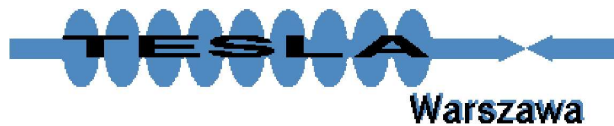


# Determination of the basic Higgs-boson couplings from combined analysis of $WW/ZZ$ decays at LHC, ILC and Photon Collider

A.F. Żarnecki, Warsaw University



with P. Nieżurawski and M. Krawczyk

NŻK

LHC / LC Study Group meeting  
SLAC, March 23, 2005

## Outline

- Higgs couplings in 2HDM (II)
- Higgs production at LHC, ILC, and PLC
- Combined analysis
- 2HDM (II) with CP violation

# CP conserving 2HDM (II)

## Higgs boson couplings

Scalar Higgs bosons  $h$  and  $H$   
with basic couplings (relative to SM):

$$\chi_x = g_{\mathcal{H}xx}/g_{\mathcal{H}xx}^{SM} \quad \mathcal{H} = h, H, A$$

	$h$	$H$	$A$
$\chi_u$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$-i \gamma_5 \frac{1}{\tan \beta}$
$\chi_d$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$-i \gamma_5 \tan \beta$
$\chi_V$	$\sin(\beta - \alpha)$	$\cos(\beta - \alpha)$	0

For charged Higgs boson couplings  
(loop contribution to  $\Gamma_{\gamma\gamma}$ ) we set

$$M_{H^\pm} = 800 \text{ GeV} \quad \mu = 0$$

Higgs couplings are related by  
“patter relation”

$$(\chi_V - \chi_d)(\chi_u - \chi_V) + \chi_V^2 = 1$$

I. F. Ginzburg, M. Krawczyk and P. Osland,  
hep-ph/0101331

Instead of angles  $\alpha$  and  $\beta$  use couplings  
 $\chi_V$  and  $\chi_u$  to parametrize cross sections

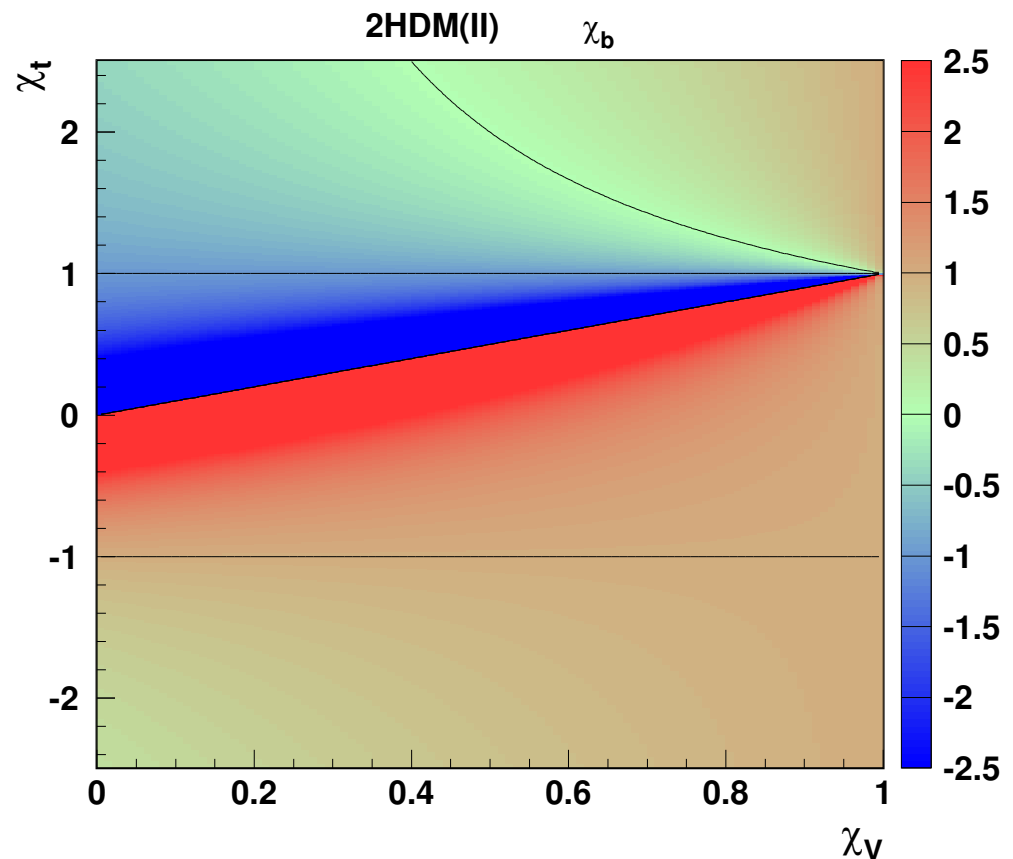
$$0 \leq \chi_V \leq 1$$

If we neglect  $H$  decays to  $h$  and  $A$   
(small) cross sections and BRs calculated for  $H$  are also valid for  $h$

## 2HDM (II)

Basic relative coupling to **down-type** fermions as a function of **vector boson** and **top** (up-type fermions) couplings:

$$\chi_d = \chi_V + \frac{1 - \chi_V^2}{\chi_V - \chi_u}$$

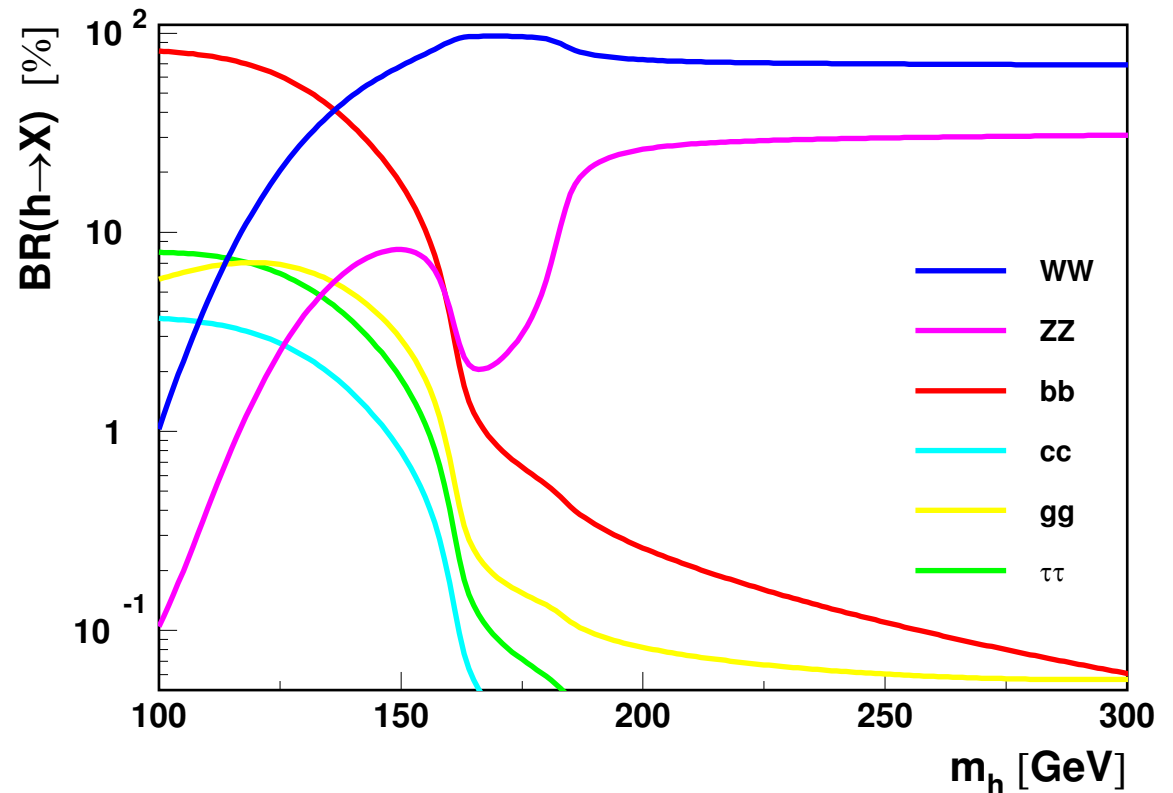


## 2HDM (II)

Higgs boson production at LHC, ILC and PLC, for Higgs boson mass between 200 and 350 GeV

For **SM-like scenarios** ( $\chi \sim 1$ ) Higgs boson decays to  $WW$  and  $ZZ$  dominate.

