

SUSY breaking, hybrid $\mathcal{N} = 1/2$ theories, and the nature of *.inos

Daniel Busbridge

Supervised by: Valya Khoze and Steve Abel

Institute for Particle Physics Phenomenology
Durham University

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Outline

1 Concepts

- What is SUSY?
- Irreducible representations of $\mathcal{N} = 1$ SUSY

2 Spontaneous SUSY

- The Sad Truth
- Generic Features

3 Dirac *.inos

- Dirac vs. Majorana Fermions
- Parameter space limitations
- R -symmetry

4 MRSSM

- Higgs Sector

5 Optional extras

What is SUSY?

SUSY is a space-time (ST) symmetry

$$\begin{aligned} Q|\text{Fermion}\rangle &= |\text{Boson}\rangle \\ Q|\text{Boson}\rangle &= |\text{Fermion}\rangle \end{aligned} \quad \left. \right\} \text{ Qs generate a ST symmetry}$$

$$\{Q, Q^\dagger\} = P \iff [\theta Q, \theta^\dagger Q^\dagger] = \theta \theta^\dagger P$$

Irreducible representations of $\mathcal{N} = 1$ SUSY

An Introduction to Superspace

$$\begin{aligned}x &\longrightarrow (x, \theta, \theta^\dagger) \\ s(x) &\longrightarrow S(x, \theta, \theta^\dagger)\end{aligned}$$

$$\Phi = \phi + \theta\psi + \theta^2 F + \dots$$

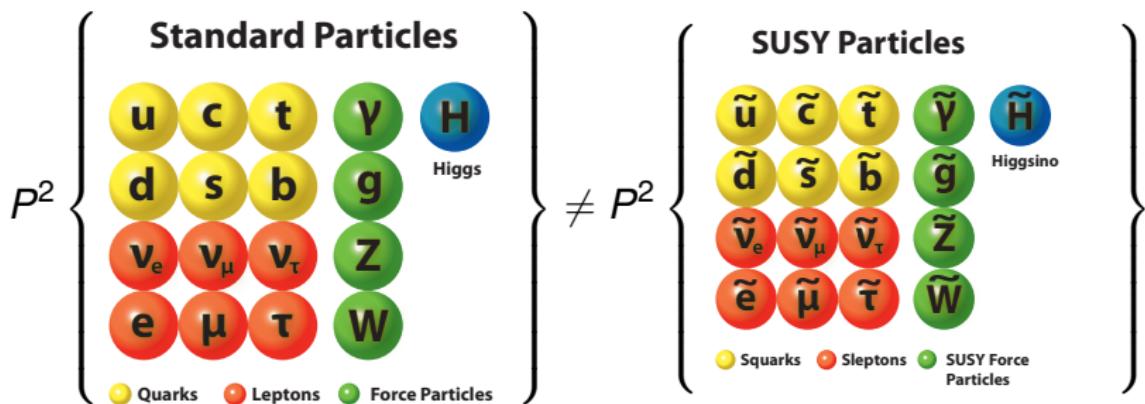
$$\mathbf{V} = \theta\theta^\dagger A + \theta^{\dagger 2}\theta\lambda + \theta^2\theta^{\dagger 2}D + \dots$$

$$\mathbf{W}_\alpha = \lambda_\alpha + \theta_\alpha D + \dots$$

The Sad Truth

Evidence

- Degeneracy in (s)particle mass spectrum not observed



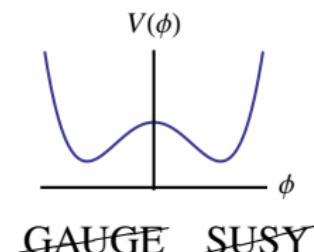
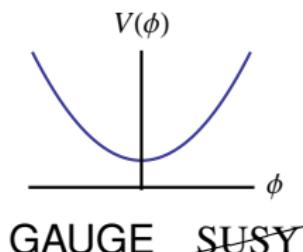
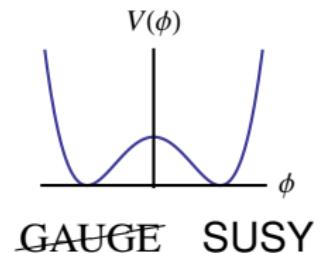
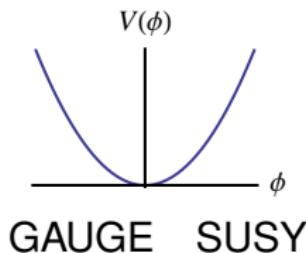
- If SUSY is realized, it is broken at low energies

Generic Features

Properties

- Theory is SUSY but scalar potential V admits ~~SUSY~~ vacua

$$Q|\text{vacuum}\rangle \neq 0 \iff V(\text{vacuum}) > 0$$



Generic Features

Recipe

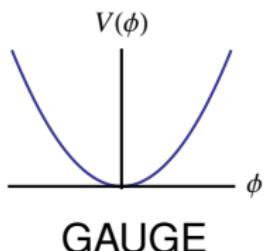
- $U(1)$ VSF spurion $\langle \mathbf{W}_\alpha \rangle = \theta_\alpha D$
- Gauge-singlet χ SF spurion $\langle \mathbf{X} \rangle = \theta^2 F$

How does this work?

