

Introduction to Event Generators

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Topics of the lectures

- 1 Lecture 1: *The Monte Carlo Principle*
- 2 Lecture 2: *Parton level event generation*
- 3 Lecture 3: *Dressing the Partons*
- 4 Lecture 4: *Modelling beyond Perturbation Theory & Improving the showers*

Thanks to

- My fellow MC authors, especially S.Gieseke, K.Hamilton, L.Lonnblad, F.Maltoni, M.Mangano, P.Richardson, M.Seymour, T.Sjostrand, B.Webber.
- the other Sherpas: J.Archibald, T.Gleisberg, S.Höche, S.Schumann, F.Siegert, M.Schönherr, and J.Winter.

Menu of lecture 4

- Hadronisation models
- Beyond factorisation: Underlying event
- Improving parton showers with exact matrix elements

Prelude: Orientation

Event generator paradigm

Divide event into stages, separated by different scales.

- **Signal/background:**

Exact matrix elements.

- **QCD-Bremsstrahlung:**

Parton showers (also in *initial state*).

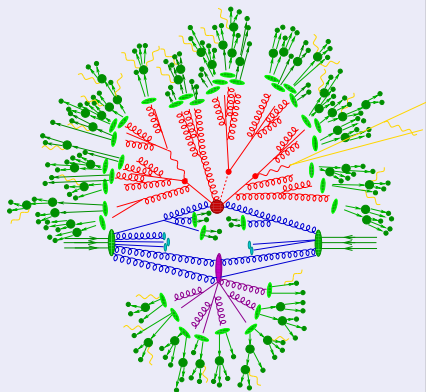
- **Multiple interactions:**

Beyond factorisation: Modelling.

- **Hadronisation:**

Non-perturbative QCD: Modelling.

Sketch of an event

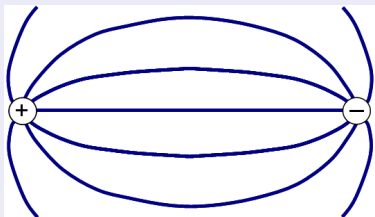


Hadronisation

Confinement

- Consider dipoles in QED and QCD

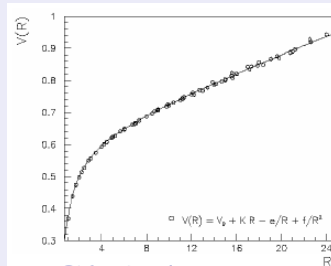
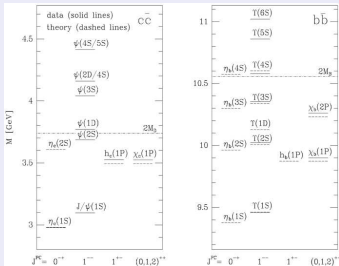
QED:



QCD:

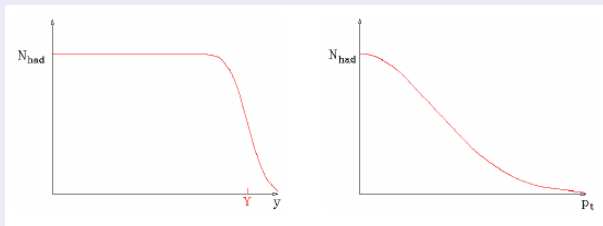


Linear QCD potential in Quarkonia



Some experimental facts $\rightarrow$ naive parameterisations

- In $e^+e^- \rightarrow$ hadrons: Limits $p_\perp$, flat plateau in y .



- Try “smearing”: $\rho(p_\perp^2) \sim \exp(-p_\perp^2/\sigma^2)$

Effect of naive parameterisations

- Use parameterisation to “guesstimate” hadronisation effects:

$$E = \int_0^Y dy dp_\perp^2 \rho(p_\perp^2) p_\perp \cosh y = \lambda \sinh Y$$

$$P = \int_0^Y dy dp_\perp^2 \rho(p_\perp^2) p_\perp \sinh y = \lambda (\cosh Y - 1) \approx E - \lambda$$

$$\lambda = \int dp_\perp^2 \rho(p_\perp^2) p_\perp = \langle p_\perp \rangle .$$

- Estimate $\lambda \sim 1/R_{\text{had}} \approx m_{\text{had}}$, with m_{had} 0.1-1 GeV.
- Effect: Jet acquire non-perturbative mass $\sim 2\lambda E$ ($\mathcal{O}(10\text{GeV})$ for jets with energy $\mathcal{O}(100\text{GeV})$).

Implementation of naive parameterisations

- Feynman-Field independent fragmentation.

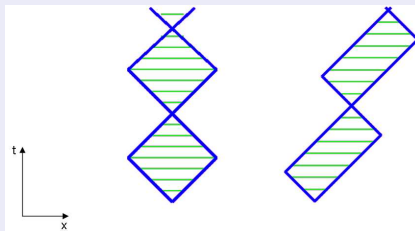
R.D.Field and R.P.Feynman, Nucl. Phys. B **136** (1978) 1

- Recursively fragment $q \rightarrow q' + \text{had}$, where
 - Transverse momentum from (fitted) Gaussian;
 - longitudinal momentum arbitrary (hence from measurements);
 - flavour from symmetry arguments + measurements.
- Problems: frame dependent, “last quark”, infrared safety, no direct link to perturbation theory,

Yoyo-strings as model of mesons

B.Andersson, G.Gustafson, G.Ingelman and T.Sjostrand, Phys. Rept. **97** (1983) 31.

