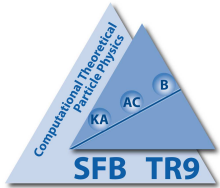


NLO, HIGGS AND OTHER THEORY ISSUES: WORKSHOP CLOSING TALK



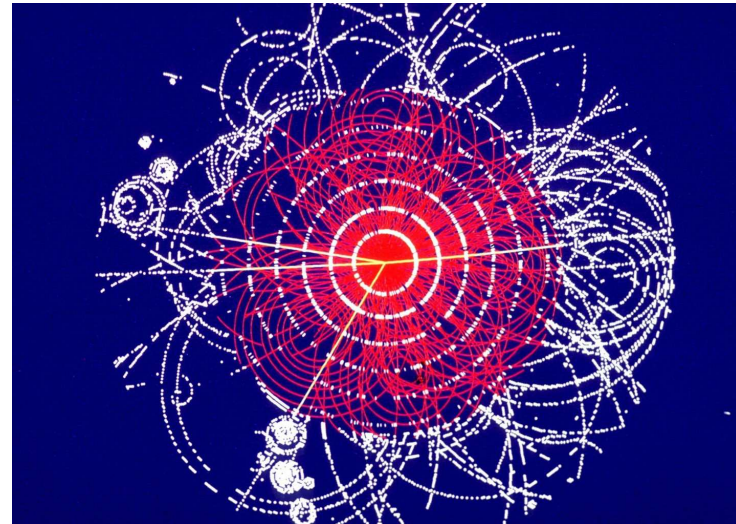
Dieter Zeppenfeld
Karlsruhe Institute of Technology (KIT)



Bundesministerium
für Bildung
und Forschung

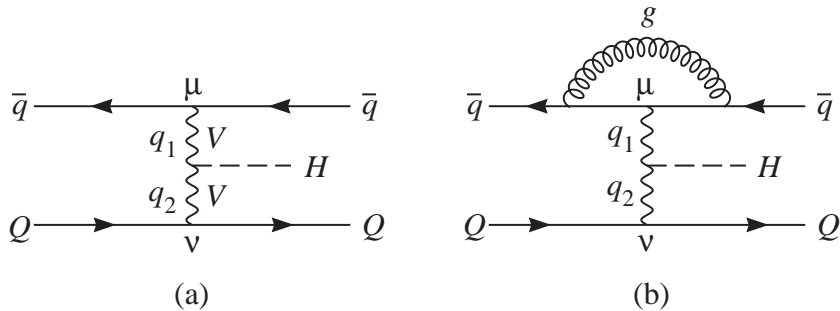
Theory Experiment Interplay at the LHC, April 8–9, 2010, RHUL

- Higgs + 2 Jets
- NLO QCD
- VBFNLO
- Conclusions



Tensor structure of the HVV coupling

Most general HVV vertex $T^{\mu\nu}(q_1, q_2)$



Physical interpretation of terms:

SM Higgs $\mathcal{L}_I \sim HV_\mu V^\mu \longrightarrow a_1$

loop induced couplings for neutral scalar

CP even $\mathcal{L}_{eff} \sim HV_{\mu\nu} V^{\mu\nu} \longrightarrow a_2$

CP odd $\mathcal{L}_{eff} \sim HV_{\mu\nu} \tilde{V}^{\mu\nu} \longrightarrow a_3$

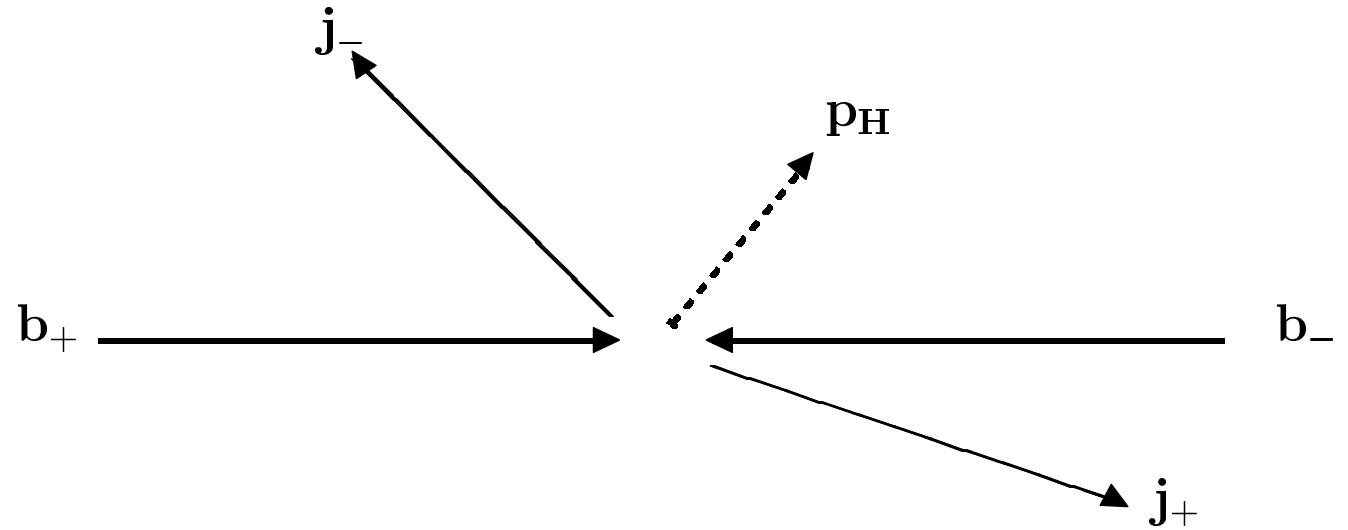
Must distinguish a_1, a_2, a_3 experimentally

$$T^{\mu\nu} = a_1 g^{\mu\nu} + a_2 (q_1 \cdot q_2 g^{\mu\nu} - q_1^\nu q_2^\mu) + a_3 \varepsilon^{\mu\nu\rho\sigma} q_{1\rho} q_{2\sigma}$$

The $a_i = a_i(q_1, q_2)$ are scalar form factors

Azimuthal angle distribution and Higgs CP properties

Kinematics of Hjj event:



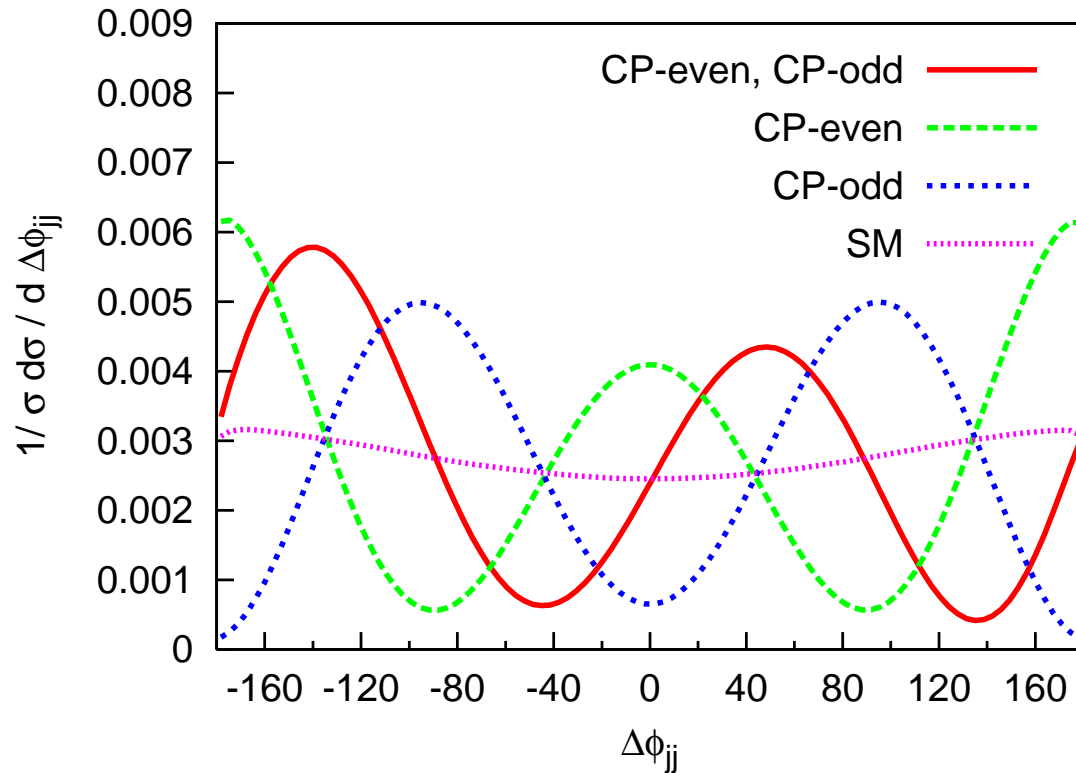
Define azimuthal angle between jet momenta j_+ and j_- via

$$\epsilon_{\mu\nu\rho\sigma} b_+^\mu j_+^\nu b_-^\rho j_-^\sigma = 2p_{T,+} p_{T,-} \sin(\phi_+ - \phi_-) = 2 p_{T,+} p_{T,-} \sin \Delta\phi_{jj}$$

- $\Delta\phi_{jj}$ is a parity odd observable
- $\Delta\phi_{jj}$ is invariant under interchange of beam directions $(b_+, j_+) \leftrightarrow (b_-, j_-)$

Work with Vera Hankele, Gunnar Klämke and Terrance Figy: [hep-ph/0609075](https://arxiv.org/abs/hep-ph/0609075)

Signals for CP violation in the Higgs Sector



mixed CP case:

$$a_2 = a_3, a_1 = 0$$

pure CP-even case:

a_2 only

pure CP odd case:

a_3 only

Position of **minimum of $\Delta\phi_{jj}$ distribution** measures relative size of CP-even and CP-odd couplings. For

$$a_1 = 0,$$

$$a_2 = d \sin \alpha,$$

$$a_3 = d \cos \alpha,$$

\Rightarrow **Minimum at $-\alpha$ and $\pi - \alpha$**

Gluon Fusion as a signal channel

Heavy quark loop induces effective Hgg vertex:

$$\text{CP – even :} \quad i \frac{m_Q}{v} \rightarrow \mathcal{L}_{eff} = \frac{\alpha_s}{12\pi v} H G_{\mu\nu}^a G^{\mu\nu,a}$$

$$\text{CP – odd :} \quad - \frac{m_Q}{v} \gamma_5 \rightarrow \mathcal{L}_{eff} = \frac{\alpha_s}{8\pi v} A G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} = \frac{\alpha_s}{16\pi v} A G_{\mu\nu}^a G_{\alpha\beta}^a \varepsilon^{\mu\nu\alpha\beta}$$

Azimuthal angle between tagging jets probes difference

- Use gluon fusion induced Φjj signal to probe structure of Hgg vertex
- Measure size of coupling (requires NLO corrections for precision)
- Find **cuts** to enhance gluon fusion over VBF and other backgrounds

\implies Study by **Gunnar Klämke** in $m_Q \rightarrow \infty$ limit (hep-ph/0703202, PhD thesis, and paper in preparation, with **Michael Rauch**)

Gluon fusion signal and backgrounds

Signal channel (LO):

- $pp \rightarrow Hjj$ in gluon fusion with $H \rightarrow W^+W^- \rightarrow l^+l^-\nu\bar{\nu}$, ($l = e, \mu$)
- $m_H = 160 \text{ GeV}$

dominant backgrounds:

- W^+W^- -production via VBF (including Higgs-channel): $pp \rightarrow W^+W^-jj$
- top-pair production: $pp \rightarrow t\bar{t}, t\bar{t}j, t\bar{t}jj$ (N. Kauer)
- QCD induced W^+W^- -production: $pp \rightarrow W^+W^-jj$

applied inclusive cuts (minimal cuts):

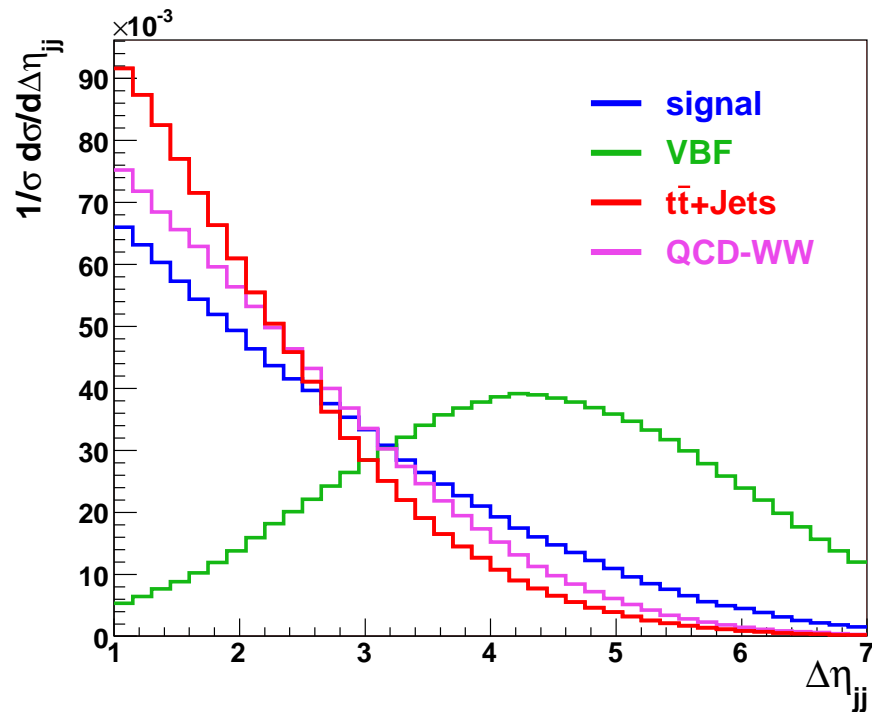
- 2 tagging-jets
 $p_{Tj} > 30 \text{ GeV}, \quad |\eta_j| < 4.5$
- 2 identified leptons
 $p_{Tl} > 10 \text{ GeV}, \quad |\eta_l| < 2.5$
- separation of jets and leptons
 $\Delta\eta_{jj} > 1.0, \quad R_{jl} > 0.7$

