\infty|_{\text{thermal}} \propto \frac{x_i}{\langle \sigma v \rangle}$$

in which  $x_i$  is the characteristic time of DM release/production

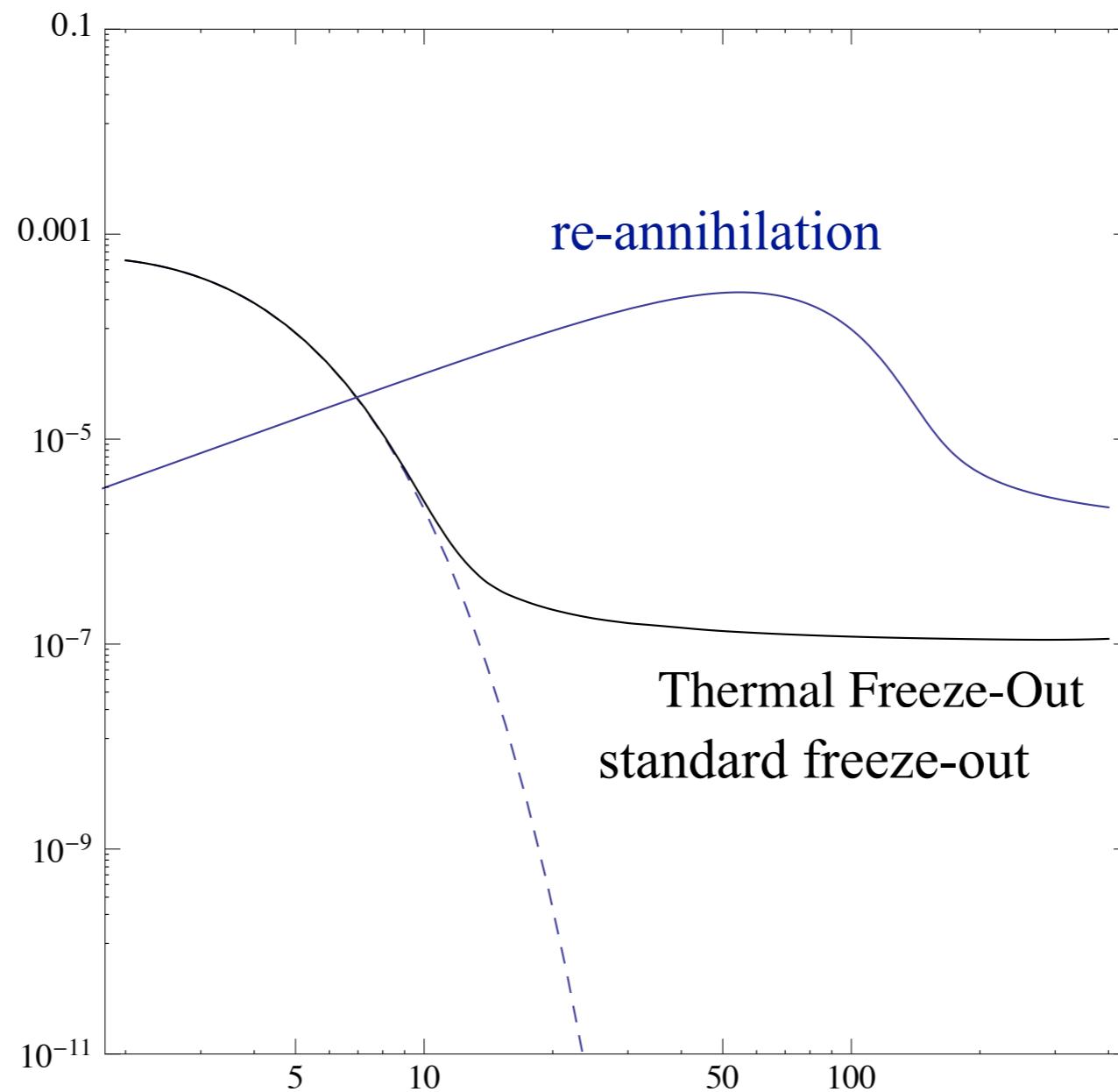
\* T. Moroi and L. Randall; B.S. Acharya, G. Kane, S. Watson, P. Kumar;...