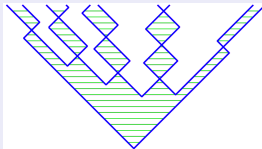
- Light quarks connected by string: area law $m^2 \propto \text{area}$.
- $L=0$ mesons only have 'yo-yo' modes:



Dynamical strings in $e^+e^- \rightarrow q\bar{q}$

B.Andersson, G.Gustafson, G.Ingelman and T.Sjostrand, Phys. Rept. **97** (1983) 31.

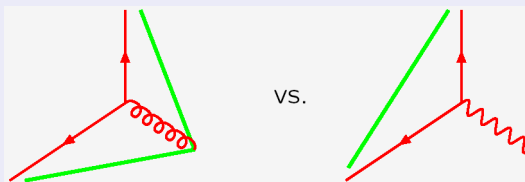
- Ignoring gluon radiation: Point-like source of string.
- Intense chromomagnetic field within string:
More $q\bar{q}$ pairs created by tunnelling.
- Analogy with QED (Schwinger mechanism):
 $d\mathcal{P} \sim dxdt \exp(-\pi m_q^2/\kappa)$, κ = “string tension”.



Gluons in strings = kinks

B.Andersson, G.Gustafson, G.Ingelman and T.Sjostrand, Phys. Rept. **97** (1983) 31.

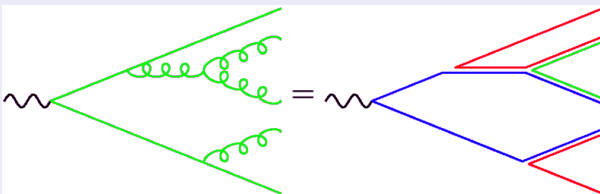
- String model = well motivated model, constraints on fragmentation (Lorentz-invariance, left-right symmetry, ...)
- Gluon = kinks on string? Check by “string-effect”



- Infrared-safe, advantage: smooth matching with PS.

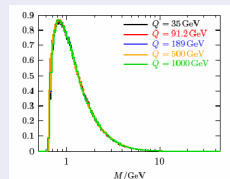
Preconfinement

- Underlying: Large N_c -limit (planar graphs).
- Follows evolution of colour in parton showers:
at the end of shower colour singlets close in phase space.
- Mass of singlets: peaked at low scales $\approx Q_0^2$.



Primordial cluster mass distribution

- Starting point: Preconfinement;
- split gluons into $q\bar{q}$ -pairs;
- adjacent pairs colour connected, form colourless (white) clusters.
- Clusters ($\approx$ excited hadrons) decay into hadrons



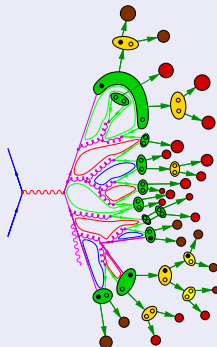
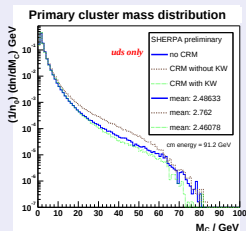
Cluster model

B.R.Webber, Nucl. Phys. B 238 (1984) 492.

- Split gluons into $q\bar{q}$ pairs, form singlet clusters:
 $\implies$ continuum of meson resonances.
- Decay heavy clusters into lighter ones;
(here, many improvements to ensure leading hadron spectrum hard enough, overall effect: cluster model becomes more string-like);
- if light enough, clusters $\rightarrow$ hadrons.
- Naively: spin information washed out, decay determined through phase space only $\rightarrow$ heavy hadrons suppressed (baryon/strangeness suppression).

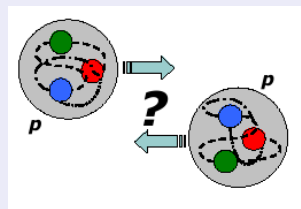
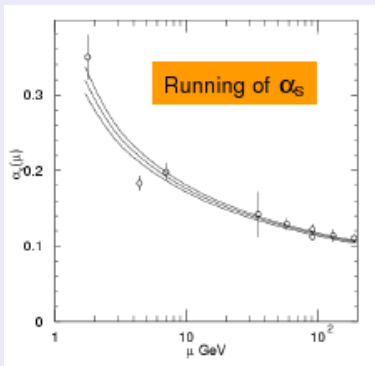
Colour reconnections in the cluster model

- Maybe toy with phenomenological models of non-perturbative colour reconnection?



Underlying Event

Multiple parton scattering?

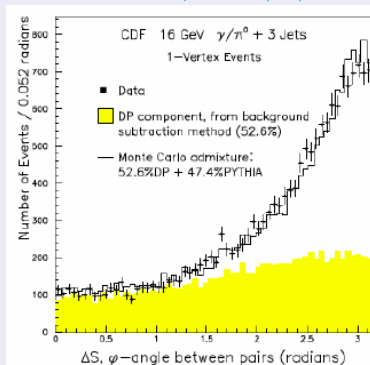


- Hadrons = extended objects!
- No guarantee for one scattering only.
- Running of α_s
⇒ preference for soft scattering.

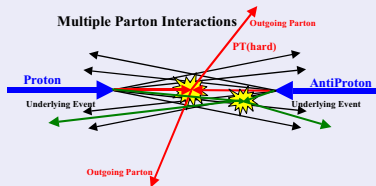
Evidence for multiple parton scattering

- Events with $\gamma + 3$ jets:
 - Cone jets, $R = 0.7$,
 $E_T > 5$ GeV; $|\eta_j| < 1.3$;
 - “clean sample”: two
softest jets with $E_T < 7$
GeV;
- $\sigma_{\text{DPS}} = \frac{\sigma_{\gamma j} \sigma_{jj}}{\sigma_{\text{eff}}}$, $\sigma_{\text{eff}} \approx 14 \pm 4$
mb.