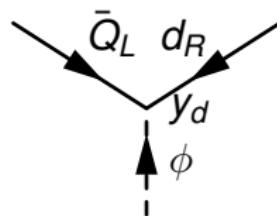
Generic Features

The Standard Model Higgs Mechanism

$$\Lambda > \Lambda_{\text{EWSB}}$$



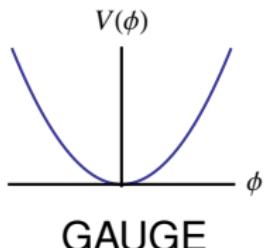
$$-\mathcal{L} \supset y_d \bar{Q}_L \phi d_R$$



Generic Features

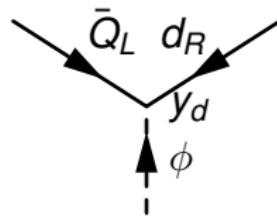
The Standard Model Higgs Mechanism

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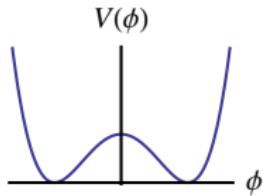
GAUGE

$$-\mathcal{L} \supset y_d \bar{Q}_L \phi d_R$$



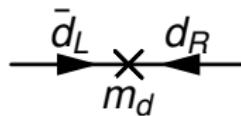
$$\Lambda < \Lambda_{\text{EWSB}}$$

$$\phi \rightarrow (0, \nu + H)$$



GAUGE

$$-\mathcal{L} \supset \underbrace{y_d \nu}_{m_d} \bar{d}_L d_R$$

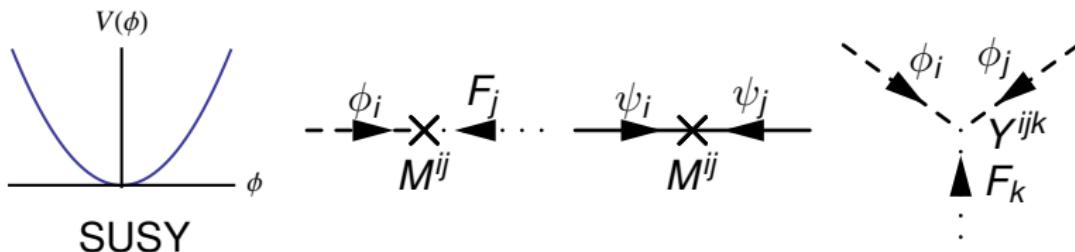


Generic Features

SUSY Breaking in Wess-Zumino Model

$$\Lambda > \Lambda_{\text{SUSY}}$$

$$\begin{aligned} \mathcal{L} = & \int d^2\theta \underbrace{M^{ij}\Phi_i\Phi_j + Y^{ijk}\Phi_i\Phi_j\Phi_k}_{W(\Phi_i)} + \text{h.c.} + \int d^2\theta d^2\theta^\dagger \underbrace{\Phi^{*i}\Phi_j}_{K(\Phi^{*i}, \Phi_j)} \\ \supset & -M^{ij} (\phi_i F_j + \psi_i \psi_j) - Y^{ijk} \phi_i \phi_j F_k + \text{h.c.} + F^{*i} F_i \end{aligned}$$

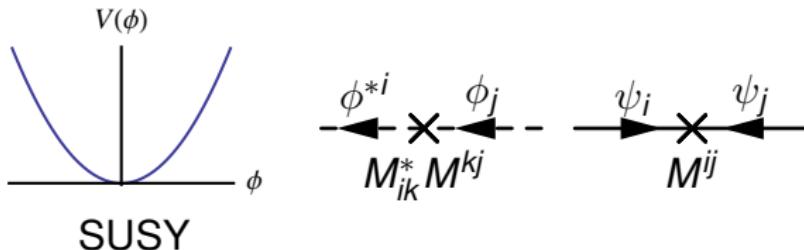


Generic Features

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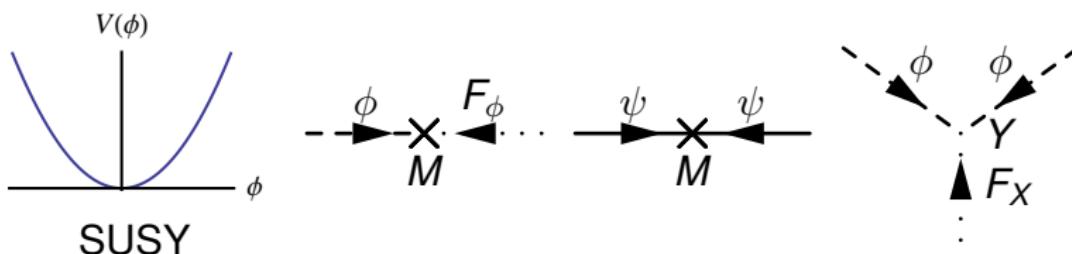