process	σ [fb]
GF $pp \rightarrow H + jj$	115.2
VBF $pp \rightarrow W^+W^- + jj$	75.2
$pp \rightarrow t\bar{t}$	6832
$pp \rightarrow t\bar{t} + j$	9518
$pp \rightarrow t\bar{t} + jj$	1676
QCD $pp \rightarrow W^+W^- + jj$	363

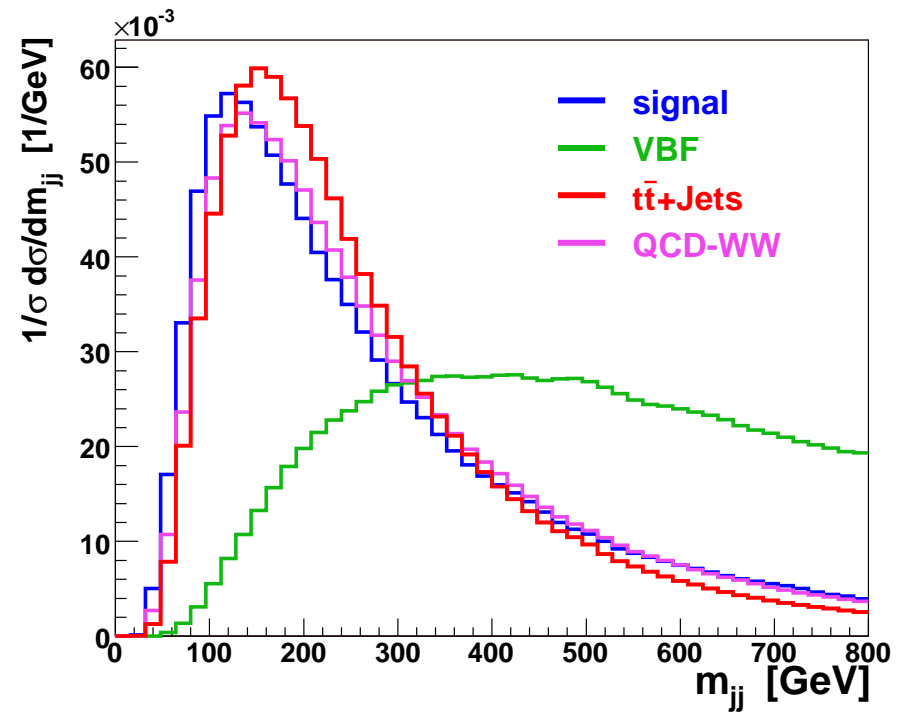
Characteristic distributions

Separation of **VBF Hjj signal** from QCD background is much easier than separation of **gluon fusion Hjj signal**

tagging jet rapidity separation



dijet invariant mass



Selection continued

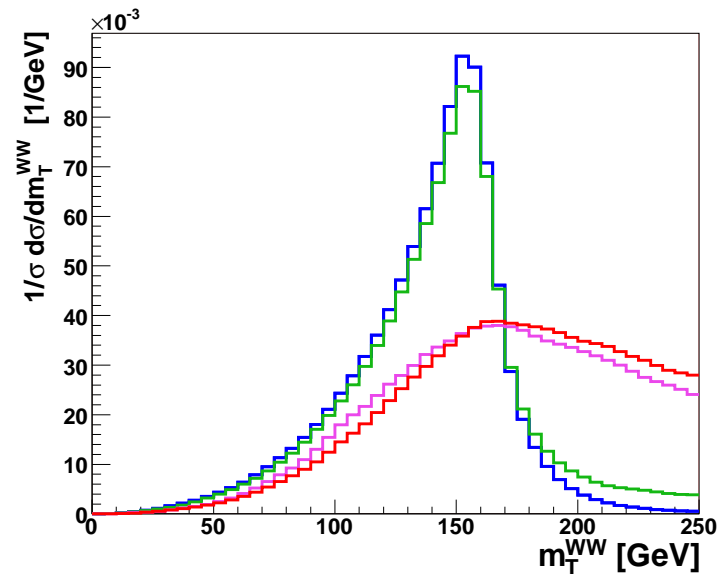
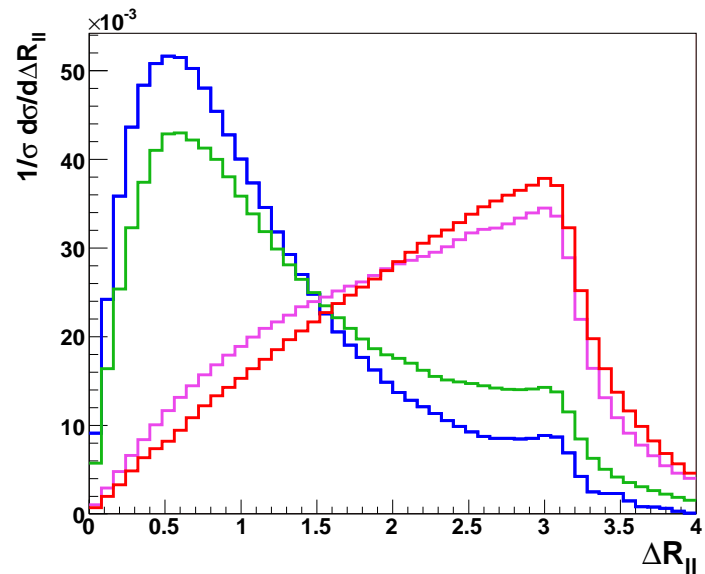
- **b-tagging** for reduction of top-backgrounds. *(CMS Note 06/014)*
 - (η, p_T) - dependent tagging-efficiencies (60% - 75%) with 10% mistagging - probability