CDF collaboration, Phys. Rev. D56 (1997) 3811.



Definition(s)



- 1 Everything apart from the hard interaction including IS showers, FS showers, remnant hadronisation.
- 2 Remnant-remnant interactions, soft and/or hard.
- 3 Lesson: **hard to define**

Model: Multiple parton interactions

- To understand the origin of MPS, realism that

$$\sigma_{\text{hard}}(p_{\perp,\text{min}}) = \int_{p_{\perp,\text{min}}^2}^{s/4} dp_{\perp}^2 \frac{d\sigma(p_{\perp}^2)}{dp_{\perp}^2} > \sigma_{pp,\text{total}}$$

for low $p_{\perp,\text{min}}$. Here: $\frac{d\sigma(p_{\perp}^2)}{dp_{\perp}^2} = \int_0^1 dx_1 dx_2 d\hat{t} f(x_1, q^2) f(x_2, q^2) \frac{d\hat{\sigma}_{2 \rightarrow 2}}{dp_{\perp}^2} \delta\left(1 - \frac{\hat{t}\hat{u}}{\hat{s}}\right)$
 $(f(x, q^2) = \text{PDF}, \hat{\sigma}_{2 \rightarrow 2} = \text{parton-parton x-sec})$

- $\langle \sigma_{\text{hard}}(p_{\perp,\text{min}}) / \sigma_{pp,\text{total}} \rangle \geq 1$
- Depends strongly on cut-off $p_{\perp,\text{min}}$ (Energy-dependent)!

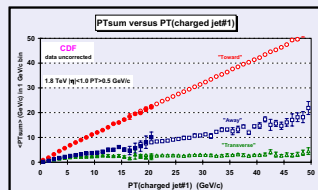
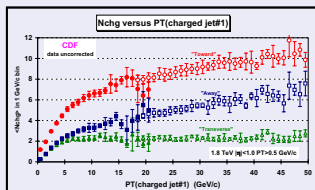
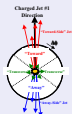
Old Pythia model: Algorithm, simplified

T.Sjostrand and M.van Zijl, Phys. Rev. D **36** (1987) 2019.

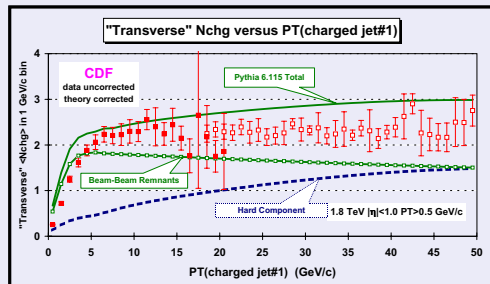
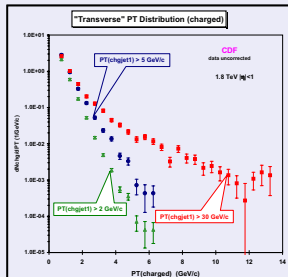
- Start with hard interaction, at scale Q_{hard}^2 .
- Select a new scale $p_{\perp}^2$
(according to $f = \frac{d\sigma_{2\rightarrow 2}(p_{\perp}^2)}{dp_{\perp}^2}$ with $p_{\perp}^2 \in [p_{\perp,\text{min}}^2, Q^2]$)
- Rescale proton momentum ("proton-parton = proton with reduced energy").
- Repeat until below $p_{\perp,\text{min}}^2$.
- May add impact-parameter dependence, showers, etc..
- Treat intrinsic $k_{\perp}$ of partons ($\rightarrow$ parameter)
- Model proton remnants ($\rightarrow$ parameter)

Observables

In the following: Data from CDF, PRD 65 (2002) 092002, plots partially from C.Buttar



Hard component in transverse region



General facts on current models

- No first-principles approach for underlying event:

Multiple-parton interactions: beyond factorisation

Factorisation (simplified) = no process-dependence in use of PDFs.

- Models usually based on xsecs in collinear factorisation:

$$d\sigma/dp_{\perp} \propto p_{\perp}^{4-8} \implies \text{strong dependence on cut-off } p_{\perp}^{\min}.$$

- “Regularisation”: $d\sigma/dp_{\perp} \propto (p_{\perp}^2 + p_0^2)^{2-4}$, also in α_S .

- Model for scaling behaviour of $p_{\perp}^{\min}(s) \propto p_{\perp}^{\min}(s_0)(s/s_0)^{\lambda}$, $\lambda = ?$

Pythia tunes: $\lambda \in [0.160.25]$.

- Herwig model similar to old Pythia and SHERPA

- New Pythia model: Correlate parton interactions with showers, more parameters.

Multijet merging

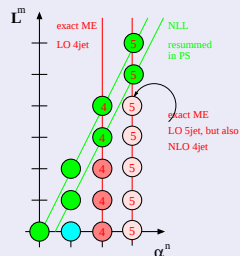
Why multijet merging?

- Parton shower yields approximation to ME
- But: lack of phase space in hadronic collisions typically results in too little QCD activity.

ME vs. PS

- MEs: hard, large-angle emissions; interferences.
- PS: soft, collinear emissions; resummation of large logarithms.
- Combine both, avoid double-counting.
- Right panel: logs in $ee \rightarrow$ jets.