SM branching ratios



# LHC

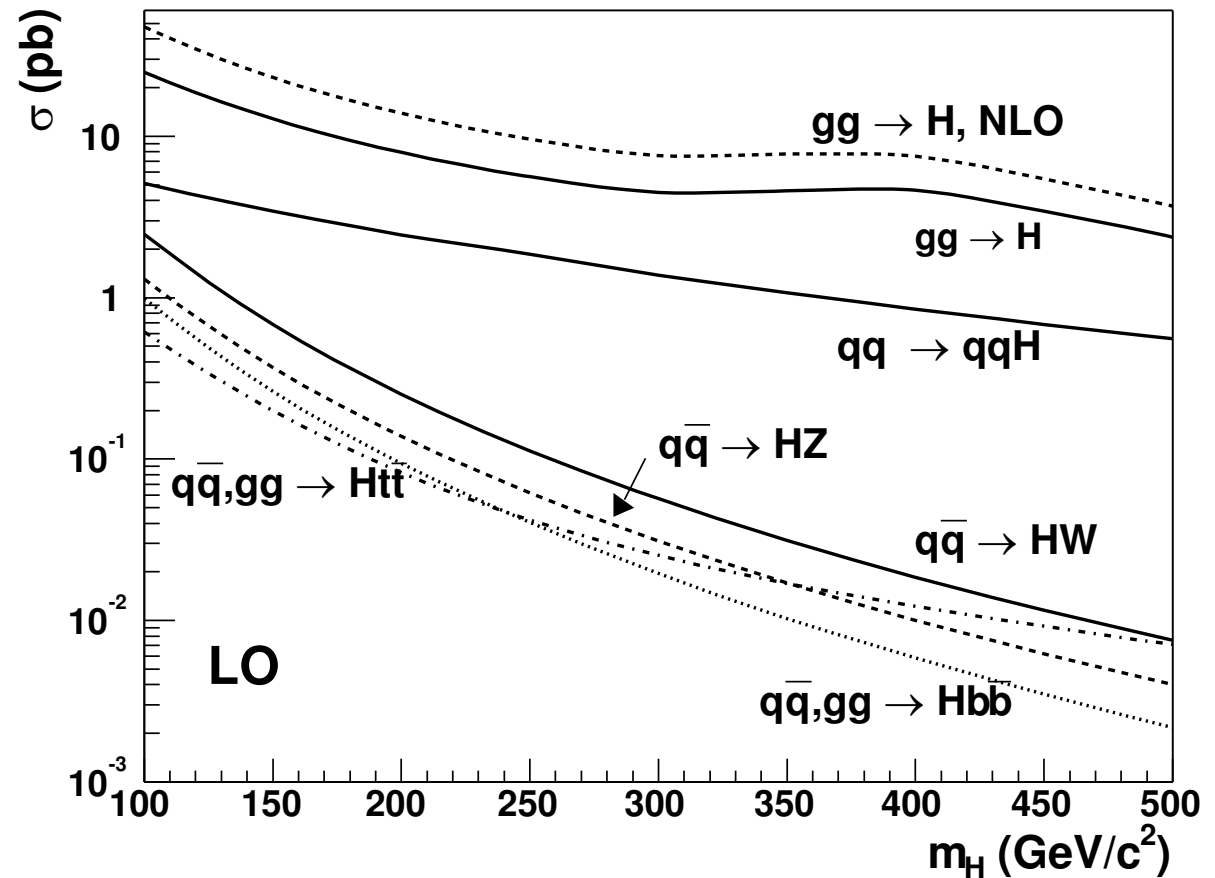
In the considered mass range Higgs boson production at LHC is dominated by the **gluon fusion** process.

$\Gamma_{hgg}$  is dominated by the **top loop** contribution  $\Rightarrow$

$$\sigma(gg \rightarrow h) \sim \chi_t^2$$

**WW fusion** process contributes to about 15% of cross section

$$\sigma(qq \rightarrow qqh) \sim \chi_V^2$$



SM Higgs boson production at LHC

LHC

Measurement of the production cross section times branching ratio

$$\sigma(pp \rightarrow hX) \cdot BR(h \rightarrow ZZ \rightarrow 4l)$$

“golden channel”

will constrain mainly the  $|\chi_u|$  value, provided  $\chi_V$  is not too small.

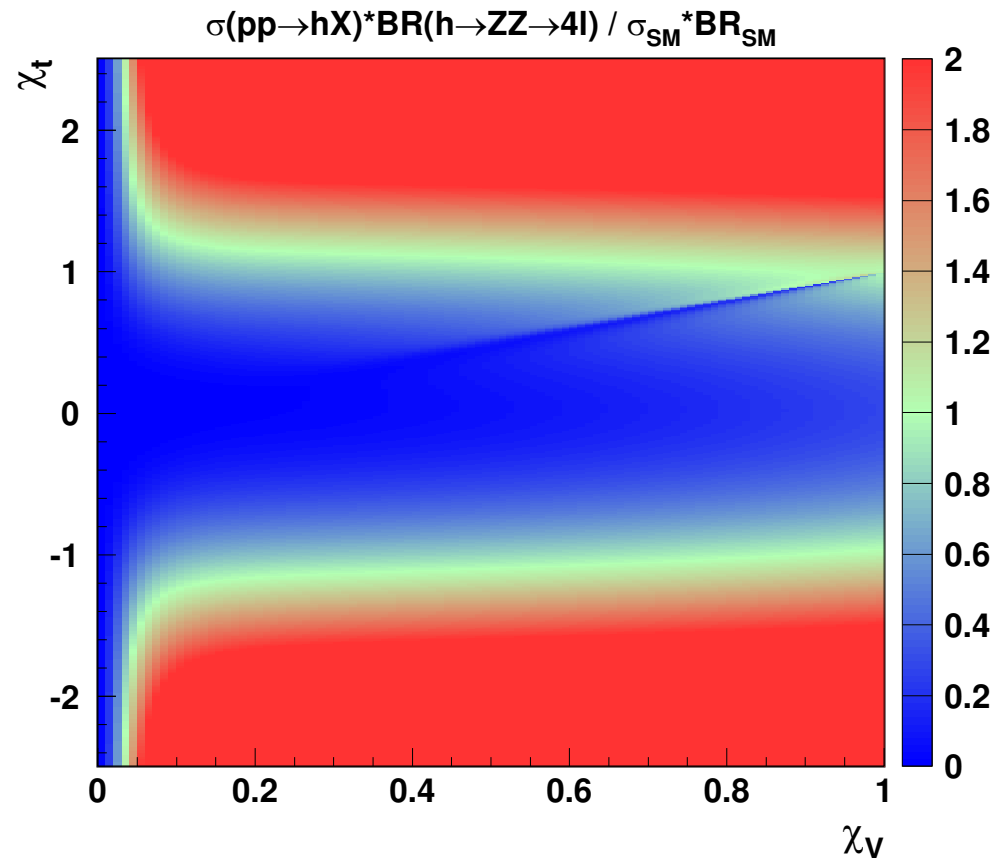
We use results of

C.P.Buszello, I.Fleck, P.Marquard, J.J. van der Bij, Eur. Phys. J. C32(2004)209

hep-ph/0212396

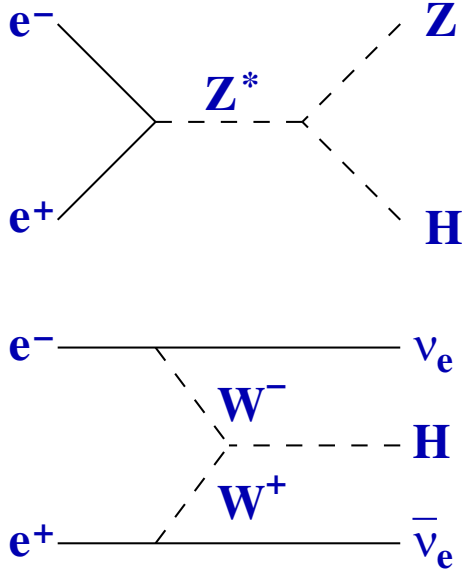
Precision  $\sim 15\%$  expected

Cross section relative to SM



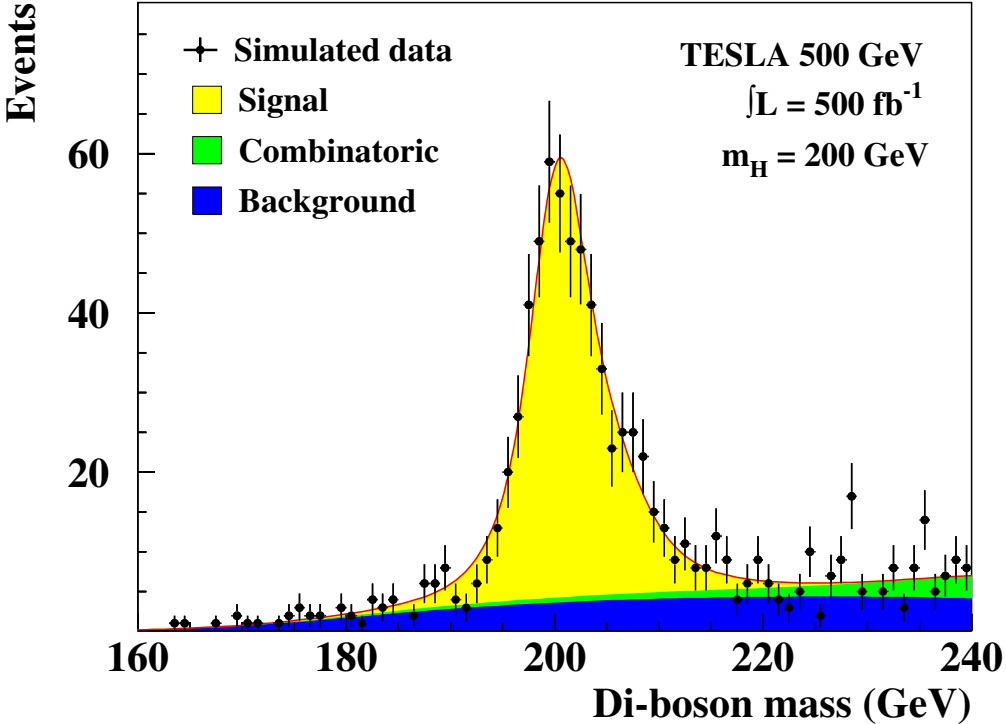
# ILC

For Higgs boson production at TESLA  
 ( $\sqrt{s} = 500 \text{ GeV}, 500 \text{ fb}^{-1}$ )  
 two processes are considered



Production is sensitive only to  $\chi_V$

Expected mass distribution (SM)



N.Meyer, Eur. Phys. J. C35 (2004) 171  
[hep-ph/0308142](https://arxiv.org/abs/hep-ph/0308142)