Generic Features

SUSY Breaking in Wess-Zumino Model

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$$\begin{aligned}\mathcal{L} = & \int d^2\theta \left(M\Phi^2 + Y\Phi^2 X \right) + \text{h.c.} + \int d^2\theta d^2\theta^\dagger \Phi^* \Phi \\ \supset & -M(\phi F_\phi + \psi \psi) - Y\phi\phi F_X + \text{h.c.} + |F_\phi|^2 + |F_X|^2\end{aligned}$$

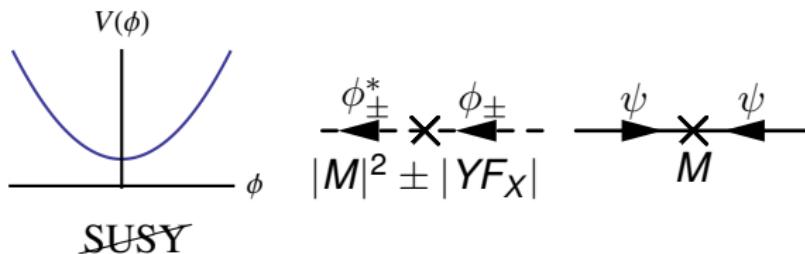


Generic Features

SUSY Breaking in Wess-Zumino Model

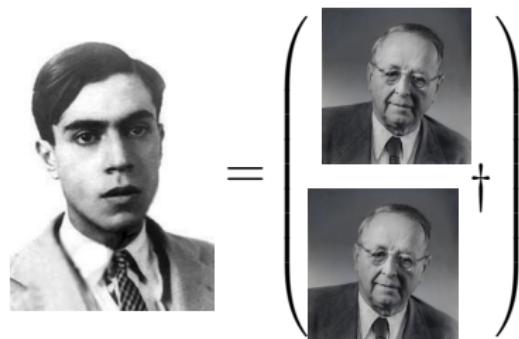
$$\Lambda < \Lambda_{\text{SUSY}} \quad \langle X \rangle = \theta^2 F$$

$$\begin{aligned} \mathcal{L} = & \int d^2\theta \left(M\phi^2 + Y\phi^2 X \right) + \text{h.c.} + \int d^2\theta d^2\bar{\theta} \phi^\dagger \Phi^* \Phi \\ \supset & -M\psi\psi - (|M|^2 \pm |YF_X|)|\phi_\pm|^2 \end{aligned}$$



Dirac vs. Majorana Fermions

Dirac and Majorana particles



Dirac vs. Majorana Fermions

Dirac and Majorana particles

$$\text{Young Dirac} = \left(\begin{array}{c} \text{Old Dirac} \\ + \\ \text{Old Dirac} \end{array} \right)$$

$$\text{Young Majorana} = \left(\begin{array}{c} \text{Old Majorana} \\ + \\ \text{Old Majorana} \end{array} \right)$$

Dirac vs. Majorana Fermions

Mass terms

Majorana mass

$$-\mathcal{L}_{\text{Majorana}} \supset M_M \bar{\Psi}_M \Psi_M = M_M (\xi \xi + \xi^\dagger \xi^\dagger) \quad \Psi_M = \begin{pmatrix} \xi \\ \xi^\dagger \end{pmatrix}$$

Dirac mass

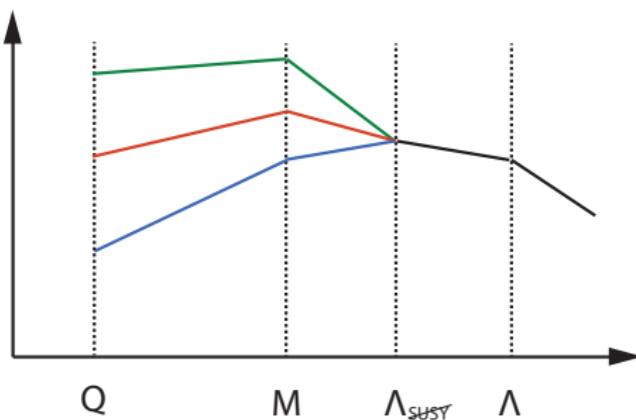
$$-\mathcal{L}_{\text{Dirac}} \supset M_D \bar{\Psi}_D \Psi_D = M_D (\xi \chi + \xi^\dagger \chi^\dagger) \quad \Psi_D = \begin{pmatrix} \xi \\ \chi^\dagger \end{pmatrix}$$

$$-\mathcal{L}_{\text{soft}}^{\text{MSSM}} \supset M_3 \widetilde{g}\widetilde{g} + M_2 \widetilde{W}\widetilde{W} + M_1 \widetilde{B}\widetilde{B}$$