α_s vs. Log



Constructing the algorithm

- Want the best of both - what else?
 - Proper description of soft/collinear and hard emissions
 - Combine QCD matrix elements of different parton multiplicity with showers
- General outline of algorithm:
 - Use LO (tree-level) matrix elements for jet production
 - Could use parton shower kernel $K_{ba}^{ME} \propto |\mathcal{M}_{n+1}|^2 / |\mathcal{M}_n|^2$ hampered by low efficiency for $n \rightarrow \infty$.
 - Idea effectively used in traditional reweighting for small n .
 - Also in generation of hardest emission in POWHEG./
 - Preserve original parton shower evolution equation
(N.B.: this guarantees preservation of log accuracy provided by shower)
 - Avoid double-counting (positive or negative)
Must slice the phase space: Jet production vs. jet evolution
 $\Rightarrow$ adds a parameter - the jet resolution criterion Q_{cut}
(but inclusive results should better not depend too strongly on this parameter)

Slicing the phase space

- Decompose splitting kernels of parton showers as $K_{ba}(z, t) = K_{ba}(z, t)\Theta[Q_{\text{cut}} - Q_{ba}(z, t)] + K_{ba}(z, t)\Theta[Q_{ba}(z, t) - Q_{\text{cut}}]$.
- In **hard** region, call $K_{ba}\Theta[Q_{ba}(z, t) - Q_{\text{cut}}] \rightarrow K_{ba}^{ME}$,
- Call $K_{ba}\Theta[Q_{\text{cut}} - Q_{ba}(z, t)] \rightarrow K_{ba}^{PS}$ in **soft** region.
- Sudakov form factor factorises (exponential):

$$\Delta_a(\mu^2, t) = \Delta_a^{PS}(\mu^2, t)\Delta_a^{ME}(\mu^2, t)$$

Also, no emission probability can be rewritten:

$$\mathcal{P}_a^{\text{no}}(z, t, \bar{t}) = \frac{\Delta_a^{PS}(\mu^2, \bar{t})}{\Delta_a^{PS}(\mu^2, t)} \frac{\Delta_a^{ME}(\mu^2, \bar{t})}{\Delta_a^{ME}(\mu^2, t)} \frac{g_a(z, t)}{g_a(z, \bar{t})}$$

- In shower, need to veto emissions with $Q_{ba} > Q_{\text{cut}}$.
But: maybe emissions at $Q < Q_{\text{cut}}$ but t larger than those in ME:
must cure “mismatch” of shower and jet measure

→ **truncated showers**

Defining PS histories

- Identify most likely splitting acc. to PS branching probability
- Combine partons into mother parton acc. to inverse PS kinematics
- Continue until $2 \rightarrow 2$ core process

$\rightsquigarrow$ shower specific cluster algorithm

$\rightsquigarrow$ predetermined shower emissions

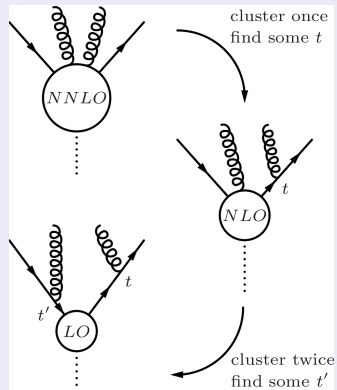
PS starts at core process

can radiate “between” ME emissions

ME branchings must be respected
evolution-, splitting- & angular variable preserved

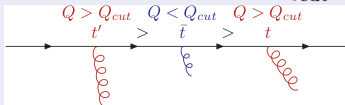
$\rightsquigarrow$ truncated shower

Example branching history

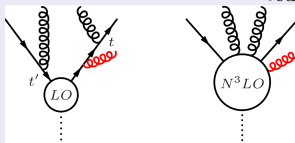


Truncated shower

Shower emission below Q_{cut} :



Shower emission above Q_{cut} :



$\rightsquigarrow$ emission accepted

$\rightsquigarrow$ large-angle soft emissions

$\rightsquigarrow$ soft color coherence

$\rightsquigarrow$ approx. in CKKW only

$\rightsquigarrow$ entire event is rejected

$\rightsquigarrow$ Sudakov suppression

$\mathcal{P}_{\text{no}, a}^{\text{ME}}(t, t')$

$\rightsquigarrow$ to be described by ME instead

$\rightsquigarrow$ σ_{tot} preserved at LO

Implementations

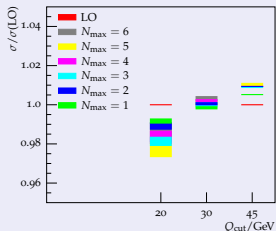
- Available implementations of this method in SHERPA & HERWIG++.
- MLM method for ALPGEN, MADGRAPH etc. (misses some terms)

Z^0 +jets at Tevatron: Total cross sections

Q_{cut} and/or N_{max} variation should affect σ_{tot} only beyond (N)LL

- Example: DY-pair production σ_{tot} @ Tevatron

		N_{max}						
		0	1	2	3	4	5	6
Q_{cut}	20 GeV	192.6(1)	191.0(3)	190.5(4)	189.0(5)	189.4(7)	188.2(8)	189.9(10)
	30 GeV		192.3(2)	192.7(2)	192.6(3)	192.9(3)	192.7(3)	193.2(3)
	45 GeV		193.6(1)	194.4(1)	194.3(1)	194.4(1)	194.6(2)	194.4(1)