# ILC

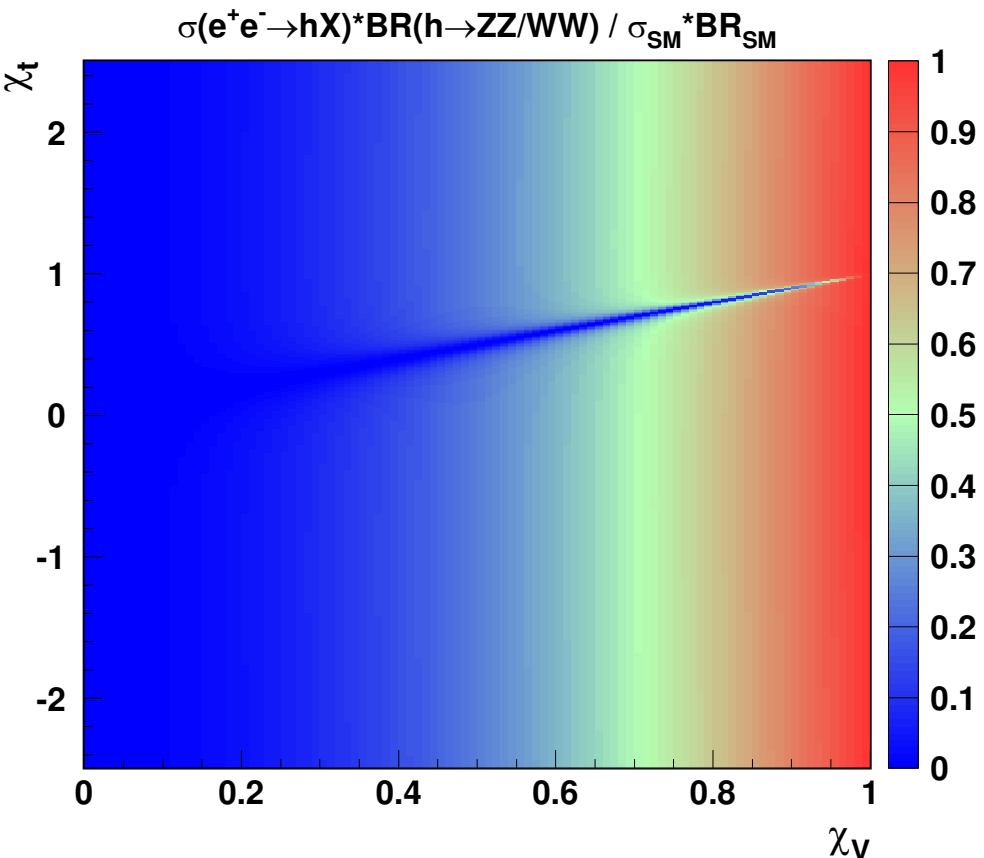
Measurement of the production cross section times branching ratio

$$\sigma(e^+e^- \rightarrow hX) \cdot BR(h \rightarrow WW/ZZ)$$

is possible with precision  $\sim 4 - 7\%$   
(SM-like scenario,  $500 \text{ fb}^{-1}$ )

This will constrain the  $\chi_V$  value

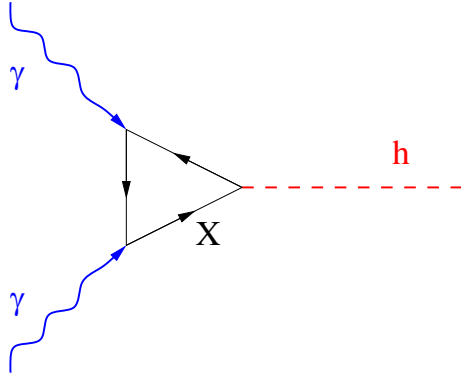
## Cross section relative to SM





# PLC

Cross section for the Higgs boson production at the **Photon Collider** is proportional to the **two-photon width**



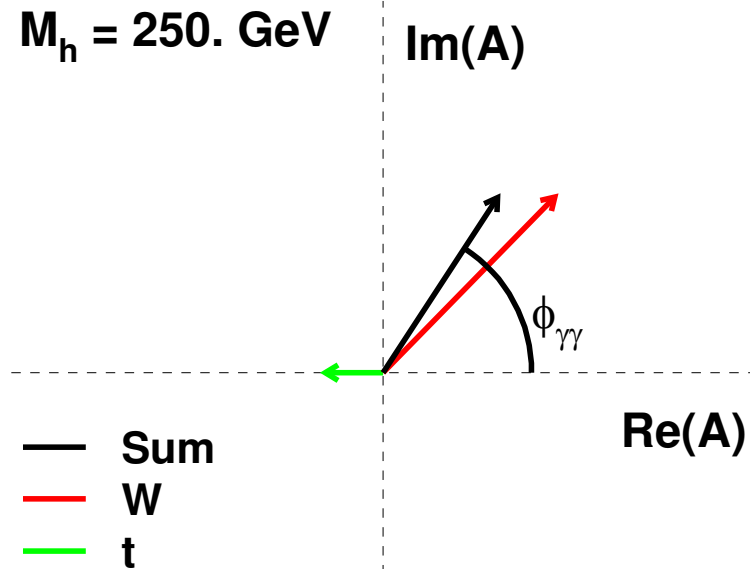
$$\Gamma(h \rightarrow \gamma\gamma) = \frac{G_F \alpha^2 M_h^3}{128 \sqrt{2} \pi^3} \cdot |\mathcal{A}|^2$$

where:

$$\mathcal{A} = A_W(M_W) + \sum_f N_c Q_f^2 A_f(M_f) + \dots$$

two-photon amplitude

In SM, dominant contributions to two-photon amplitude  $\mathcal{A}$  are due to  $W^\pm$  and **top** loops.

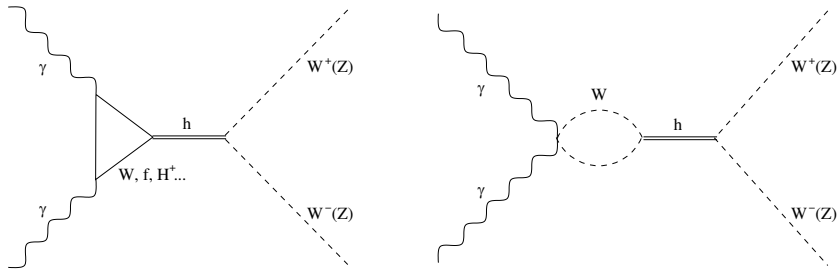


Phases of  $W^\pm$  and **top** contributions differ  
Phase of top distribution changes with  $\Phi_{HA}$  !

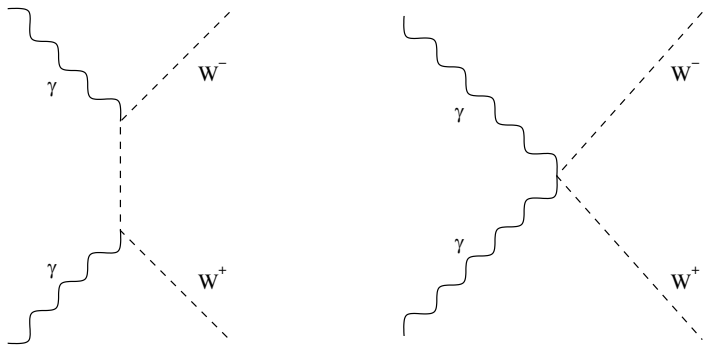
$\Rightarrow$  Both  $\Gamma_{\gamma\gamma}$  and the phase of the amplitude  $\phi_{\gamma\gamma}$  depend on  $\chi_V$  and  $\chi_t$

# PLC

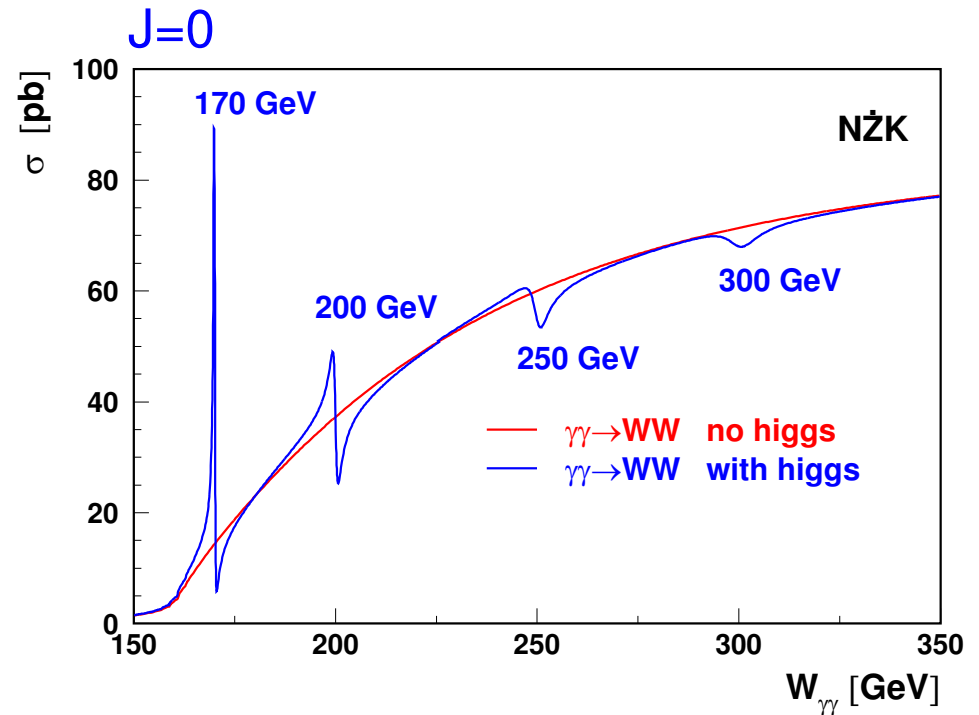
For **resonant**  $\gamma\gamma \rightarrow h \rightarrow W^+W^-$  signal



there is a large **non-resonant** bg.