Parameter space limitations

Approximate SQCD β Functions

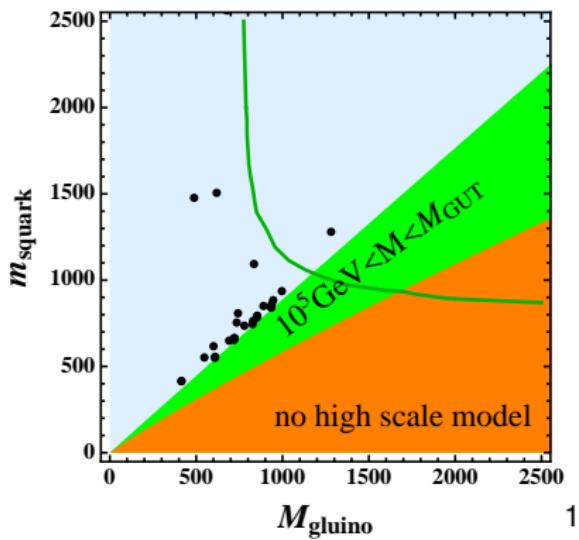
$$\frac{d}{dt} m_{\tilde{q}}^2 \sim m_{\tilde{q}}^2 + M_{\tilde{g}}^2$$
$$\frac{d}{dt} M_{\tilde{g}} \sim M_{\tilde{g}}$$



$$m_{\tilde{q}}^2(Q) \sim m_{\tilde{q}}^2(M) + a m_{\tilde{q}}^2(M) + b M_{\tilde{g}}^2(Q)$$

Parameter space limitations

The Forbidden Zone



¹ Jaeckel, J., Khoze, V. V., Plehn, T., & Richardson, P. (2011). Travels on the squark-gluino mass plane. <http://arxiv.org/abs/1109.2072>

R-symmetry

What is *R*-symmetry?

$$\{Q, Q^\dagger\} = P$$

Invariant under

$$Q \rightarrow e^{iR_Q \theta} Q, \quad Q^\dagger \rightarrow Q^\dagger e^{-iR_Q \theta}, \quad P \rightarrow P$$

Choose $R_Q = -1$

$$[Q, R] = Q$$

$$[\theta, R] = -\theta$$

$$[Q^\dagger, R] = -Q^\dagger$$

$$[\theta^\dagger, R] = \theta^\dagger$$

R-symmetry

R-charge of Gauginos

$$V = V^\dagger \implies R_V = 0$$

$$V \supset \theta^{\dagger 2} \theta \lambda$$

$$R_\theta = -R_{\theta^\dagger} = 1 \implies R_\lambda = 1$$

R-symmetry

Majorana Gaugino Masses

$$-\mathcal{L}_{\text{Majorana}}^{\text{gaugino}} \supset M_M(\lambda\lambda + \lambda^\dagger\lambda^\dagger)$$

$$\lambda\lambda \xrightarrow{U(1)_R} e^{2i\theta}\lambda\lambda$$

Majorana gaugino masses violate $U(1)_R$ symmetry

R-symmetry

Dirac Gaugino Masses

$$-\mathcal{L}_{\text{Dirac}} \supset M_D(\lambda\chi + \lambda^\dagger\chi^\dagger)$$

$$\lambda\chi \xrightarrow{U(1)_R} e^{i(1+R_\chi)\theta} \lambda\chi$$

Dirac gaugino masses can preserve $U(1)_R$ symmetry

R-symmetry

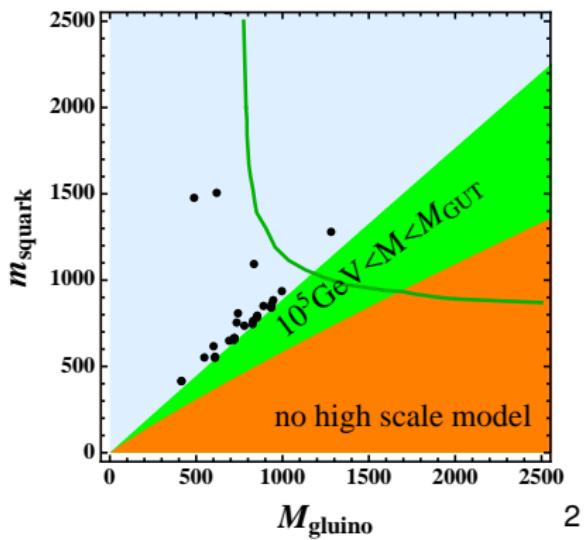
The idea

$$\begin{array}{ccc} U(1)_R & \longleftrightarrow & \cancel{U(1)_R} \\ M_M \rightarrow 0 & & \frac{M_M}{M_D} \gg 1 \end{array}$$



R-symmetry

The Forbidden Zone



² Jaeckel, J., Khoze, V. V., Plehn, T., & Richardson, P. (2011). Travels on the squark-gluino mass plane. <http://arxiv.org/abs/1109.2072>

R-symmetry

Minimal Dirac Gauginos

$$R_{\chi_g} = -1, \quad \mathbf{O}_g \supset \theta \chi_g, \quad \langle \mathbf{W}'_\alpha \rangle = \theta_\alpha D$$