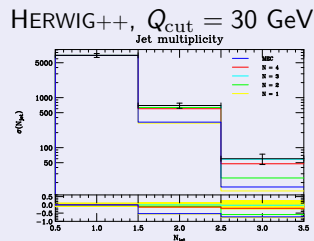
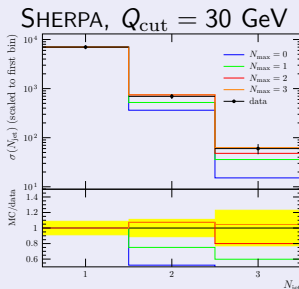
- improved “merging systematics” of $\sigma_{\text{tot}} < \pm 3\%$

Z^0 +jets at Tevatron: jet multiplicities

Jet rates and -spectra improved compared to pure PS simulation

- Example: DY-pair production $\sigma_{e^+e^-+N_{\text{jet}}}$

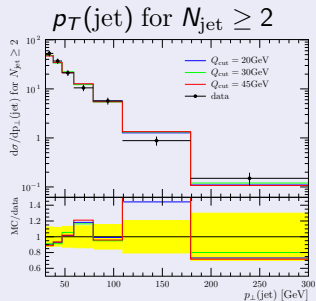
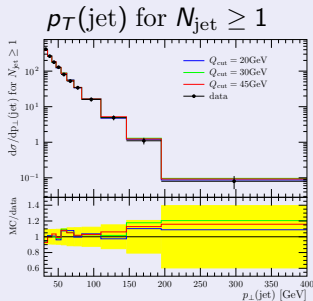
CDF Data: PRL 100 (2008) 102001



Z^0 +jets at Tevatron: jet spectra

- Example: All-jets p_T 's in DY-pair production
- Compare with results from SHERPA

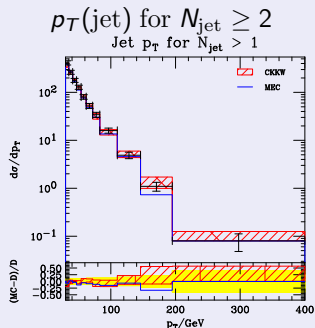
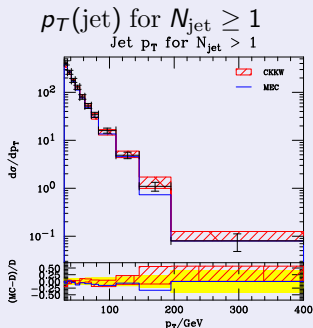
CDF Data: PRL 100 (2008) 102001



Z^0 +jets at Tevatron: jet spectra

- Example: All-jets p_T 's in DY-pair production
- Compare with results from HERWIG++

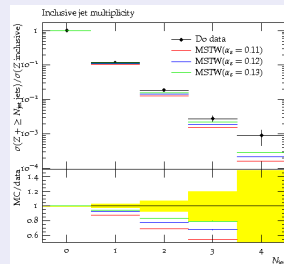
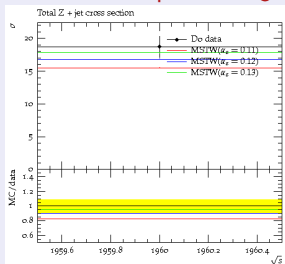
CDF Data: PRL 100 (2008) 102001



Z^0 +jets at Tevatron: cross sections

CDF data from PRL 100 (2008) 102001 and D0/, arXiv:0808.1296

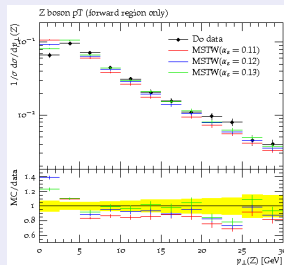
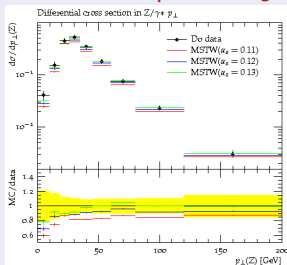
Impact of α_S - global in SHERPA



Z^0 +jets at Tevatron: Z/γ^* transverse momentum

DØ data: PRL 100 (2008) 102002

Impact of α_S - global in SHERPA



A new Monte Carlo approach for Prompt-Photon Production

(S.Höche, S.Schumann, F.Siebert PRD **81** (2010) 034026)

- treat photons and QCD partons fully democratically

(Glover, Morgan Z. Phys. C **62** (1994) 311)

- combine matrix elements of different parton/photon multiplicity with
- QCD $\oplus$ QED evolution and hadronisation $\rightsquigarrow$ models $D_{q,g}^\gamma(z, Q^2)$

Generalised merging formalism

- Emission probabilities factorise trivially as before

$$\Delta_a(Q_0^2, Q^2) = \Delta_a^{(\text{QCD})}(Q_0^2, Q^2) \Delta_a^{(\text{QED})}(Q_0^2, Q^2)$$

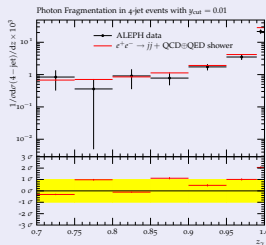
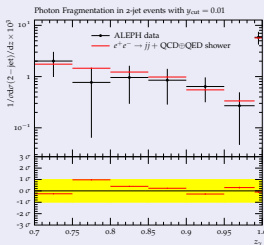
- Implemented by adding splitting functions $q \rightarrow q\gamma$
- Different then large- N_C QCD: spectators *all* particles with opposite charge
- Neglect (negative) interference with same-sign charges