Large **interference** effects are expected in the considered mass range



Interference is sensitive to the phase of the two-gamma amplitude

# PLC

Measurement of the production cross section times branching ratio

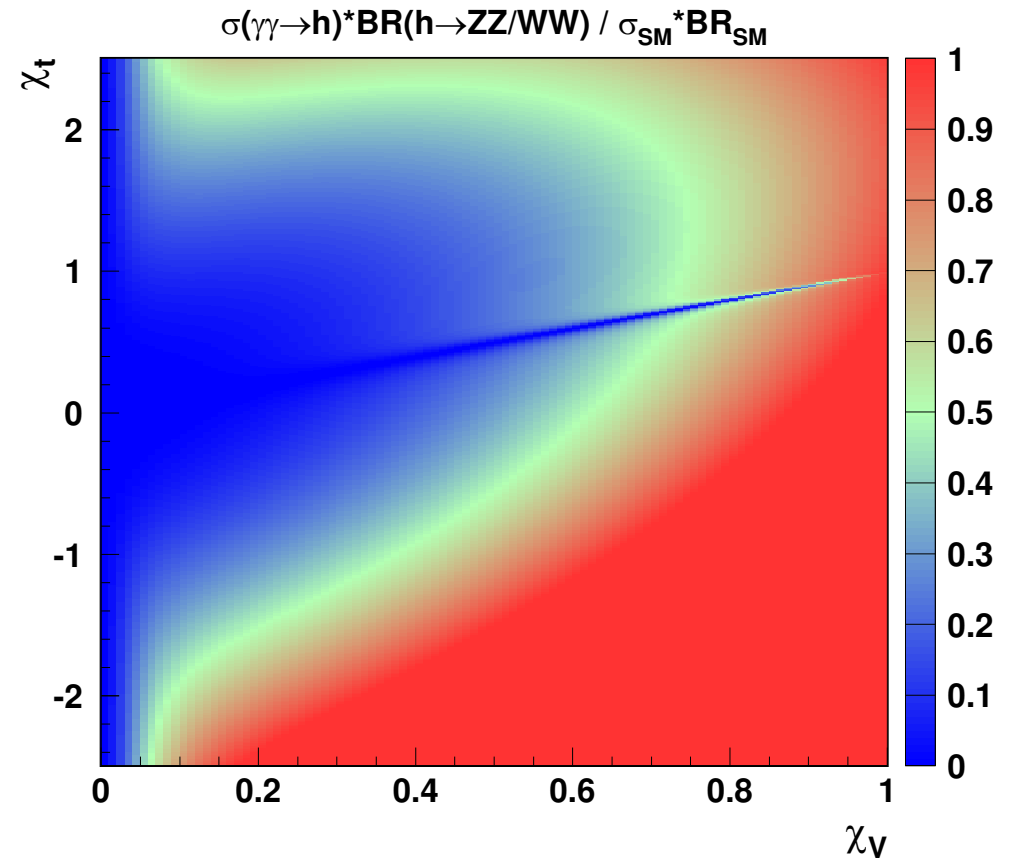
$$\sigma(\gamma\gamma \rightarrow h) \cdot BR(h \rightarrow WW/ZZ)$$

is possible with precision  $\sim 4 - 9\%$

$\phi_{\gamma\gamma}$  can be measured with precision  
40 – 120 mrad

JHEP 0211 (2002) 034 [hep-ph/0207294]

Cross section relative to SM

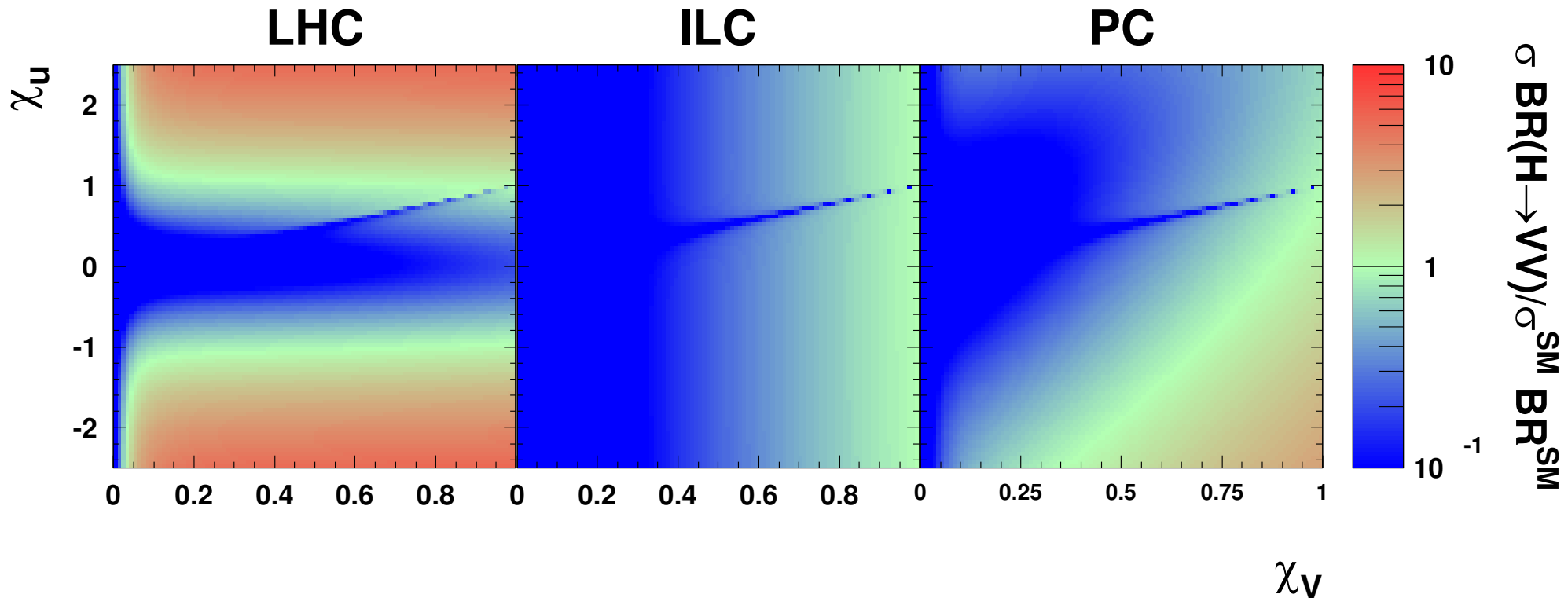


LHC ⊕ ILC ⊕ PC

Measurements at LHC, ILC and Photon Collider are complementary, being sensitive to different combinations of Higgs-boson couplings

Cross sections × BR relative to SM

$M_H = 250 GeV$



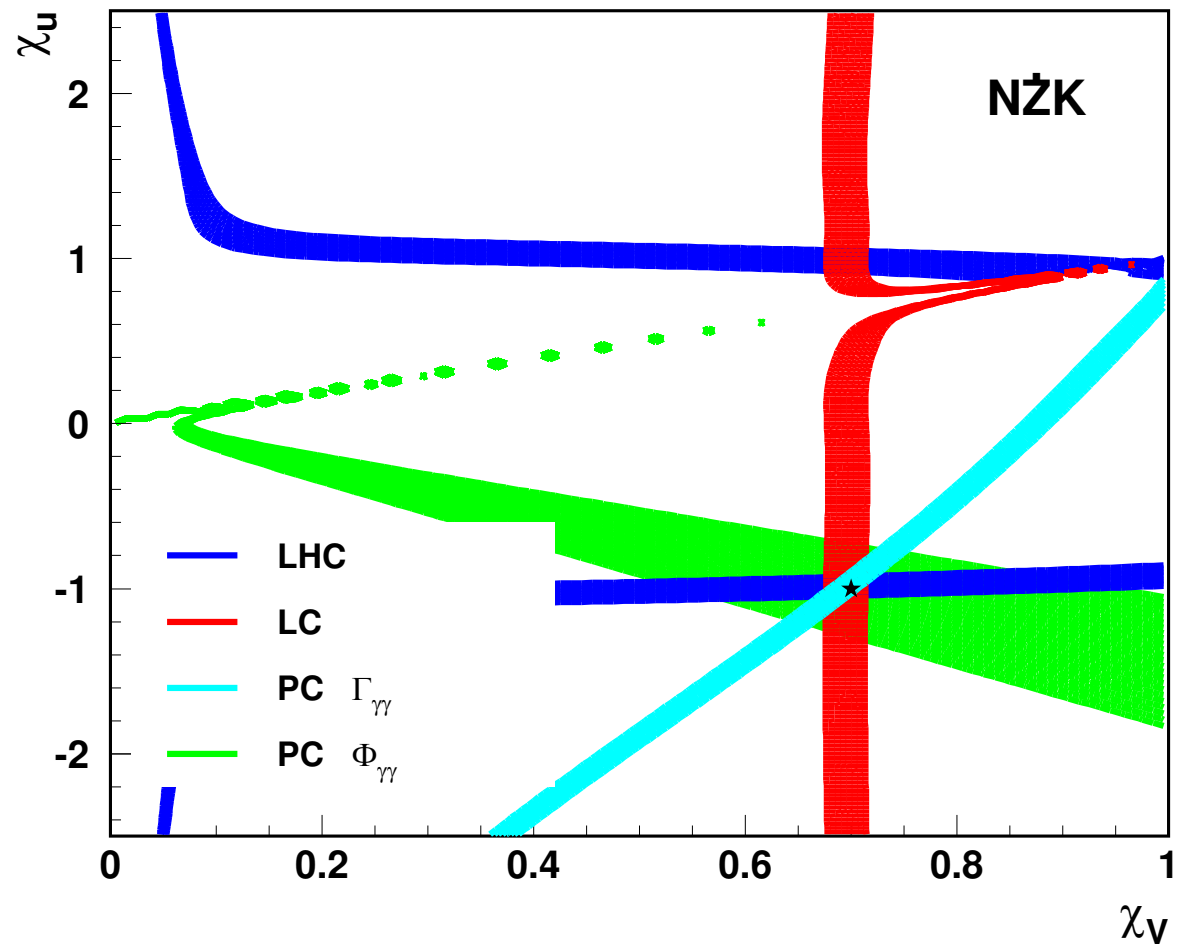
# LHC ⊕ ILC ⊕ PC

Allowed coupling values ( $1\sigma$ ) from **cross section** measurements at **LHC**, **ILC** and **PC**, and the phase measurement at **PC**.