Names	Superfield	$SU(3)_C$	$U(1)_R$
RHGs	\mathbf{O}_g	Ad	0
GFs	$\mathbf{W}_{3\alpha}$	Ad	1

$$\mathcal{L}_{\text{gluino}}^{\text{Dirac}} = \int d^2\theta \frac{\mathbf{W}'^\alpha}{\Lambda} \text{Tr} [\mathbf{W}_{3\alpha} \mathbf{O}_g] \supset -m_D \lambda_3 \chi_g$$

$$m_D = \frac{D}{\Lambda} \tag{1}$$

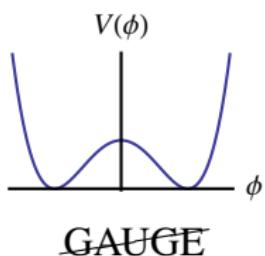
$\mathcal{N} = 2$ vector multiplet $(\mathbf{O}_g, \mathbf{V}_3)$

Higgs Sector

MSSM Higgs

$$W_{\text{MSSM}} = y_u \bar{\mathbf{u}} \mathbf{Q} \cdot \mathbf{H}_u + y_d \bar{\mathbf{d}} \mathbf{Q} \cdot \mathbf{H}_d + \mu \mathbf{H}_u \cdot \mathbf{H}_d + \dots$$

$$\Lambda < \Lambda_{\text{EWSB}}$$



$$H_u^0 \rightarrow \nu_u + \dots$$
$$H_d^0 \rightarrow \nu_d + \dots$$

GAUGE

$$\mathcal{L} \supset \int d^2\theta W(\Phi_i) \supset -\mu \tilde{\mathbf{H}}_u \cdot \tilde{\mathbf{H}}_d$$

Higgs Sector

Dirac Higgsinos

Superfield	$SU(2)_L$	$U(1)_Y$	$U(1)_R$
\mathbf{H}_u	□	$\frac{1}{2}$	0
\mathbf{R}_d	□	$\frac{1}{2}$	2
\mathbf{H}_d	□	$-\frac{1}{2}$	0
\mathbf{R}_u	□	$-\frac{1}{2}$	2

$$W_{\text{Higgs}} = \left(\mu_u + \lambda_u^S \mathbf{S} \right) \mathbf{H}_u \cdot \mathbf{R}_u + \lambda_u^T \mathbf{H}_u \cdot \mathbf{T R}_u + (u \leftrightarrow d)$$

$\mathcal{N} = 2$ Hypermultiplet ($\mathbf{H}_u, \mathbf{R}_d$)

Higgs Sector

Is R -symmetry useful?

- Dangerous $\Delta L = \Delta B = 1$ operators forbidden
- Proton decay through $Q_L Q_L Q_L L_L, U_R U_R D_R E_R$ forbidden
- Majorana Neutrino mass $H_u H_u L_L L_L$ allowed³

³Kribs, G., Poppitz, E., & Weiner, N. (2008). Flavor in supersymmetry with an extended R symmetry. Physical Review D, 78(5) 055010

Higgs Sector

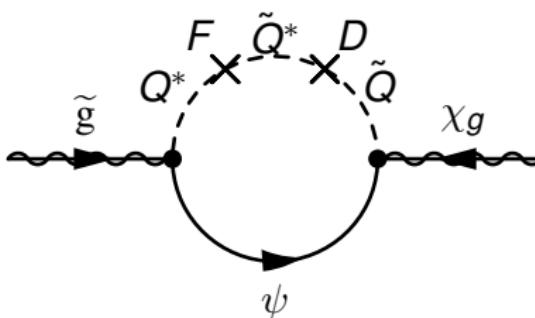
Summary of MRSSM

- All *.inos are Dirac
- Higgs and Gauge sector form $\mathcal{N} = 2$ representations
- Gauginos much heavier than squarks possible

Higgs Sector

Outlook

- High-scale completion? Gauge mediation?⁴



- Create a consistent effective theory at the high scale
- Identify important phenomenology using simplified models

⁴Benakli, K., & Goodsell, M. D. (2008). Dirac Gauginos in GGM.
arXiv:0811.4409

Concepts
oo

Spontaneous SUSY
oooooooo

Dirac *.inos
oooooooooooo

MRSSM
ooooo●

Optional extras

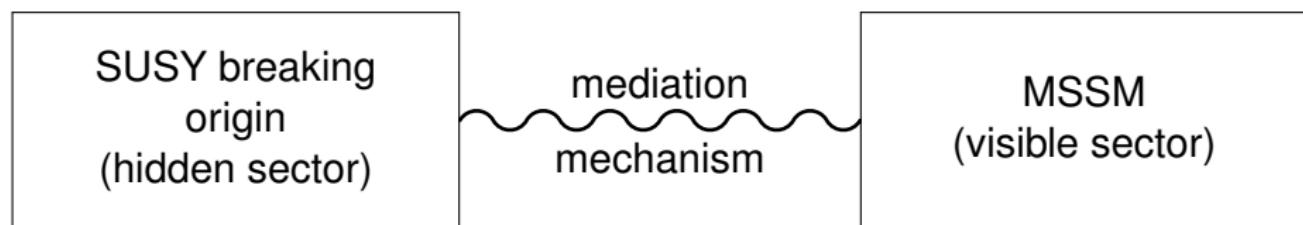
Higgs Sector

Thanks

Thanks for listening!

Where to Break Supersymmetry

Hidden sectors



Concepts
oo

Spontaneous SUSY
oooooooo

Dirac *.inos
oooooooooooo

MRSSM
oooooo

Optional extras

How to Communicate SUSY

Tree-level?