(S.Dittmaier, Nucl. Phys. B **565** (2000) 69)

Results: photon fragmentation function in $e^+e^- \rightarrow \text{Hadrons}$

(Aleph data from Z. Phys. C **69** (1996) 365)

- Validation of the shower/hadronisation component
- Perform jet finding including final-state photons
- Study photon-energy fraction wrt its containing jet: $z_\gamma \equiv E_\gamma/E_{\text{jet}}$



Isolated prompt-photon production at Tevatron

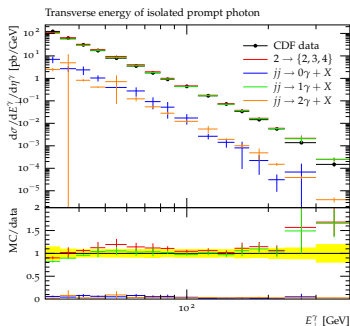
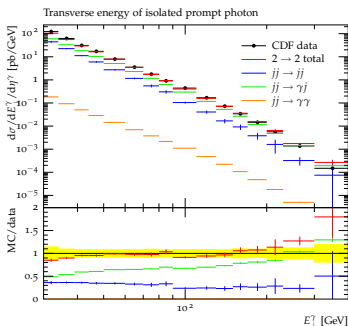
(Data from CDF, Phys. Rev. D **80** (2009) 111106)

cuts: $30 < E_T^\gamma < 400$ GeV, $|\eta^\gamma| < 1$, isolation: $E_T^{R=0.4} - E_T^\gamma < 2$ GeV

- Sherpa: pure shower vs. ME $\oplus$ TS

E_T^γ – pure shower

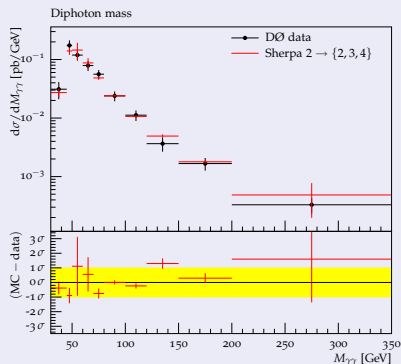
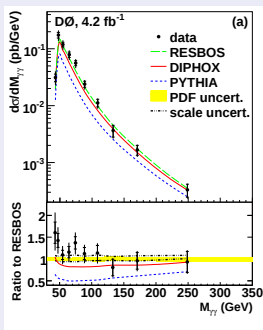
E_T^γ – ME $\oplus$ TS



$\gamma\gamma$ production at Tevatron: Invariant mass

(DØ/ data, arXiv:1002.4917)

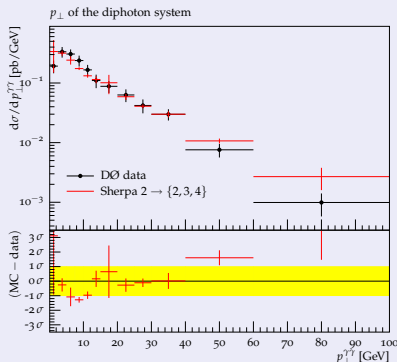
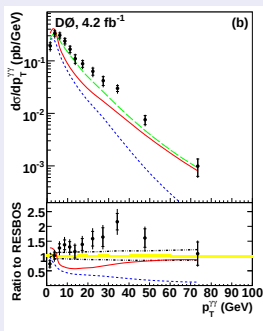
- Compare with other codes: **DiPhox**, **ResBos**, **Pythia**
- Sherpa: merged $2 \rightarrow \{2, 3, 4\}$ plus $gg \rightarrow \gamma\gamma$ box



$\gamma\gamma$ production at Tevatron: Transverse momentum of pair

(D0/ data, arXiv:1002.4917)

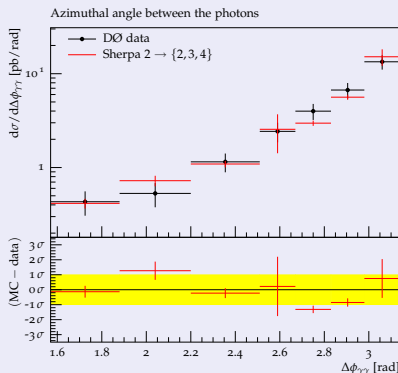
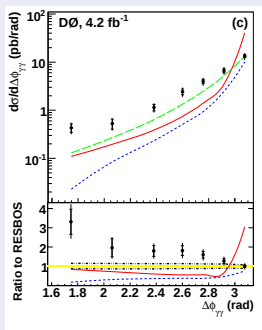
- Compare with other codes: **DiPhox**, **ResBos**, **Pythia**
- Sherpa: merged $2 \rightarrow \{2, 3, 4\}$ plus $gg \rightarrow \gamma\gamma$ box



$\gamma\gamma$ production at Tevatron: Azimuthal decorrelation

(DØ/ data, arXiv:1002.4917)

- Compare with other codes: **DiPhox**, **ResBos**, **Pythia**
- Sherpa: merged $2 \rightarrow \{2, 3, 4\}$ plus $gg \rightarrow \gamma\gamma$ box



The POWHEG method

Basic idea

- Want total cross section and first emission correct at $\mathcal{O}(\alpha_S)$
- Master formula:

$$d\sigma_{\text{NLO}} = d\Phi_{\mathcal{B}} \bar{\mathcal{B}}(\Phi_{\mathcal{B}}) \left[\bar{\Delta}(p_{\perp, \min}) + \int_{p_{\perp, \min}} d\Phi_{\mathcal{R}|\mathcal{B}} \frac{\mathcal{R}(\Phi_{\mathcal{R}})}{\mathcal{B}(\Phi_{\mathcal{R}})} \bar{\Delta}(p_{\perp}) \right].$$