- selection cuts:

$$p_{Tl} > 30 \text{ GeV}, \quad M_{ll} < 75 \text{ GeV}, \quad M_{ll} < 0.44 \cdot M_T^{WW}, \quad R_{ll} < 1.1,$$

$$M_T^{WW} < 170 \text{ GeV}, \quad \cancel{p}_T > 30 \text{ GeV}$$

$$M_T^{WW} = \sqrt{(\cancel{E}_T + E_{Tll})^2 - (\vec{\cancel{p}}_T + \vec{p}_{Tll})^2}$$



signal
VBF
 $t\bar{t}$ +Jets
QCD-WW

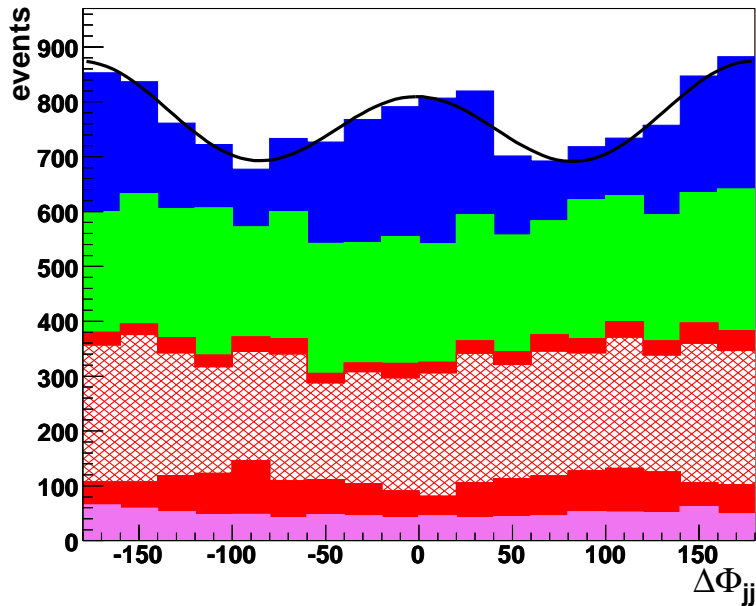
Results

process	σ [fb]	events/ 30 fb^{-1}
GF $pp \rightarrow H + jj$	31.5	944
VBF $pp \rightarrow W^+W^- + jj$	16.5	495
$pp \rightarrow t\bar{t}$	23.3	699
$pp \rightarrow t\bar{t} + j$	51.1	1533
$pp \rightarrow t\bar{t} + jj$	11.2	336
QCD $pp \rightarrow W^+W^- + jj$	11.4	342
Σ backgrounds	113.5	3405

$$\Rightarrow \mathbf{S/\sqrt{B} \approx 16.2 \text{ for } 30 \text{ fb}^{-1}}$$

$\Delta\Phi_{jj}$ -Distribution in gluon fusion: WW case

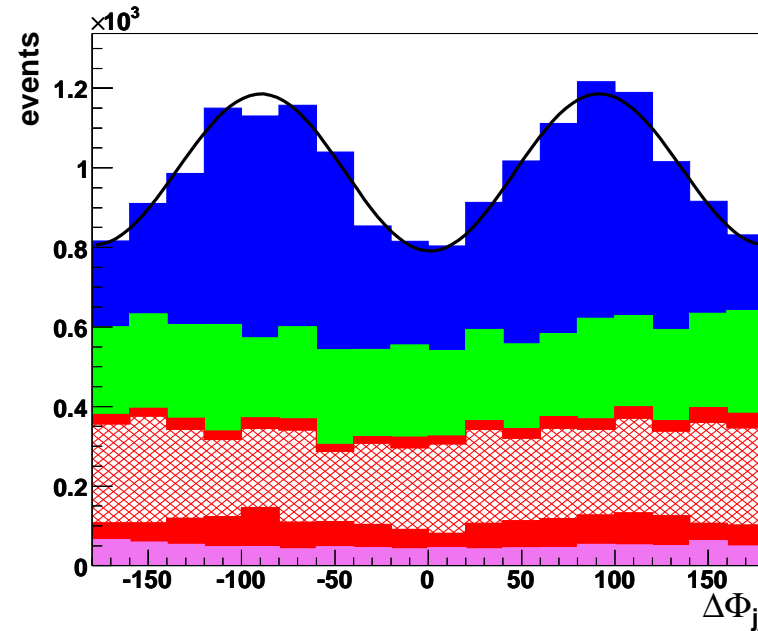
Fit to Φ_{jj} -distribution with function $f(\Delta\Phi) = N(1 + A \cos[2(\Delta\Phi - \Delta\Phi_{max})] - B \cos(\Delta\Phi))$



CP-even

$$A = 0.100 \pm 0.039$$

$$\Delta\Phi_{max} = 5.8 \pm 15.3$$



CP-odd

$$A = 0.199 \pm 0.034$$

$$\Delta\Phi_{max} = 93.7 \pm 5.1$$

Signal

VBF

$t\bar{t}$ +Jets

QCD-WW

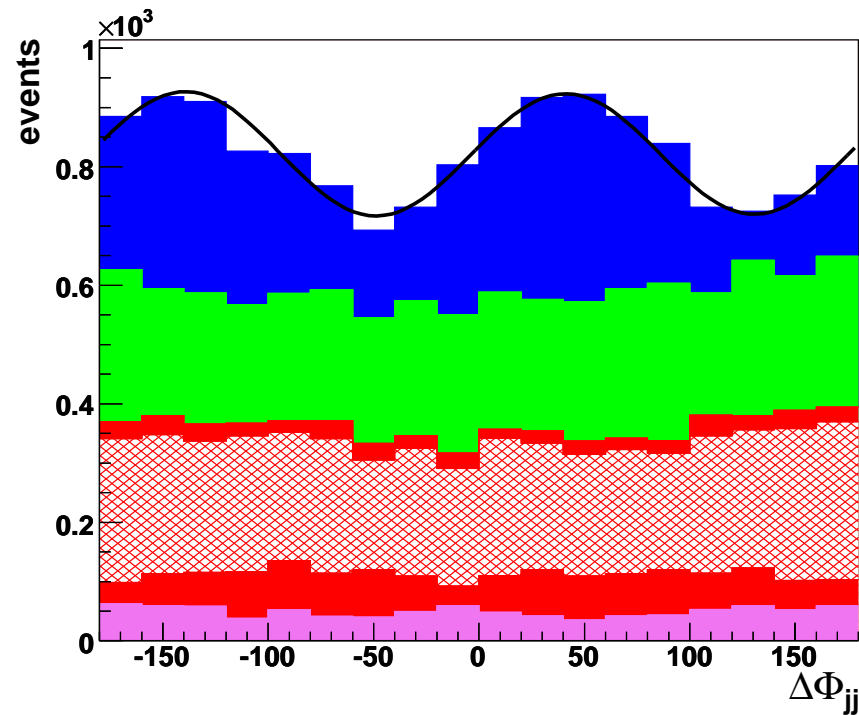
$L = 300 \text{ fb}^{-1}$

$(\Delta\eta_{jj} > 3.0)$

fit of the background only : $A = 0.069 \pm 0.044$ and $\Delta\Phi_{max} = 64 \pm 25$