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- Supertrace Theorem:

tree level communication
+
renormalizable couplings } SUSY partner lighter
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Tree-level?

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- Non-renormalizable \implies Planck-Scale Mediated SUSY
- Non-tree-level \implies Gauge Mediated SUSY (GMSB)

Particle Content and Superpotential

blank

Messenger mass spectrum

Messenger mass spectrum

$$\begin{array}{c|c} & m^2 \\ \hline \phi, \bar{\phi} & M^2 \pm F^2 \\ \psi, \bar{\psi} & M^2 \end{array}$$

Messenger mass spectrum

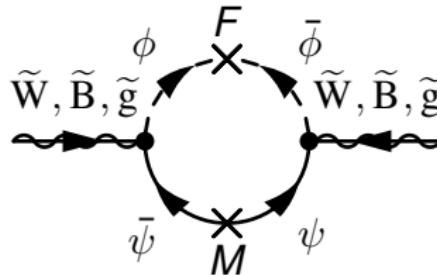
Messenger mass spectrum

$$\begin{array}{c|c} & m^2 \\ \hline \phi, \bar{\phi} & M^2 \pm F^2 \\ \psi, \bar{\psi} & M^2 \end{array}$$

SUSY is broken!

Soft Mass Generation

Majorana Gaugino masses at one-loop

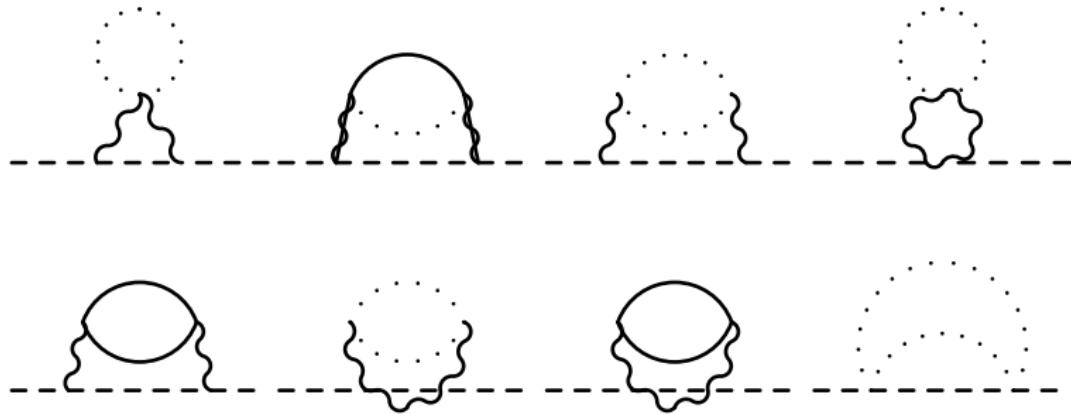


$$M_a \propto \alpha_a \Lambda$$

$$\Lambda = \frac{F}{M}$$

Soft Mass Generation

Squark/Slepton masses at two-loop



$$m_{\text{sq, sl}}^2 \propto \Lambda^2 \sum_a \alpha_a^2$$

$$\Lambda = \frac{F}{M}$$

Solving the Higgs Hierarchy Problem

Quick Higgs revision

Standard Model Higgs potential

$$V(H) \sim \mu^2 |H|^2 + \lambda |H|^4$$

Higgs vacuum expectation value (VEV)

$$\langle H \rangle = \sqrt{-\mu^2/2\lambda} \sim 174 \text{ GeV}$$

Implies a Higgs mass

$$m_H^2 = -\mu^2 \sim 100 \text{ GeV}$$

Solving the Higgs Hierarchy Problem

Higgs self-energy at one-loop

$$-\mathcal{L} \subset \lambda |s|^2 |H|^2 + g H \bar{f} f$$

$s = \text{scalars}$
 $f = \text{fermions}$

$$H - \text{---} \begin{array}{c} s \\ \text{---} \\ s \\ \text{---} \\ s \end{array} \text{---} H \sim -\lambda_s m_S^2 \ln \left(\frac{\Lambda}{m_S} \right)$$

$$H - \text{---} \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \text{---} H \sim \lambda_s \Lambda^2$$

$$H - \text{---} \begin{array}{c} f \\ \text{---} \\ f \end{array} \text{---} H \sim -\lambda_f^2 \Lambda^2$$

Solving the Higgs Hierarchy Problem

UV cut-off at one-loop

At one-loop

$$m_H^2 \longrightarrow m_H^2 + \Lambda^2 \left(\sum_{\text{scalars}} \lambda_s - \sum_{\text{fermions}} g_f^2 \right) - \sum_{\text{scalars}} \lambda_s m_s^2 \ln \left(\frac{\Lambda}{m_s} \right)$$

Natural Higgs mass

$$\Lambda \sim m_{\text{Pl}} \implies m_{\text{nat}} \sim m_{\text{Pl}}$$

Solving the Higgs Hierarchy Problem

Dim-reg at one-loop

At one-loop

$$m_H^2 \longrightarrow m_H^2 - \sum_{\text{scalars}} \lambda_s m_s^2 \ln \left(\frac{\mu}{m_s} \right)$$

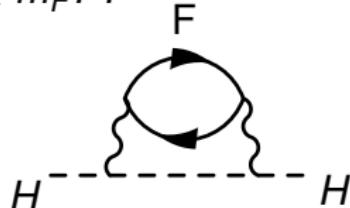
- m_H sensitive to *heaviest* particles Higgs couples to!
- Why is m_H so small?