Consistency of all these measurements verifies the **coupling structure of the model**

statistical errors only

$$\chi_V = 0.7 \quad \chi_u = -1 \quad M_H = 250 \text{ GeV}$$



# LHC ⊕ ILC ⊕ PC

Combined fit to the expected invariant mass distributions:

LHC

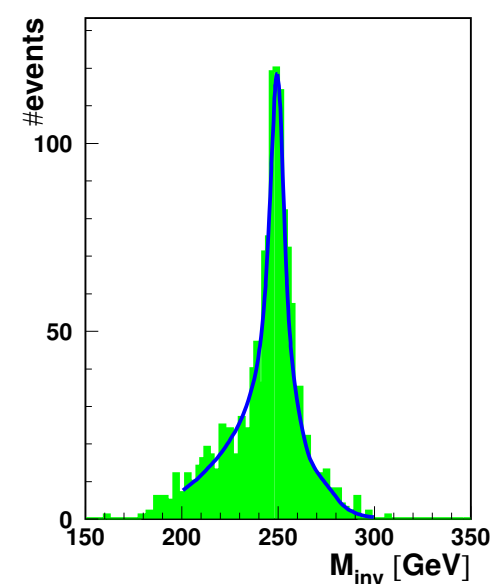
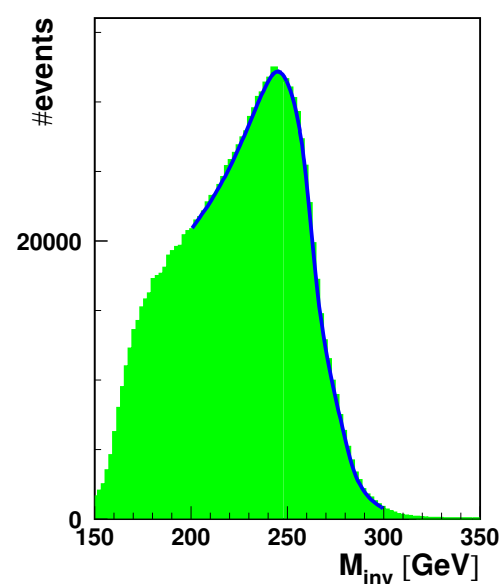
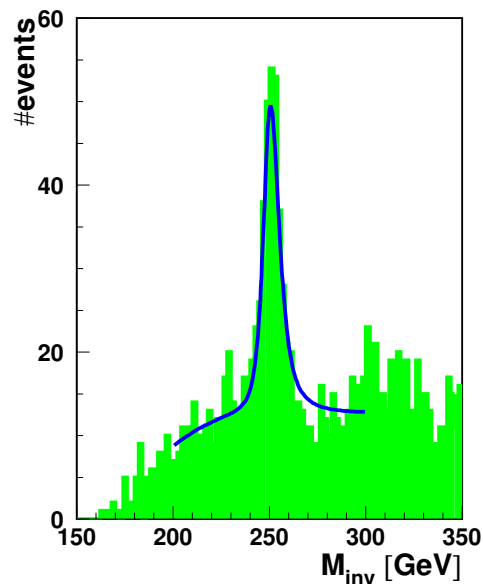
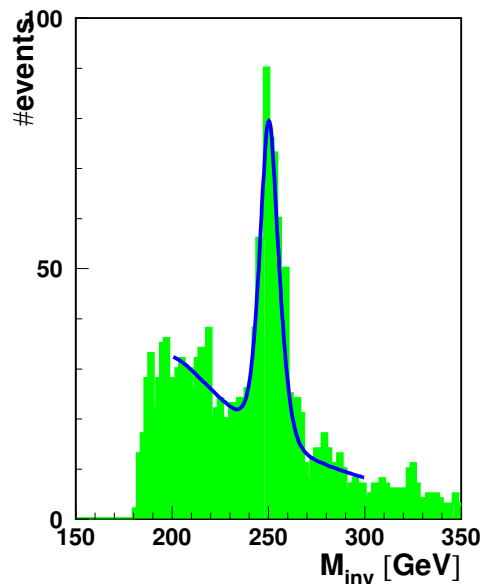
ILC

PC

$H \rightarrow WW$

PC

$H \rightarrow ZZ$



9 parameter fit: ●  $\chi_V$  ●  $\chi_u$  ●  $M_H$

+ 6 normalization and  $\gamma\gamma$ -spectra shape parameters (systematic uncertainties)

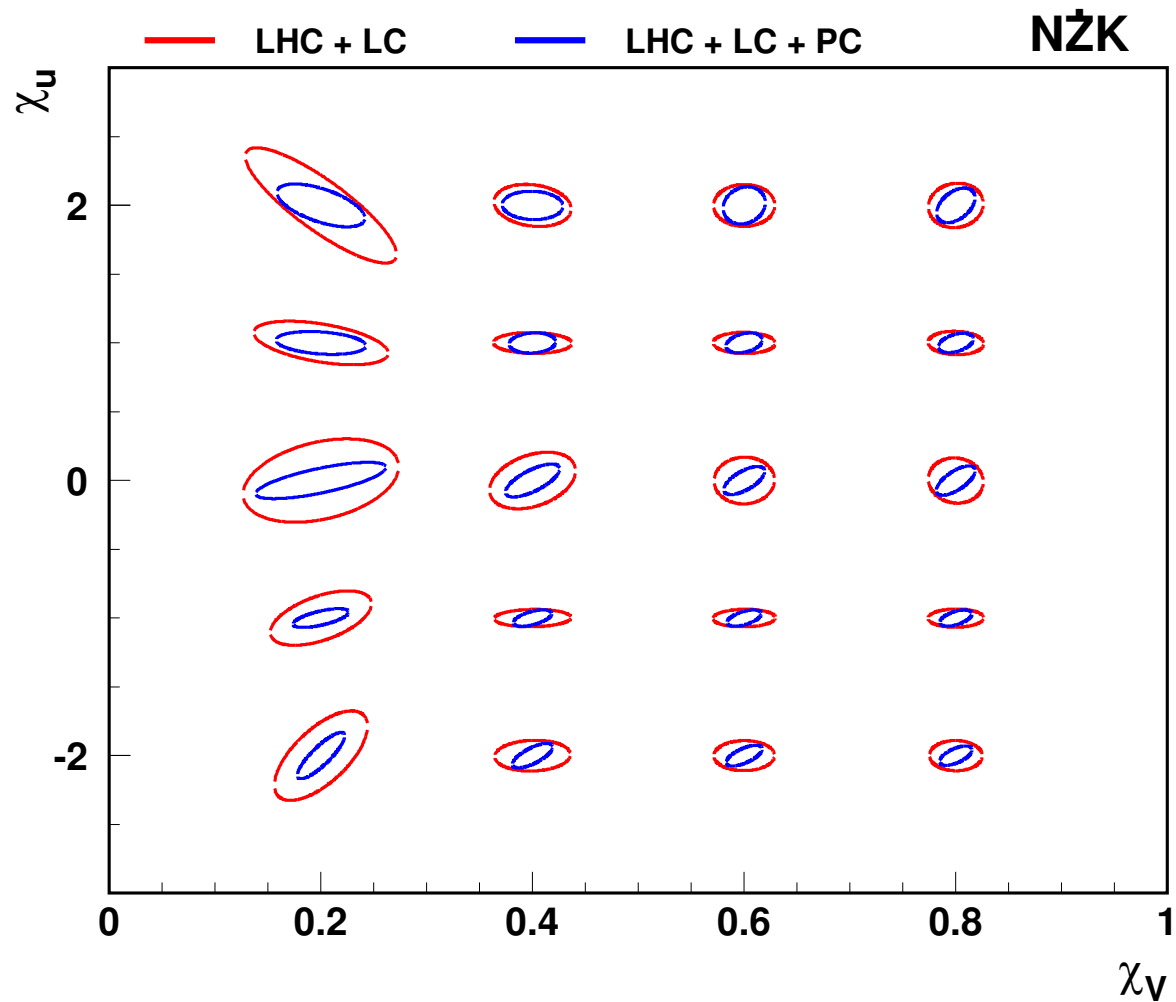
# LHC ⊕ ILC ⊕ PC

Simultaneous fit to LHC, ILC and PC ( $W^+W^-$  and  $ZZ$ ) invariant mass distributions

$1\sigma$  (stat.+sys.) contours

Comparison of error contours for combined analysis without and with weak PC

$H$  couplings to vector bosons ( $\chi_V$ ) and up fermions ( $\chi_u$ ) for  $M_H = 250$  GeV