For instance  $x_i > x^*$  requires  $\langle \sigma v \rangle$  to be larger than 1 pbarn to reach the same relic abundance



e.g. Production of DM (e.g. scattering  $SM + \Sigma \rightarrow X + SM'$ )

followed by annihilation  $X + X \rightarrow SM + SM$



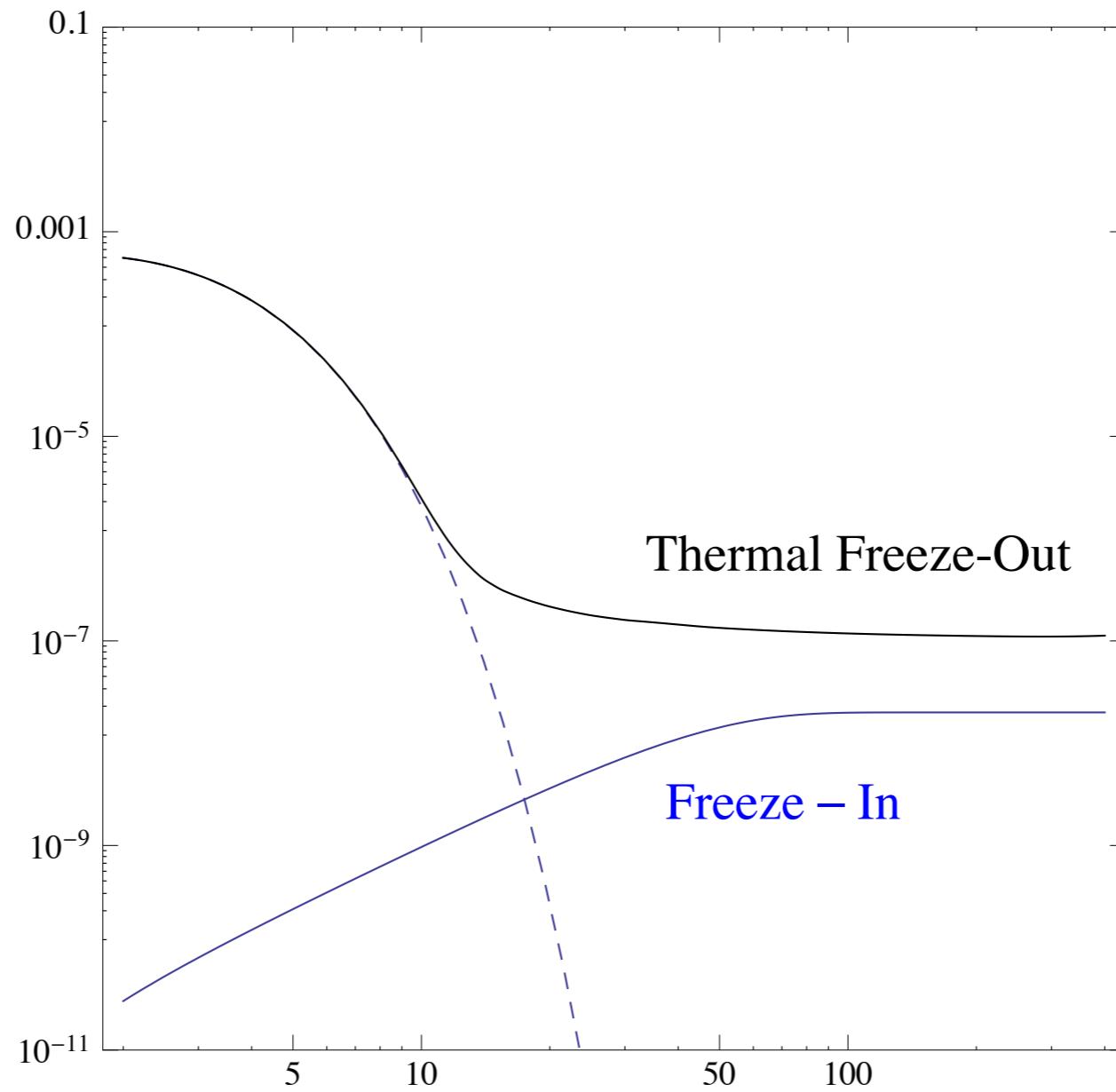
This is called a **re-annihilation** regime.\*