(mean values of 10 independent fits of data for $L = 30 \text{ fb}^{-1}$ each)

$\Delta\Phi_{jj}$ -Distribution: CP violating case



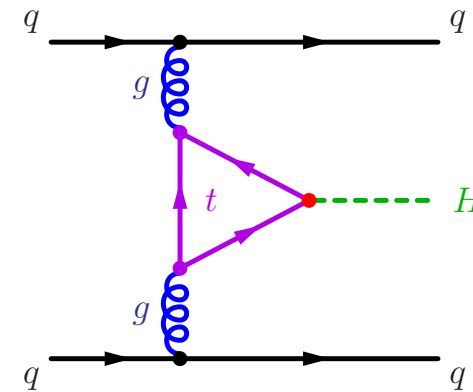
CP-mixture: equal CP-even and CP-odd contributions

$$A = 0.153 \pm 0.037$$

$$\Delta\Phi_{max} = 45.6 \pm 7.3$$

Higgs + 2 Jets in Gluon Fusion, $H \rightarrow \tau\tau \rightarrow \ell^+ \ell^- \nu \bar{\nu}$

- this channel has not been studied so far
- interesting for SM Higgs (≈ 120 GeV) and SUSY scenario with large $\tan \beta$ ($m_H \approx m_A \gtrsim 150$ GeV)
- x-section times branching ratio of ≈ 50 fb looks promising (SM)
- has potential for study of Higgs CP-properties



Studied so far (by [Gunnar Klämke](#)):

- Study of signal and SM backgrounds for $m_H = 120$ GeV case (simple cut based analysis)
- same for one MSSM scenario $m_A = 200$ GeV, $\tan \beta = 50$

Questions:

- How many signal and background events are there after cuts (what's the statistical significance)
- What are the prospects of CP-measurements via jet-jet azimuthal angle correlation

finite detector resolution

The detector has a finite resolution. The measured jet energy and missing transverse energy have large uncertainties. Parameterization (from CMS NOTE 2006/035, CMS NOTE 2006/036):

Jets :

$$\frac{\Delta E_j}{E_j} = \left(\frac{a}{E_{Tj}} \oplus \frac{b}{\sqrt{E_{Tj}}} \oplus c \right)$$

	a	b	c
$\eta_j < 1.4$	5.6	1.25	0.033
$1.4 < \eta_j < 3$	4.8	0.89	0.043
$\eta_j > 3$	3.8	0	0.085

Leptons :

$$\frac{\Delta E_\ell}{E_\ell} = 2\%$$

Missing p_T :

$$\Delta \cancel{p}_x = 0.46 \cdot \sqrt{\sum E_{Tj}}$$

SM Higgs with 120 GeV mass

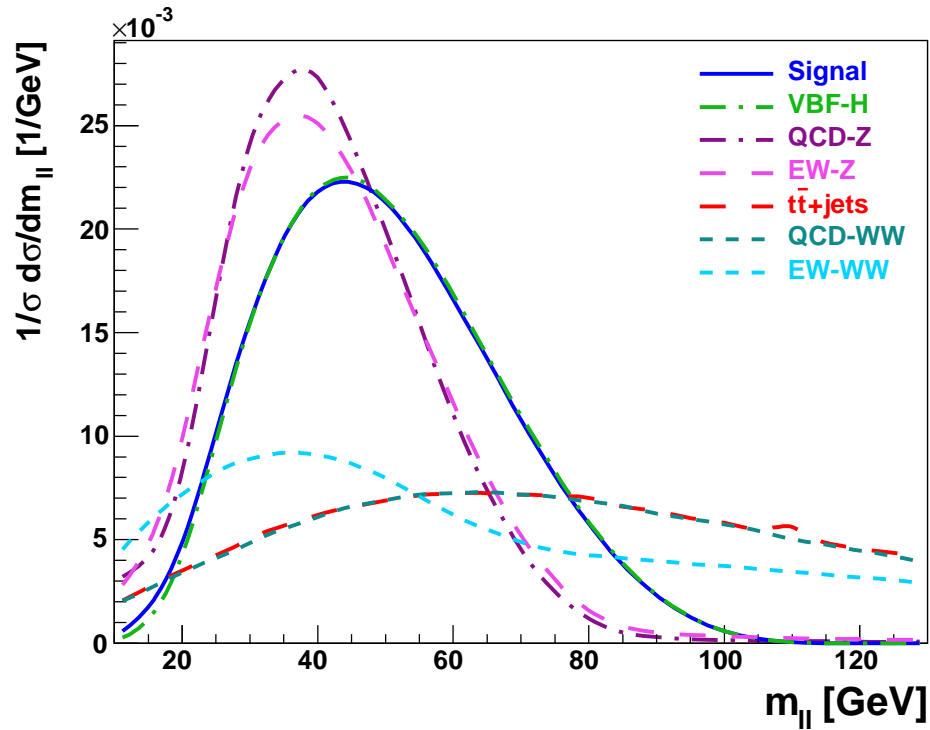
inclusive cuts

$$p_{T,jets} > 30 \text{ GeV}, \quad p_{T,\ell} > 10 \text{ GeV}, \quad |\eta_j| < 4.5, \quad |\eta_\ell| < 2.5, \quad \Delta\eta_{jj} > 1.0, \quad \Delta R_{j\ell} > 0.7,$$