- $\mathcal{B}$, $\mathcal{R}$ denote Born and real emission ME, with phase space $\Phi_{\mathcal{B}, \mathcal{R}}$.
- $\Phi_{\mathcal{R}|\mathcal{B}}$ is the phase space for one particle splitting connecting both.
- Since Sudakov form factor $\bar{\Delta}$ reads:

$$\bar{\Delta}(p_{\perp}) = \exp \left[- \int d\Phi_{\mathcal{R}|\mathcal{B}} \Theta[k_{\perp}(\Phi_{\mathcal{R}}) - p_{\perp}] \frac{\mathcal{R}(\Phi_{\mathcal{R}})}{\mathcal{B}(\Phi_{\mathcal{R}})} \right],$$

the expression in square bracket above = 1 (unitarity).

- $\bar{\mathcal{B}}(\Phi_{\mathcal{B}})$ denotes the NLO-weighted differential xsec for Born config..

Algorithm

- Generate a starting Born-type parton configuration distributed according to

$$d\Phi_B \bar{\mathcal{B}}(\Phi_B) = d\Phi_B [\mathcal{B}(\Phi_B) + \mathcal{V}(\Phi_B) + \int d\Phi_{\mathcal{R}|\mathcal{B}} \mathcal{R}(\Phi_{\mathcal{R}})]$$

with $\mathcal{B}$ the **Born**, $\mathcal{V}$ the **virtual**, and $\mathcal{R}$ the **real emission** contribution.

- Generate the hardest emission according to $\bar{\Delta}$, where the usual splitting kernel $\mathcal{K}(t, z)$ is replaced by the ratio $\mathcal{R}(\Phi_{\mathcal{R}})/\mathcal{B}(\Phi_B)$:

$$\frac{dt}{t} dz \mathcal{K}(t, z) \rightarrow d\Phi_{\mathcal{R}|\mathcal{B}}(t, z) \frac{\mathcal{R}(\Phi_{\mathcal{R}})}{\mathcal{B}(\Phi_B)}$$

- Perform **truncated shower** on resulting parton configuration.
- Three publicly available implementations:
HERWIG++, POWHEGBOX, and SHERPA
- The POWHEGBOX implementation “sits” on top of arbitrary parton shower through LHE-Interface, harms truncating the shower.

Available processes/implementations in SM

Process	POWHEGBoX	HERWIG++	SHERPA
$e^+e^- \rightarrow jj$	✗	✓	✓
DIS	✗	in prep.	✓
$pp \rightarrow W/Z$	✓	✓	✓
$pp \rightarrow H$ (gluon fusion)	✓	✓	✓
$pp \rightarrow V + H$	✗	✓	✓
$pp \rightarrow VV$	✗	✓	✓
VBF	✓	in prep.	in prep.
$pp \rightarrow Q\bar{Q}$	✓	✗	✗
$pp \rightarrow Q\bar{Q} + j$	in prep.	✗	✗
single-top	✓	✗	✗
$pp \rightarrow V + j$	✓	✗	in prep.
$pp \rightarrow V + jj$	in prep.	✗	in prep.
$pp \rightarrow H + j$ (gluon fusion)	✗	✗	in prep.
$pp \rightarrow H + jj$ (gluon fusion)	✗	✗	in prep.
$pp \rightarrow V + b\bar{b}$	in prep.	✗	in prep.
dijets	✓	✗	in prep.
$pp \rightarrow W^+W^+jj$	✓	✗	✗

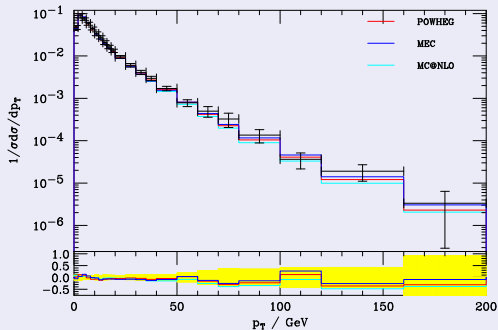
(SHERPA benefits from ME-generator plus subtraction terms - makes implementations fairly automatic . . .)

W +jets at Tevatron: $p_{\perp}^W$ -spectra

- POWHEG method as implemented in HERWIG++ vs. MC@NLO and HERWIG++.

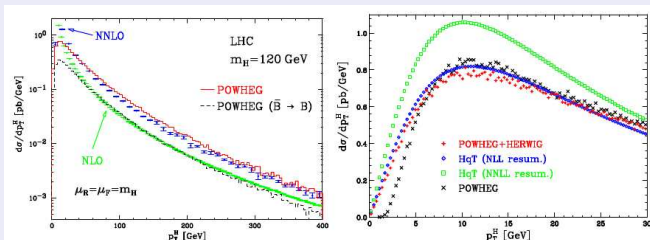
(Note: when only shape considered, do not expect difference to native HERWIG++ with ME corrections included)

⇒ simple check of implementation.)