# LHC ⊕ ILC ⊕ PC

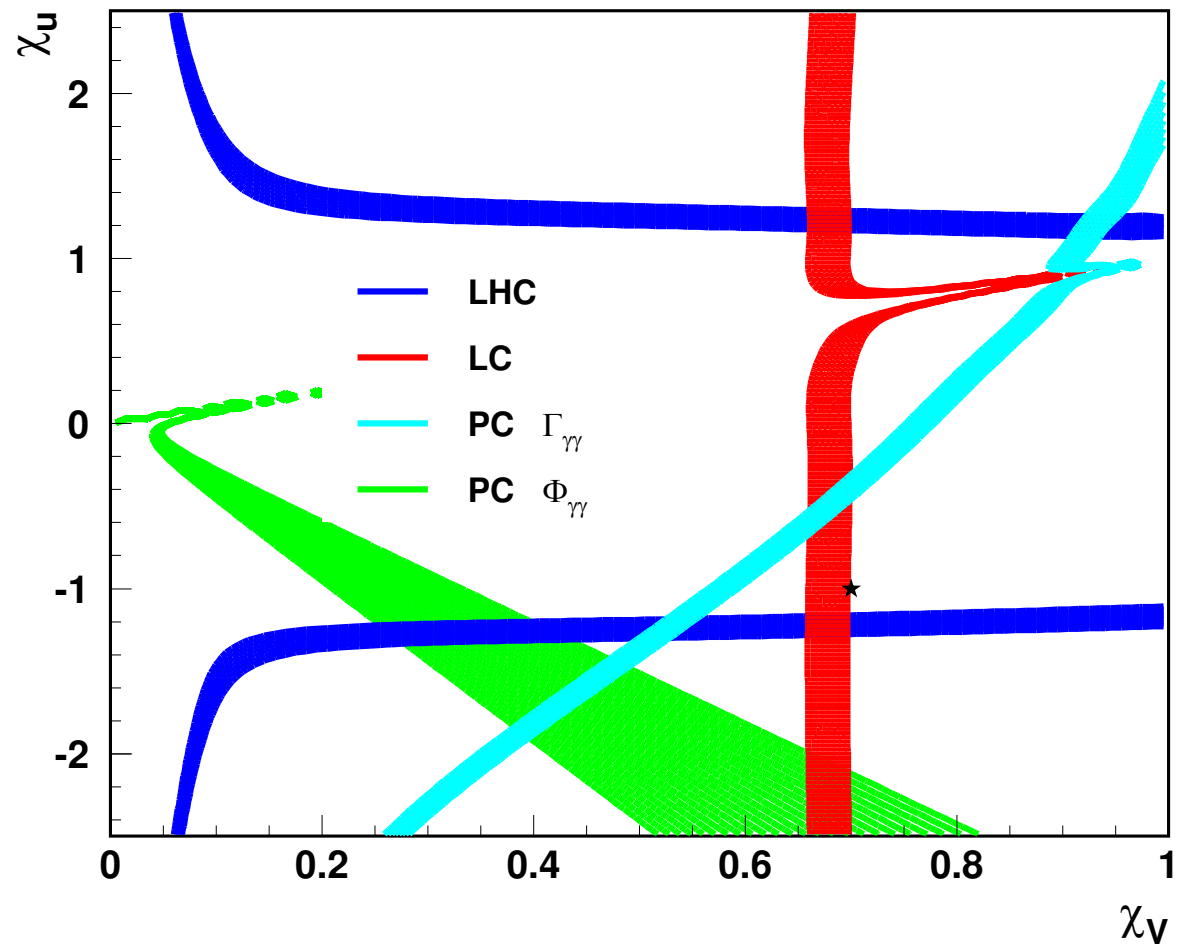
Allowed coupling values from **cross section** measurements at **LHC**, **ILC** and **PC**, and the phase measurement at **PC**.

Measurements compared assuming **CP-conserving 2HDM(II)** not consistent ⇒ “new physics”:

- different **coupling structure** (eg. CP violation)
- existence of **new heavy particles** contributing to  $\Gamma_{gg}$  and  $\Gamma_{\gamma\gamma}$

$$\chi_V = 0.7 \quad \chi_u = -1 \quad \Phi_{HA} = -0.2$$

**NŻK**





## 2HDM (II) with CP violation

### $H - A$ mixing

Mass eigenstates of the neutral Higgs-bosons  $h_1$ ,  $h_2$  and  $h_3$  do not need to match CP eigenstates  $h$ ,  $H$  and  $A$ .

We consider weak CP violation through a small mixing between  $H$  and  $A$  states:

$$\begin{aligned}\chi_X^{h_1} &\approx \chi_X^h \\ \chi_X^{h_2} &\approx \chi_X^H \cdot \cos \Phi_{HA} + \chi_X^A \cdot \sin \Phi_{HA} \\ \chi_X^{h_3} &\approx \chi_X^A \cdot \cos \Phi_{HA} - \chi_X^H \cdot \sin \Phi_{HA}\end{aligned}$$

⇒ additional model parameter: **CP-violating mixing phase  $\Phi_{HA}$**

⇒ see our paper JHEP 0502:041,2005 [hep-ph/0403138]

In general case

**combined analysis** of LHC, Linear Collider and Photon Collider data is needed

We consider  $h_2$  production and decays, for  $|\Phi_{HA}| \ll 1$  (weak CP violation)

LHC

Measurement of the production cross section times branching ratio

$$\sigma(pp \rightarrow hX) \cdot BR(h \rightarrow ZZ \rightarrow 4l)$$

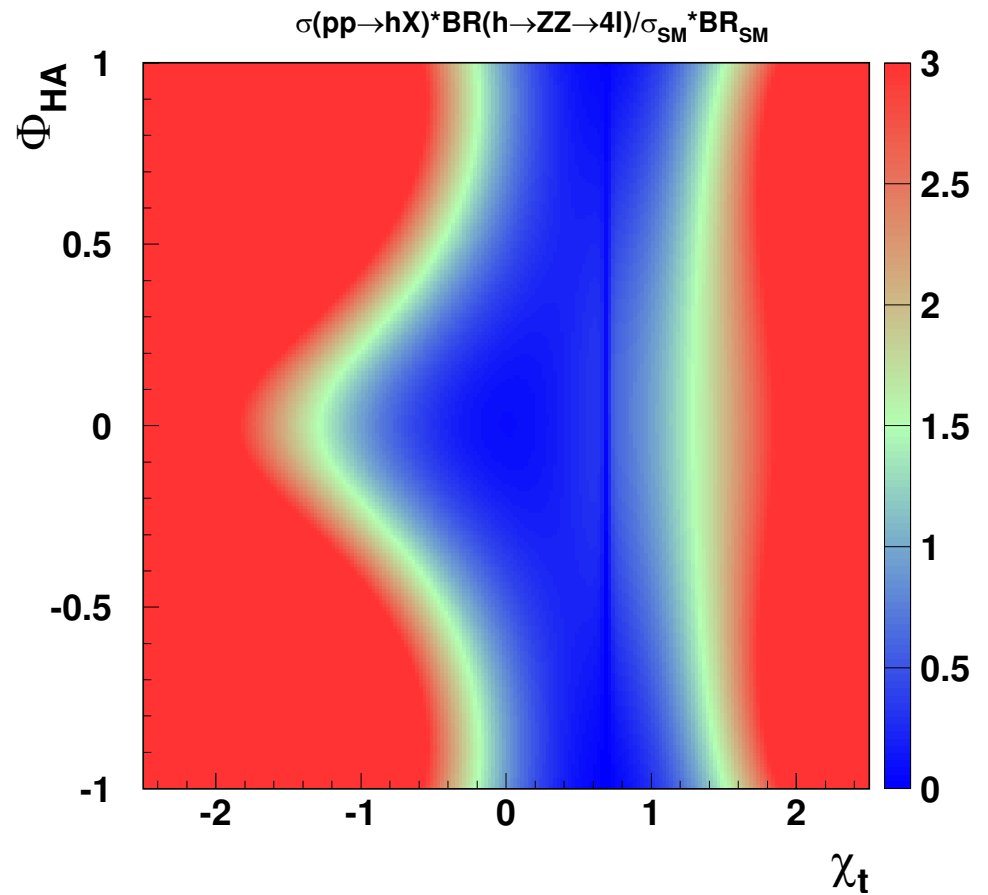
not sensitive to  $\chi_V$

constrains mainly  $|\chi_u|$  value

Limited sensitivity to  $\Phi_{HA}$

for  $\Phi_{HA} \approx 0$

Cross section relative to SM



ILC

Measurement of the production cross section times branching ratio

$$\sigma(e^+e^- \rightarrow hX) \cdot BR(h \rightarrow WW/ZZ)$$

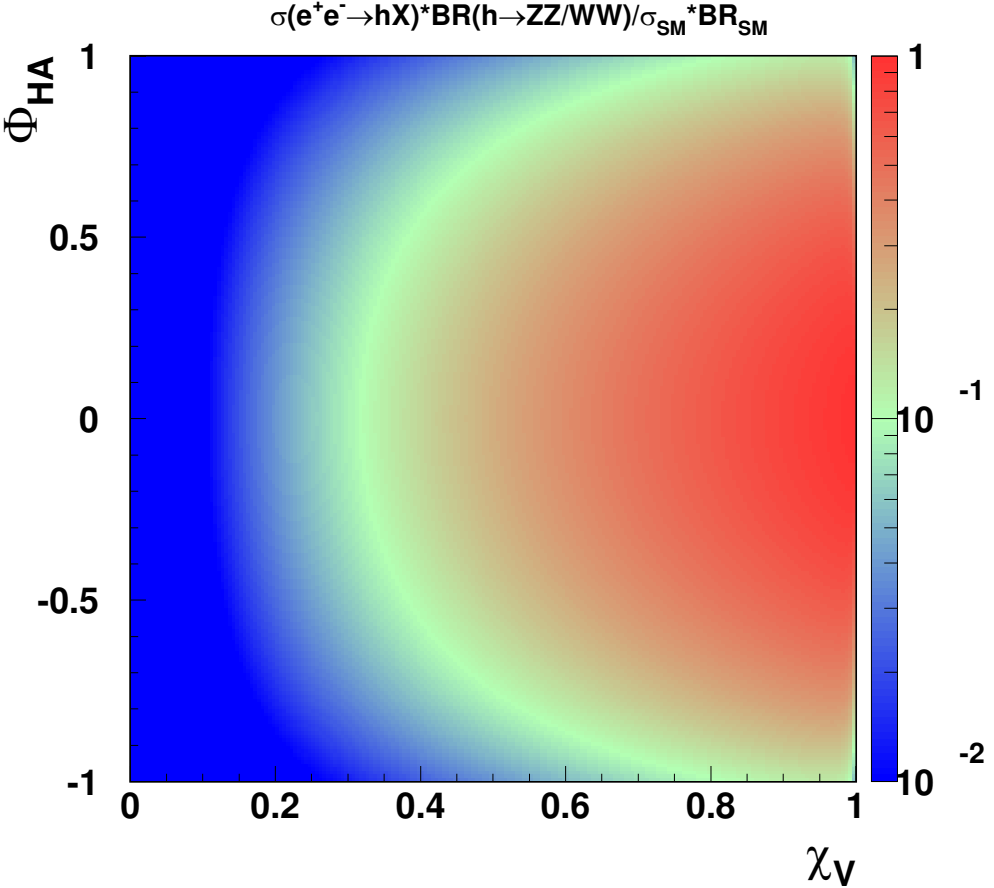
not sensitive to  $\chi_t$

constrains mainly  $\chi_V$  value

Even smaller sensitivity to  $\Phi_{HA}$

for  $\Phi_{HA} \approx 0$

Cross section relative to SM



# PLC

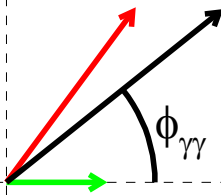
Contributions from  $W^\pm$  and top loops to the two-photon amplitude:

CP-conserving 2HDM (II)

$$\chi_V = 0.7, \chi_t = -1$$

$M_h = 300. \text{ GeV}$

Im(A)



Re(A)

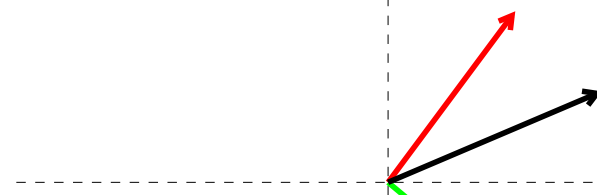
— SM  
— W  
— t

2HDM (II) with weak CP violation

$$\chi_V = 0.7, \chi_t = -1, \Phi_{HA} = -0.2$$

$M_h = 300. \text{ GeV}$

Im(A)



Re(A)

— SM  
— W  
— t

Significant change both in  $\Gamma_{\gamma\gamma}$  and in  $\phi_{\gamma\gamma}$

# PLC

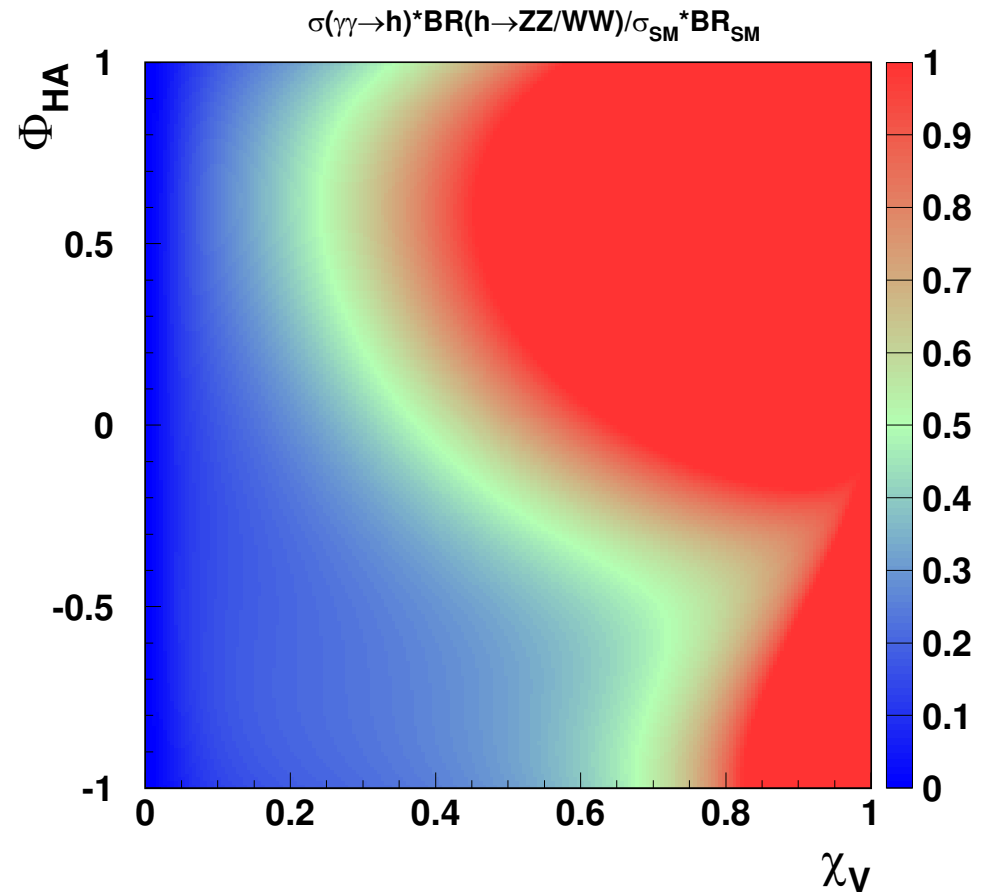
Measurement of the production cross section times branching ratio

$$\sigma(\gamma\gamma \rightarrow h) \cdot BR(h \rightarrow WW/ZZ)$$

sensitive to both  $\chi_V$  and  $\chi_t$

also very sensitive to  $\Phi_{HA}$

Cross section relative to SM



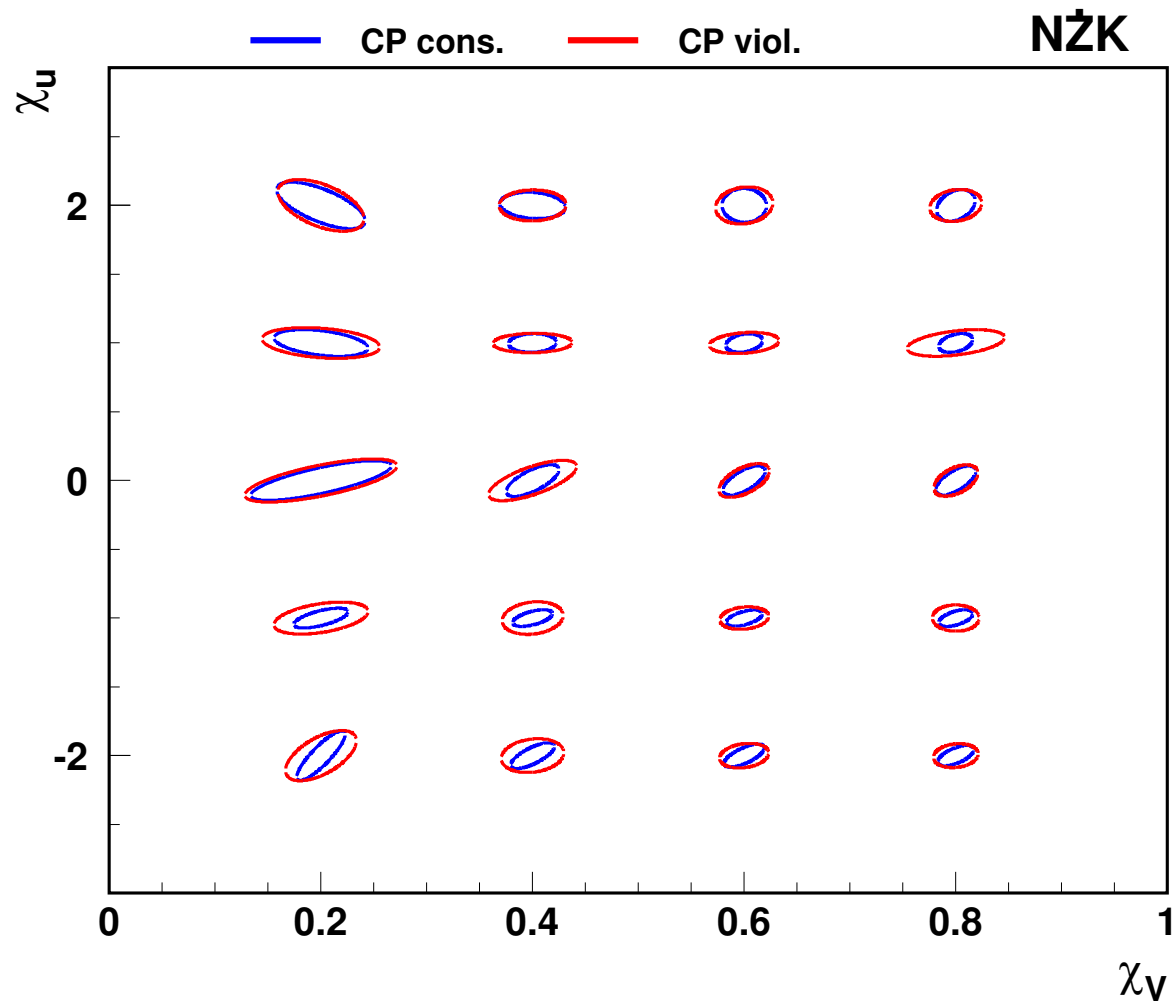
# LHC ⊕ ILC ⊕ PC

Simultaneous fit to LHC, ILC and PC ( $W^+W^-$  and  $ZZ$ ) invariant mass distributions

$1\sigma$  (stat.+sys.) contours

Comparison of error contours for model without and with weak CP violation

$H$  couplings to vector bosons ( $\chi_V$ ) and up fermions ( $\chi_u$ ) for  $M_H = 250$  GeV