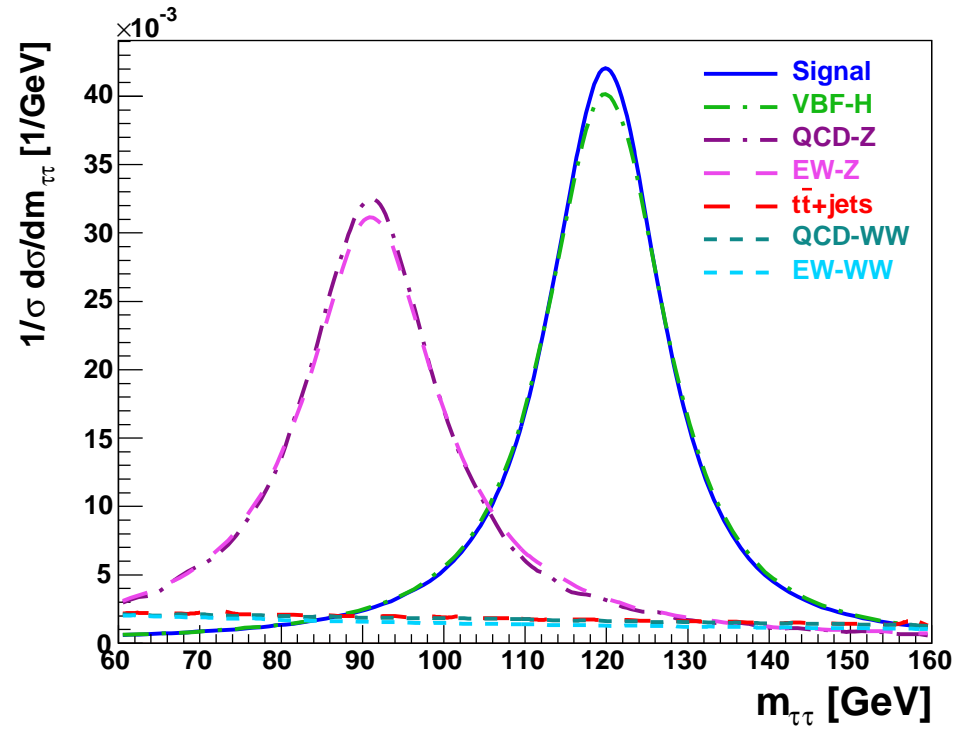
cross sections for inclusive cuts for signal and background

process	σ [fb]	events / 600 fb ⁻¹
GF $pp \rightarrow H + jj \rightarrow \tau\tau jj$	11.283	6770
GF $pp \rightarrow A + jj \rightarrow \tau\tau jj$	25.00	15002
VBF $pp \rightarrow H + jj \rightarrow \tau\tau jj$	5.527	3316
QCD $pp \rightarrow Z + jj \rightarrow \tau\tau jj$	1652.8	991700
VBF $pp \rightarrow Z + jj \rightarrow \tau\tau jj$	15.70	9418
$pp \rightarrow t\bar{t}$	6490	3893900
$pp \rightarrow t\bar{t} + j$	9268	5560890
$pp \rightarrow t\bar{t} + jj$	1629	977263
QCD $pp \rightarrow W^+W^- + jj$	334.2	200540
VBF $pp \rightarrow W^+W^- + jj$	24.78	14871

Distributions



dilepton invariant mass



reconstructed $\tau\tau$ invariant mass

selection cuts

a b-veto was applied to reduce the top backgrounds.

$$R_{\ell\ell} < 2.4, \quad \cancel{p}_T > 30 \text{ GeV}, \quad m_{\ell\ell} < 80 \text{ GeV}, \quad 110 \text{ GeV} < m_{\tau\tau} < 135 \text{ GeV}, \quad 0 < x_i < 1$$

process	σ [fb]	events / 600 fb ⁻¹
GF $pp \rightarrow H + jj \rightarrow \tau\tau jj$	4.927	2956
GF $pp \rightarrow A + jj \rightarrow \tau\tau jj$	11.43	6860
VBF $pp \rightarrow H + jj \rightarrow \tau\tau jj$	2.523	1514
QCD $pp \rightarrow Z + jj \rightarrow \tau\tau jj$	27.62	16573
VBF $pp \rightarrow Z + jj \rightarrow \tau\tau jj$	0.475	285
$pp \rightarrow t\bar{t}$	3.86	2316
$pp \rightarrow t\bar{t} + j$	8.84	5306
$pp \rightarrow t\bar{t} + jj$	3.8	2283
QCD $pp \rightarrow W^+W^- + jj$	1.48	887
VBF $pp \rightarrow W^+W^- + jj$	0.147	88
Σ backgrounds	48.84	29300

for cp-even higgs: $S/\sqrt{B} \approx 17$ (600 fb⁻¹)

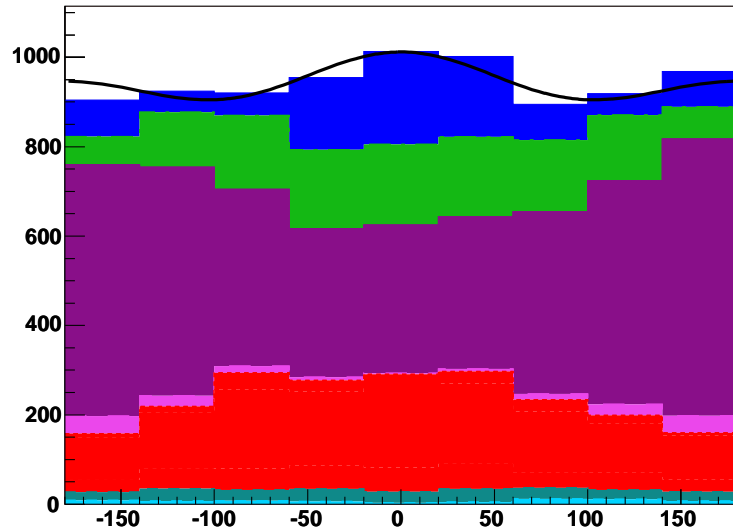
this corresponds to: $S/\sqrt{B} \approx 5$ (50 fb⁻¹)

for cp-odd higgs: $S/\sqrt{B} \approx 40$ (600 fb⁻¹)

this corresponds to: $S/\sqrt{B} \approx 5$ (10 fb⁻¹)

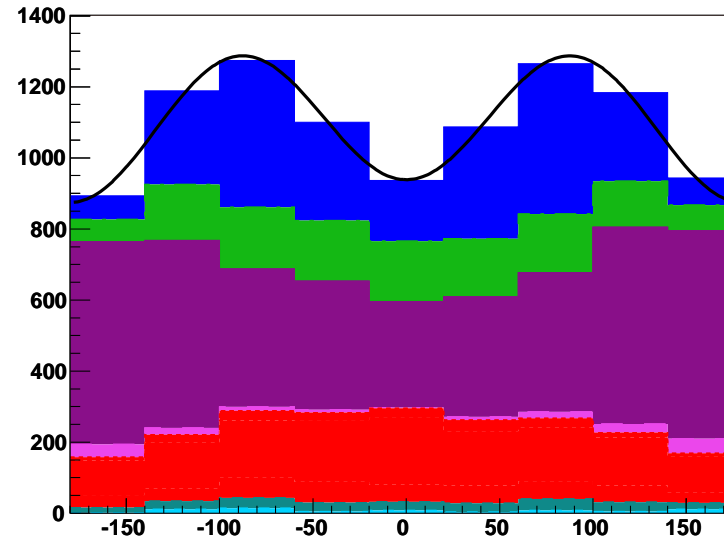
$H \rightarrow \tau\tau$ case: $\Delta\Phi_{jj}$ -distribution with backgrounds