Solving the Higgs Hierarchy Problem

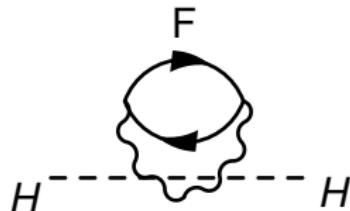
Some two loop Higgs self-energy processes

$$-\mathcal{L} \subset m_F \bar{F} F$$

$F = \text{fermions}$



$$\sim g^4 \left(\Lambda^2 + m_F^2 \ln \left(\frac{\Lambda}{m_F} \right) \right)$$



Solving the Higgs Hierarchy Problem

You saved us... thanks supersymmetry!

$$\frac{\psi/\phi/A \text{ pairings} + \lambda_f = \lambda_s^2 \text{ etc.}}{V(\phi) \text{ well behaved}}$$

Unavoidable with
supersymmetry



Gauge Coupling Unification

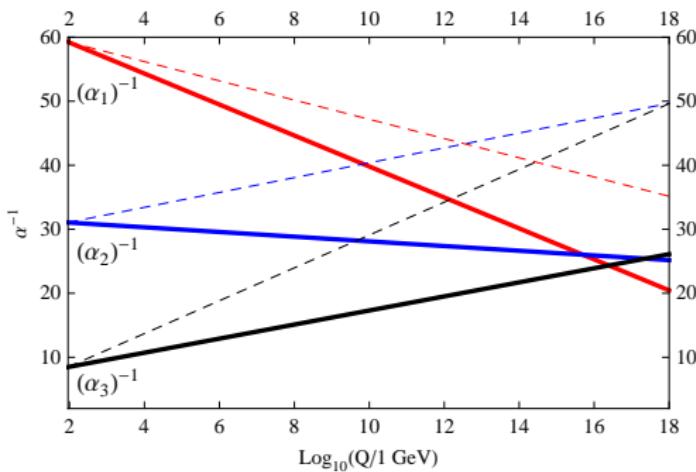


Figure: RGE of α_i^{-1} in SM (dashed) and MSSM (solid)

Dark Matter, Triggering EWSB

- In R -parity conserving SUSY, LSP is DM candidate

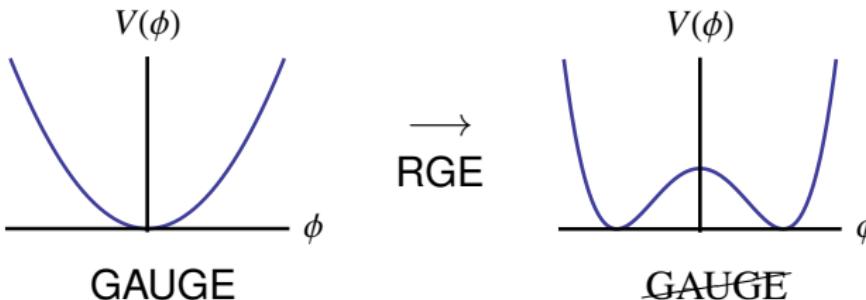
$$\begin{array}{lcl} \text{Gauge Mediated SUSY} & \rightarrow & \tilde{G} \\ \text{Gravity Mediated SUSY} & \rightarrow & \tilde{\chi}_1^0 \end{array}$$

Dark Matter, Triggering EWSB

- In R -parity conserving SUSY, LSP is DM candidate

$$\begin{array}{lcl} \text{Gauge Mediated SUSY} & \rightarrow & \tilde{G} \\ \text{Gravity Mediated SUSY} & \rightarrow & \tilde{\chi}_1^0 \end{array}$$

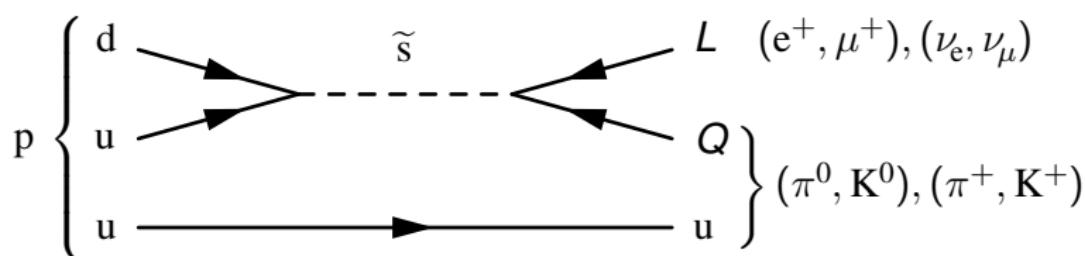
- Renormalization Group Evolution (RGE) triggers EWSB