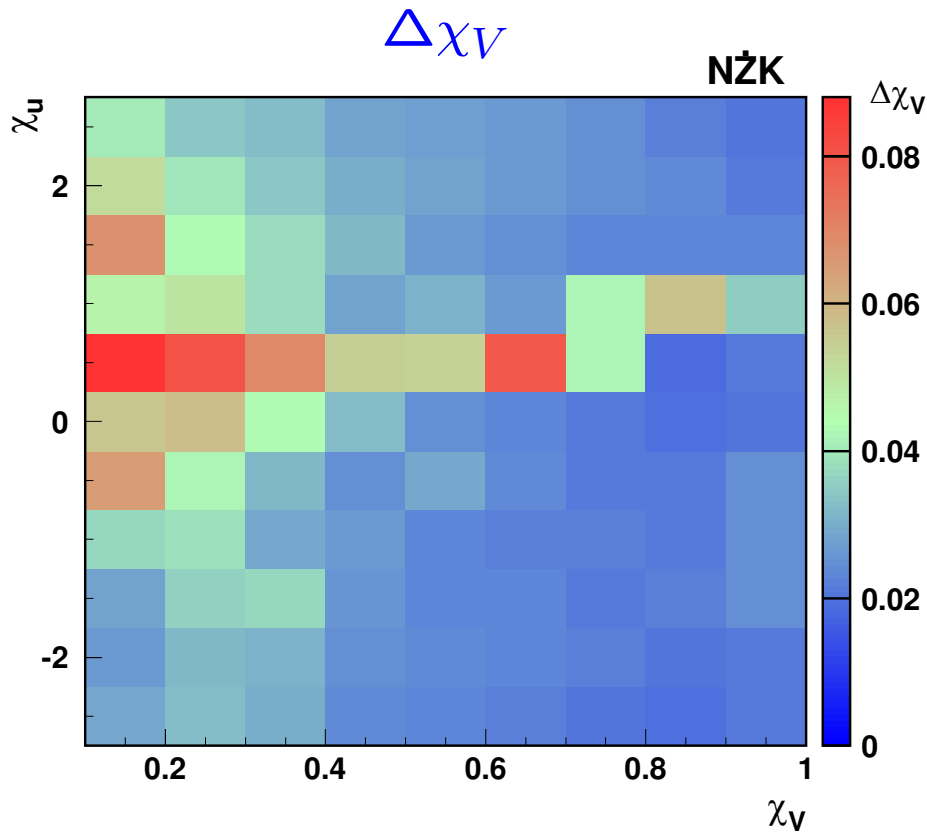


coupling errors  $\Rightarrow$  next slide

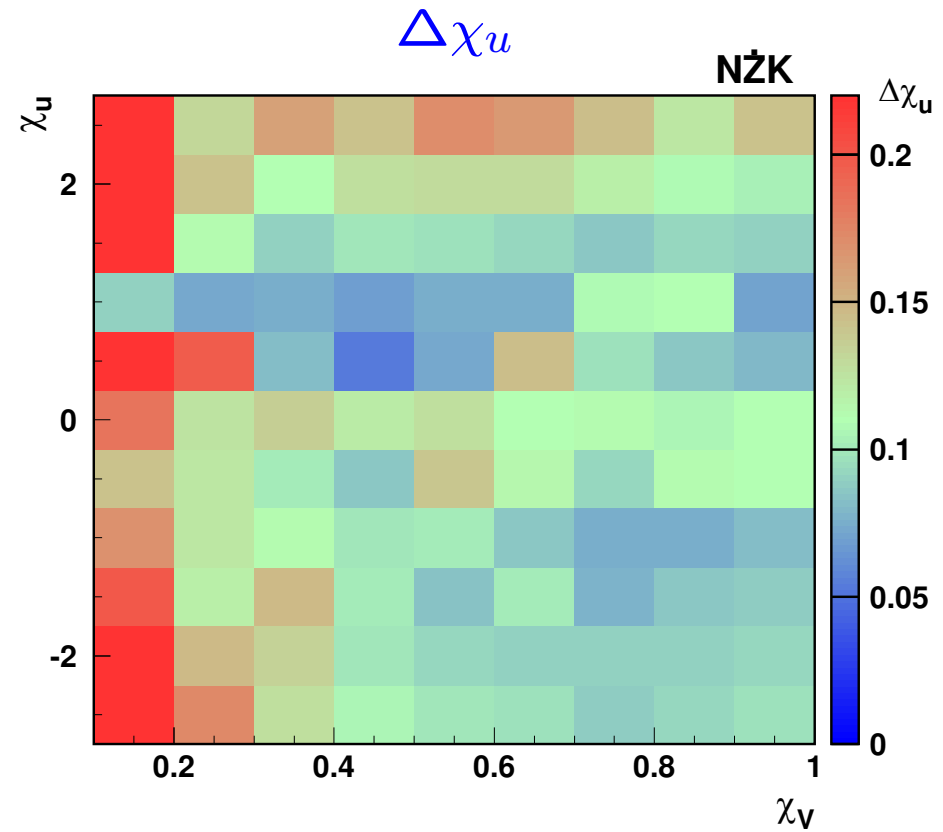
LHC ⊕ ILC ⊕ PC

## Coupling errors

Estimated total errors on Higgs boson **couplings** for  $M_H=250$  GeV



$$\langle \Delta\chi_V \rangle = 0.033$$

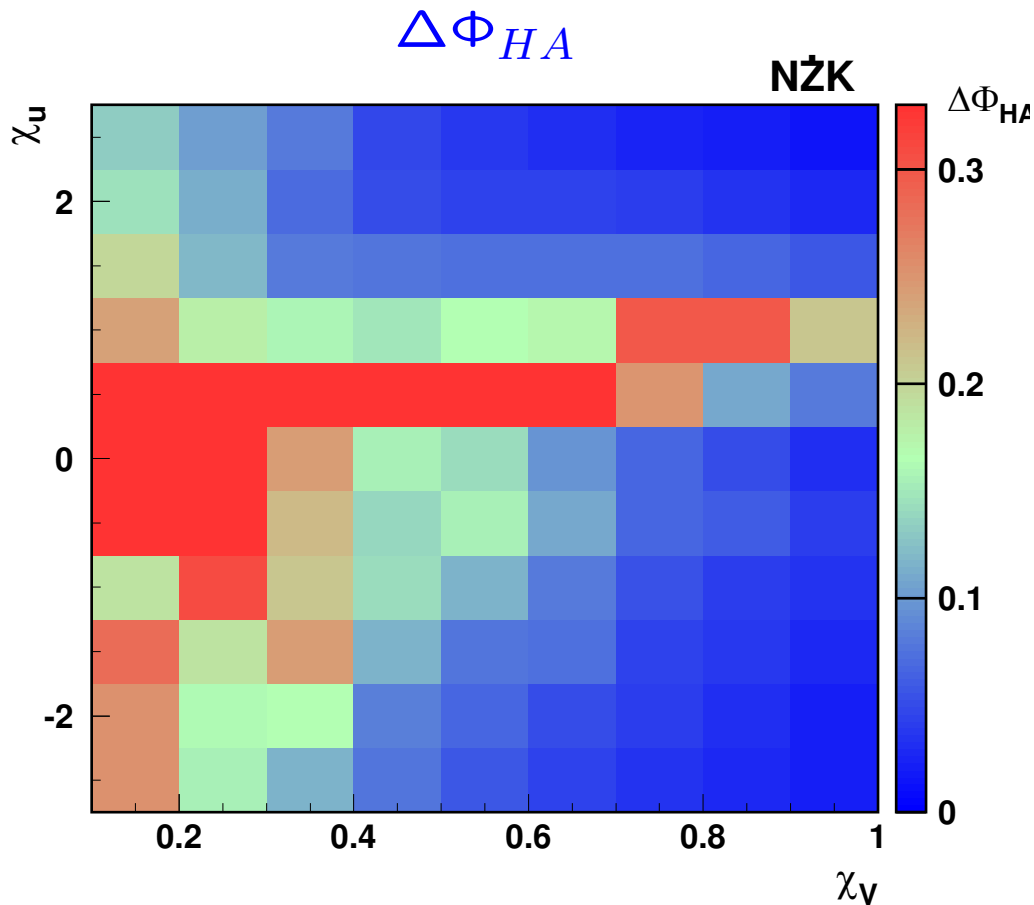


$$\langle \Delta\chi_u \rangle = 0.12$$

LHC ⊕ ILC ⊕ PC

$\Phi_{HA}$  error

Estimated total errors on  $H - A$  mixing angle, for  $M_H=250$  GeV



For a wide range of couplings

$$\Delta\Phi_{HA} \leq 100 \text{ mrad}$$

Determination of  $\Phi_{HA}$  not possible  
without **Photon Collider** data

$$\langle \Delta\Phi_{HA} \rangle = 150 \text{ mrad}$$



## Summary

Heavy **Higgs** boson production and decays to **WW/ZZ** studied for masses between **200** and **350 GeV**.

**2HDM(II)** considered, without and with (weak) **CP violation**

**Measurements** at **LHC**, **ILC** and Photon Collider are **complementary**, being sensitive to different combinations of Higgs-boson couplings.

Only the **combined analysis** of LHC, ILC and PC measurements allows for the determination of the CP-violating  **$H - A$  mixing** angle  $\Phi_{HA}$ .

In most of the considered parameter space  $\Phi_{HA}$  measured to better than **100 mrad**.

# Systematic uncertainties

## LHC ⊕ ILC ⊕ PC analysis

### Parameter:

- Higgs boson mass
- $\gamma\gamma$  luminosity
- $\gamma\gamma$  spectra shape parameters
- background normalization for  $e^+e^-$
- signal normalization for  $pp$
- background normalization for  $pp$

### Assumed uncertainty:

- ⇒ unconstrained
- ⇒ unconstrained
- ⇒ 5% uncertainty
- ⇒ 5% uncertainty
- ⇒ 10% uncertainty
- ⇒ 10% uncertainty