Fit to Φ_{jj} -distribution with function $f(\Delta\Phi) = N(1 + A \cos[2(\Delta\Phi)] - B \cos(\Delta\Phi))$



CP-even

$$A = 0.004 \pm 0.015$$



CP-odd

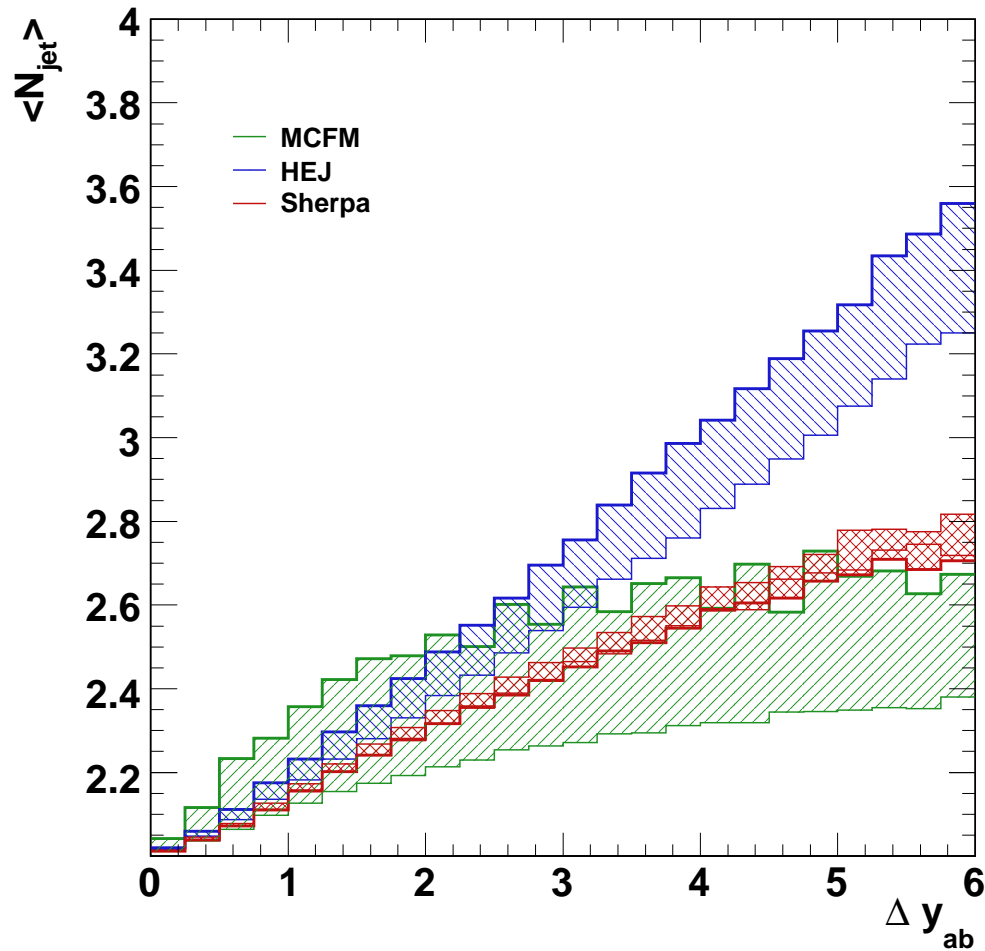
$$A = -0.161 \pm 0.014$$

Signal
VBF-H
QCD-Z
EW-Z
 $t\bar{t}$ +Jets

$L = 600 \text{ fb}^{-1}$
 $(\Delta\eta_{jj} > 3.0)$

fit of the background only : -0.043 ± 0.016
 \Rightarrow significance for CP-even vs. CP-odd ≈ 8

Improvements for multijet situation: Jeppe Andersen

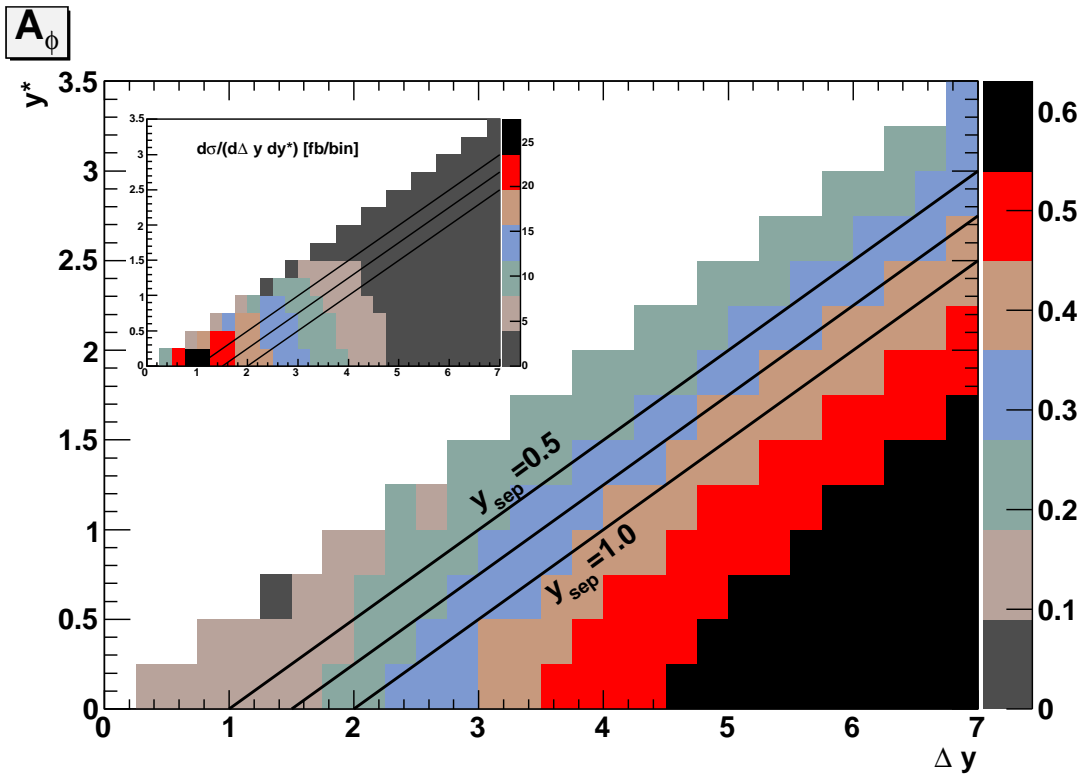


Large probability for additional jets between most forward and backward jets (of $E_T > 40$ GeV)