\* Cheung, Elor, Hall and Kumar

Now, if

$$Y(x_i) \lesssim Y_\infty|_{\text{thermal freeze-out}}$$

there is no re-annihilation. Instead  $Y_\infty = Y(x_i)$ .



This is called **freeze-in** \*

\* Mc Donald (02); Hall, Jedamzik, March-Russell and West (09)

Typically freeze-in leads to

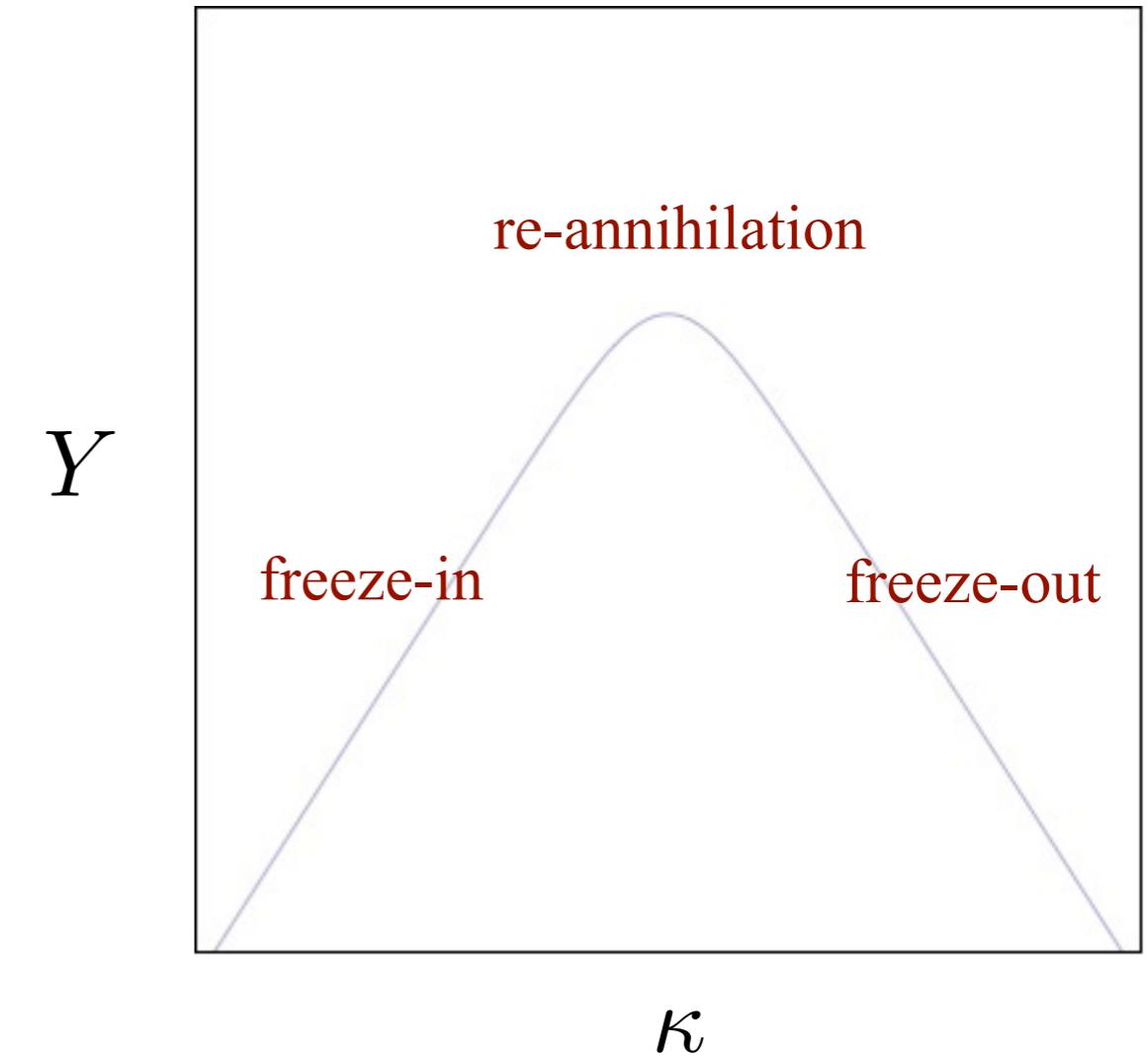
$$Y_{FI} \sim \kappa^2 \times M \times t_U$$