Dark Matter Candidate

Proton decay

- General MSSM \implies rapid proton decay



- Forbid these interactions by imposing symmetries

Dark Matter Candidate

R-parity

- Define a multiplicatively conserved quantum number P_R
- Let all (supersymmetric) particles have $P_R = (-1)^{\text{L}}$

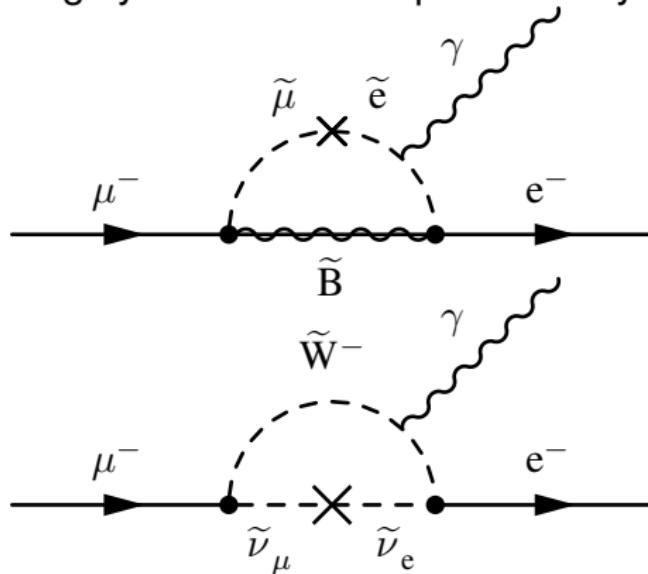


- Interaction vertices contain even numbers of superpartners
- Forbids process mediating rapid proton decay
- The lightest supersymmetric particle (LSP) is stable

Dark matter candidate!

Flavour Changing Neutral Currents

- $\mu^- \rightarrow e^- \gamma$ is highly constrained experimentally



- Forbid/suppress the additional loop processes from SUSY

Pros and Cons

Advantages

- Flavour-blind communication automatic
- Theory is renormalizable

Pros and Cons

Advantages

- Flavour-blind communication automatic
- Theory is renormalizable

Problems

- Higgs ' b ' term difficult to generate
- LSP is always gravitino

Flavour Universality

$$-\mathcal{L}_{\text{soft}}^{\text{MSSM}} \subset \sum_{\phi=Q,L,\bar{u},\bar{d},e} \tilde{\phi}^\dagger m_\phi^2 \tilde{\phi} + \left(\tilde{u} a_u \tilde{Q} H_u - \tilde{d} a_d \tilde{Q} H_d - \tilde{e} a_e \tilde{L} H_d + \text{h.c.} \right)$$

Easiest way:

- Assume supersymmetry breaking is ‘universal’

$$(m_i)_{jk} = m_i \delta_{jk}, \quad i = (Q, L, u, d, e)$$

- Assume that the (scalar)³ couplings are \propto the corresponding Yukawa couplings

$$a_i \propto y_i, \quad i = (u, d, e)$$

Consequences

We find...

At any RG scale, the squark and slepton mass matrices appear

$$\left(m_\phi^2\right)_{ij} \approx \begin{pmatrix} m_{\phi_1}^2 & 0 & 0 \\ 0 & m_{\phi_1}^2 & 0 \\ 0 & 0 & m_{\phi_3}^2 \end{pmatrix}_{ij} \quad \phi = (Q, L, u, d, e)$$

How to Communicate SUSY

Tree-level?

- For tree-level renormalizable couplings

$$\text{STr}\mathcal{M}^2 = \sum_J (-1)^{2J} (2J+1) \mathcal{M}_J^2 = 0,$$



superpartner lighter than SM counterpart

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- Non-renormalizable \implies Planck-Scale Mediated SUSY
- Non-tree-level \implies Gauge Mediated SUSY (GMSB)

Minimal Model

Content

- Extra field content

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
Φ	\square	\square	$-\frac{1}{3}$
$\bar{\Phi}$	$\bar{\square}$	$\bar{\square}$	$+\frac{1}{3}$
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- Superpotential

$$W = \lambda \bar{\Phi} X \Phi$$

- X is goldstino superfield

$$\langle X \rangle = M + \theta^2 F$$

MSSM Soft Lagrangian

The most general set of positive mass dimension terms who obey SM symmetries but break SUSY are

$$\begin{aligned}\mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left(M_3 \tilde{g}\tilde{g} + M_2 \tilde{W}\tilde{W} + M_1 \tilde{B}\tilde{B} + \text{c.c.} \right) \\ & - \left(\tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.} \right) \\ & - \tilde{Q}^\dagger \mathbf{m}_Q^2 \tilde{Q} - \tilde{L}^\dagger \mathbf{m}_L^2 \tilde{L} - \tilde{u} \mathbf{m}_u^2 \tilde{u}^\dagger - \tilde{d} \mathbf{m}_d^2 \tilde{d}^\dagger - \tilde{e} \mathbf{m}_e^2 \tilde{e}^\dagger \\ & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.}),\end{aligned}$$

and form the soft supersymmetry breaking Lagrangian density