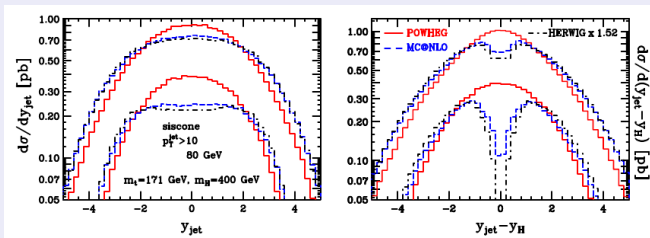
H +jets at LHC: Implicit higher orders in POWHEG

- Can replace $\bar{B} \rightarrow B$ in $d\sigma$ to check if huge K -factor of $\mathcal{O}(2)$ is just due to proper NLO correction (left panel): expect only a vertical shift.
- Can also check for shape w.r.t. higher-order code and switch on/off shower & hadronisation effects (right panel)



H +jets at LHC: Implicit higher orders in POWHEG

- Cross check with MC@NLO (similar goal, different algorithm).
- Problem in MC@NLO becomes apparent: resides on HERWIG-shower, which does not have full phase space coverage - interplay of positive and negative weights with this partial phase space filling produces dips.
- That's why I like POWHEG better - and it's easier to implement.



The MENLOPS method

Basic idea

- At present:
 - can merge “arbitrary” tree-level MEs with PS
 - Several automated codes on the market
 - Automation of 1-loop QCD corrections seems feasible (automated codes now emerging)
- We should make use of both and automate $\text{ME} \otimes \text{PS}$ at 1-loop
- Strategy: Use whatever is available
 - Process NLO parton-level events with PS at low multiplicities (through MC@NLO or, preferably, POWHEG method)
 - Combine NLO simulation with higher-order tree-level using standard $\text{ME} \otimes \text{PS}$ technique for high multiplicities
- First step: POWHEG for lowest multiplicity only.

Some theoretical considerations

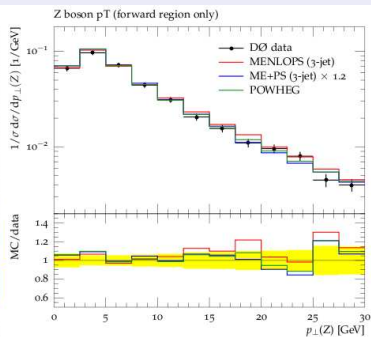
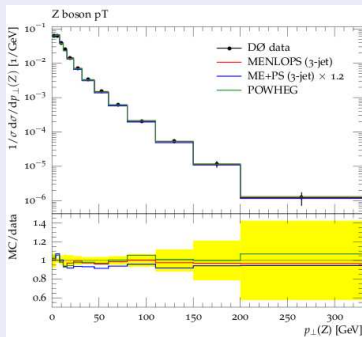
- Compare $\sigma_{(\text{NLO})}$ for POWHEG and $\text{ME} \otimes \text{PS}$:

$$\begin{aligned}
 d\sigma_{\text{NLO}}^{(\text{POW})} &= \\
 d\Phi_{\mathcal{B}} \bar{\mathcal{B}}(\Phi_{\mathcal{B}}) &\left[\bar{\Delta}(p_{\perp, \min}) + \int_{p_{\perp, \min}} d\Phi_{\mathcal{R}|\mathcal{B}} \frac{\mathcal{R}(\Phi_{\mathcal{R}})}{\mathcal{B}(\Phi_{\mathcal{R}})} \bar{\Delta}(p_{\perp}) \right] ; \\
 d\sigma_{\text{NLO}}^{(\text{MEPS})} &= \\
 d\Phi_{\mathcal{B}} \mathcal{B}(\Phi_{\mathcal{B}}) &\left[\Delta(p_{\perp, \min}) + \int_{p_{\perp, \min}} d\tilde{\Phi}_{\mathcal{R}|\mathcal{B}} \frac{\mathcal{R}(\Phi_{\mathcal{R}})}{\mathcal{B}(\Phi_{\mathcal{R}})} \Delta(p_{\perp}) \right] .
 \end{aligned}$$

- Nearly the same. Most notably: NLO vs. LO normalisation.
Boils down to a local K factor $= \bar{\mathcal{B}} / \mathcal{B}$
- Also note: different Sudakovs, in $\text{ME} \otimes \text{PS}$ [...] does not integrate to one.
Reason: Kernel in Sudakov Δ differs from $\mathcal{R}/\mathcal{B}$.

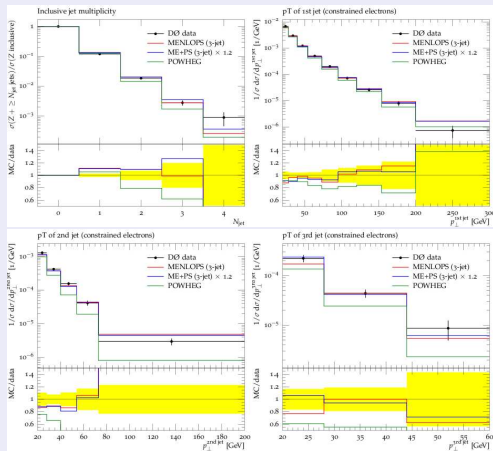
Drell-Yan production at Tevatron

Data from D0, comparison in S.Hoeche et al., arXiv:1009.1127



Drell-Yan production at Tevatron

Data from D0, comparison in S.Hoeche et al., arXiv:1009.1127



Summary of lecture 4

- Hadronisation

- Various phenomenological models;
- tuned to LEP data, overall agreement satisfying;
- validity for hadron data not quite clear.

(beam remnant fragmentation not in LEP.)

- Underlying event

- Theoretically not understood;
- models typically based on collinear factorisation and semi-independent multi-parton scattering;
- models highly parameter-dependent, leading to large differences in predictions;
- even unclear: good observables to distinguish models.