Some **small**  
coupling (the time scale  
 $t_U$  depends on process)

To be compared to

$$Y_{F0} \sim \frac{1}{\kappa^2 \times M \times t_U}$$



## A VERY SIMPLE HIDDEN SECTOR

$$\mathcal{L}_{HS} = i\bar{\chi}\not{D}'\chi - m_\chi\bar{\chi}\chi + \dots$$

$\chi$  is a **Dirac fermion**, charged under a **massless** U(1)' gauge field  $B'_\mu$

Stable simply because it is assumed to be the lightest charged particle in the HS \*

\*Feldman, Kors, Nath (06); Pospelov, Ritz, Voloshin (08) Mambrini (10);... Rem: for a massive Z'.

Interaction with the Visible Sector is through the **Kinetic Portal** \*

$$\mathcal{L} \supset -\frac{\epsilon}{2} B^{\mu\nu} B'_{\mu\nu}$$

\* Bob Holdom (86)

## MOTIVATION?

Among the **simplest** models for DM.

Only 3 parameters (4 if  $A'$  is made massive, say, à la Stueckelberg).

$$(m_\chi, e', \epsilon \rightarrow \kappa = \epsilon e' / e)$$

Some very natural features (**stability** from charge conservation, tiny mixing).

Visible Sector = Standard Model Only !

Yet **very rich phenomenology** (both for cosmology and particle physics).

New long range interactions and dark radiation \*

Broad range of DM candidates (from sub-MeV to TeV)

Archetype for many VS-HS structures : 4 regimes for DM creation.

\* Dark Radiation studied in details, but with no mediator, by Ackerman, Buckley, Carroll, Kamionkovski (08); Feng, Kaplinghat, Tu, Yu (09); Feng, Tu, Yu (08); see also Foot *et al* (06-10)

# RELIC DENSITY IN $\kappa$ - $a'$ PLANE

4 regimes:

I. Freeze-in

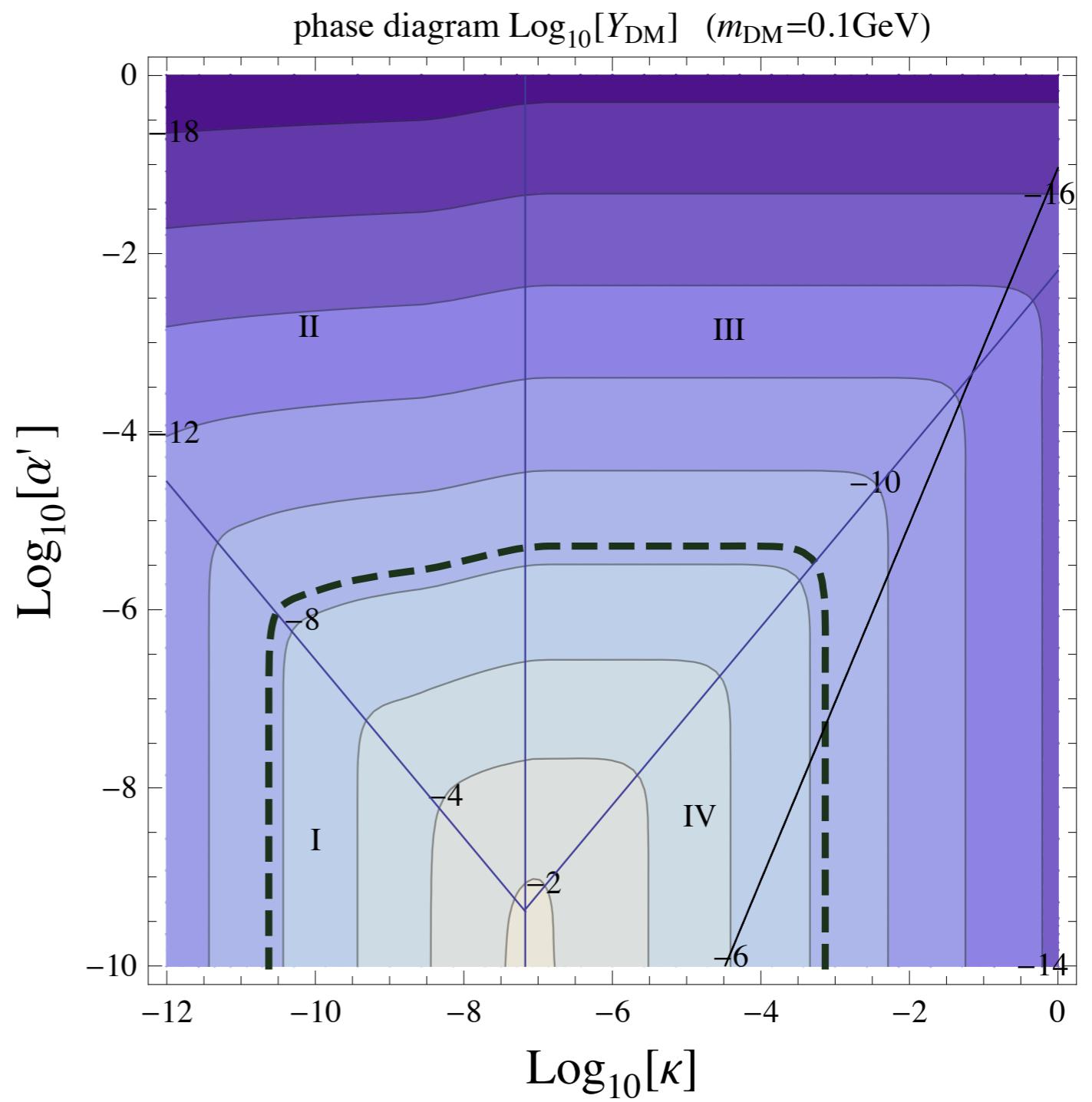
II. Reannihilation

IV. Freeze-out with thermalization of HS

V. Freeze-out without thermalization of HS

In the figure, the levels correspond to  $\Omega_{\text{dm}}$

The dashed line is  $\Omega_{\text{dm}} = 0.23$   
(here for  $m_{\text{dm}} = 100 \text{ MeV}$ )

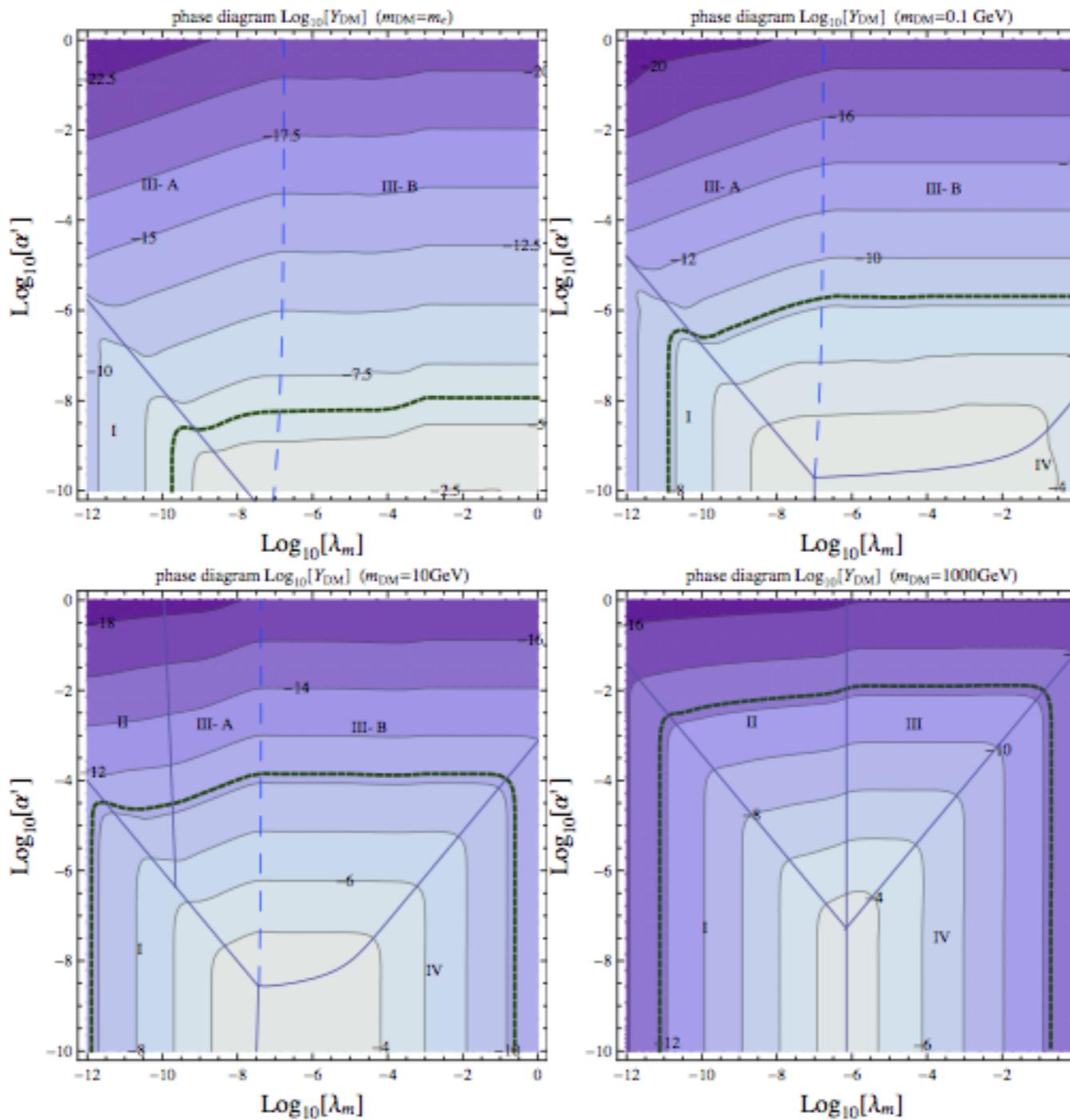




jeudi 18 juillet 2013

# This structure is generic (Here shown for Higgs portal)

$m_{DM} = m_e$



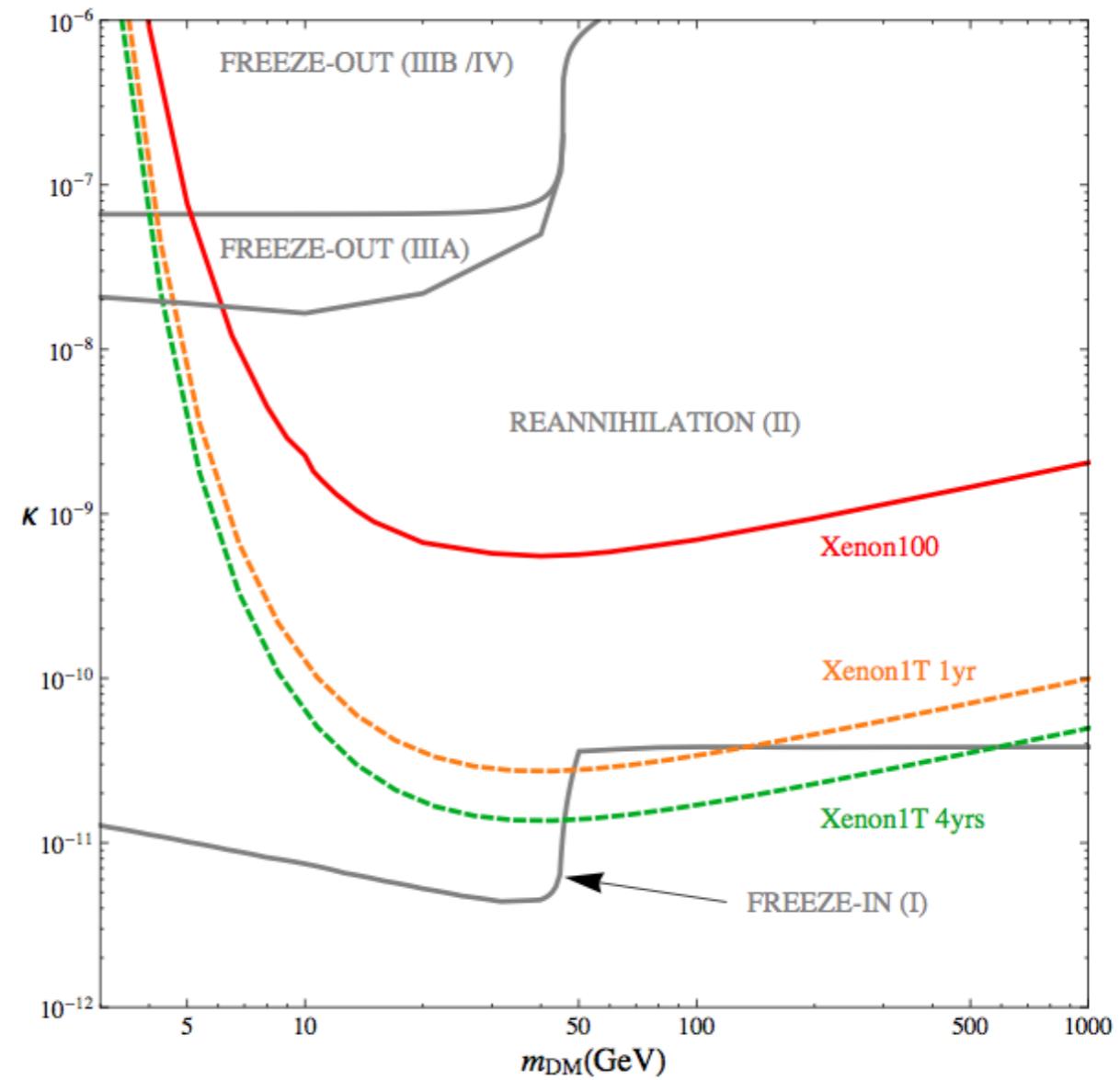
$m_{DM} = 0.1 \text{ GeV}$

$m_{DM} = 10 \text{ GeV}$

$m_{DM} = 1 \text{ TeV}$

# More about Direct Detection (kinetic portal)

Here, we assume that the local abundance (ie at the Sun's location) is 0.3 GeV/cm<sup>3</sup>



FOR  $\langle \sigma v \rangle \sim 3 \cdot 10^{-26} \text{cm}^3 \cdot \text{s}^{-1}$

LET  $\langle \sigma v \rangle \sim \frac{\alpha^2}{M_{DM}^2}$  THEN  $M_{\text{DM}} \sim \text{TeV}$

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GRIEST-KAMIONKOWSKI UNITARITY BOUND:

$$\langle \sigma_{\max} v \rangle \approx \frac{4\pi(2J+1)}{M_{DM}^2 v} \longrightarrow M_{\text{DM}} \lesssim 340 \text{ TeV}$$