Define $\Delta\Phi_{jj}$ in terms of jet clusters on either side of Higgs

Quality of $\Delta\Phi_{jj}$ correlation largely preserved in multijet situation

Strong rapidity ordering



Alternative rapidity cuts on jets:

$$\min\{|y_j - y_H|\} > y_{sep} \quad \text{instead of} \quad \Delta y = |y_{j_1} - y_{j_2}| > 3$$

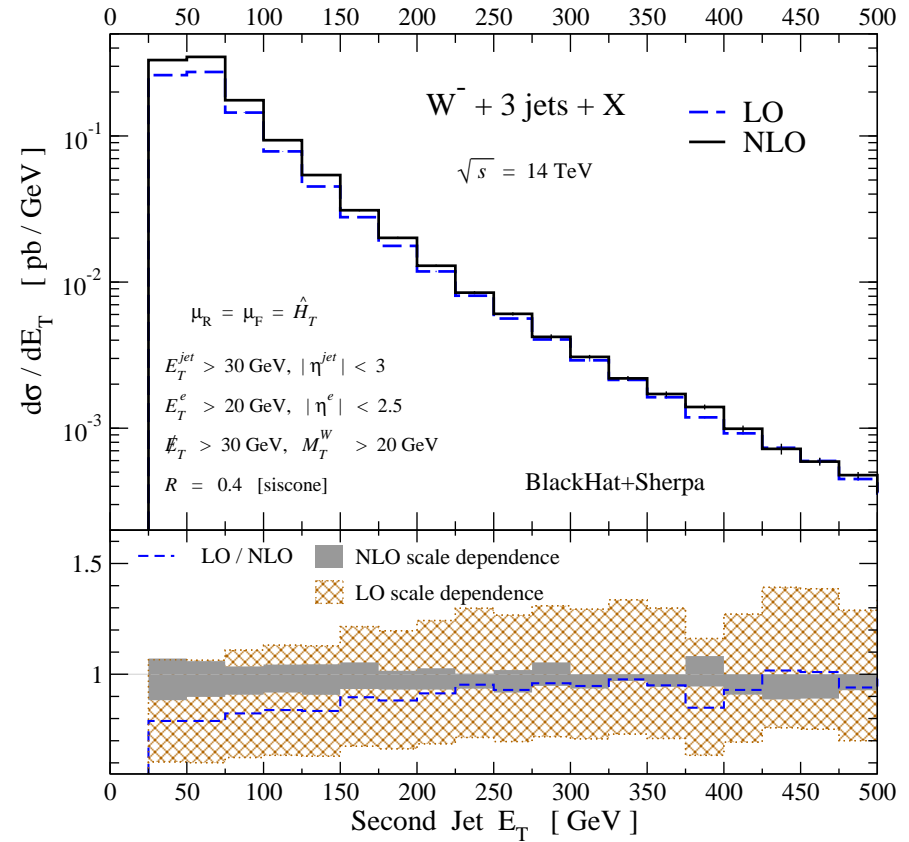
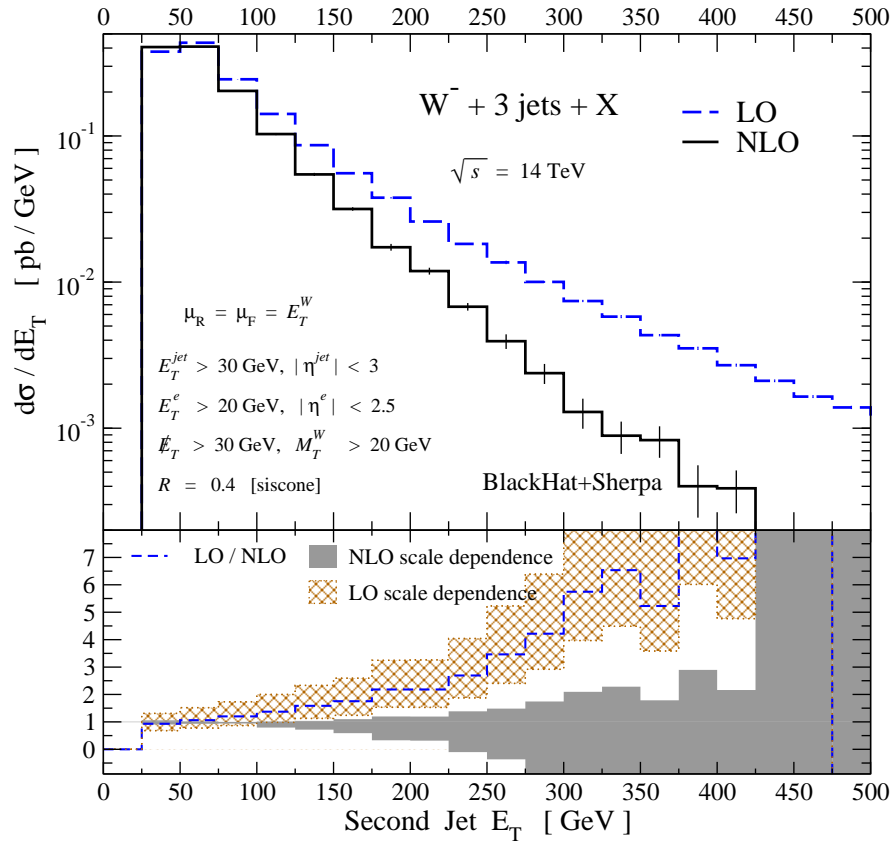
little effect on significance of azimuthal correlations once backgrounds are taken into account

Progress on calculation tools

- **Alexander Belyaev:** tutorial on Calcchep
great tree level tool for studying SM processes and beyond
- **Frank Krauss:** progress on Sherpa
- **Chris White:** $t\bar{t}$ vs Wt production
- **Mark Rodgers:** how to calculate multileg loops with GOLEM
impressive tool for calculating pentagons and hexagons
applications to ZZj production and neutralino pair production
- **Darren Forde:** automated loop calculations with Blackhat
Application: $W + 3$ jets and $Z + 3$ jets
- **Giulia Zanderighi:** $W + 3$ jets at NLO
Phenomenological studies

Scale choice in $W + 3$ Jet events at LHC: Blackhat...

Consider E_T distribution of second jet (Darren Forde)

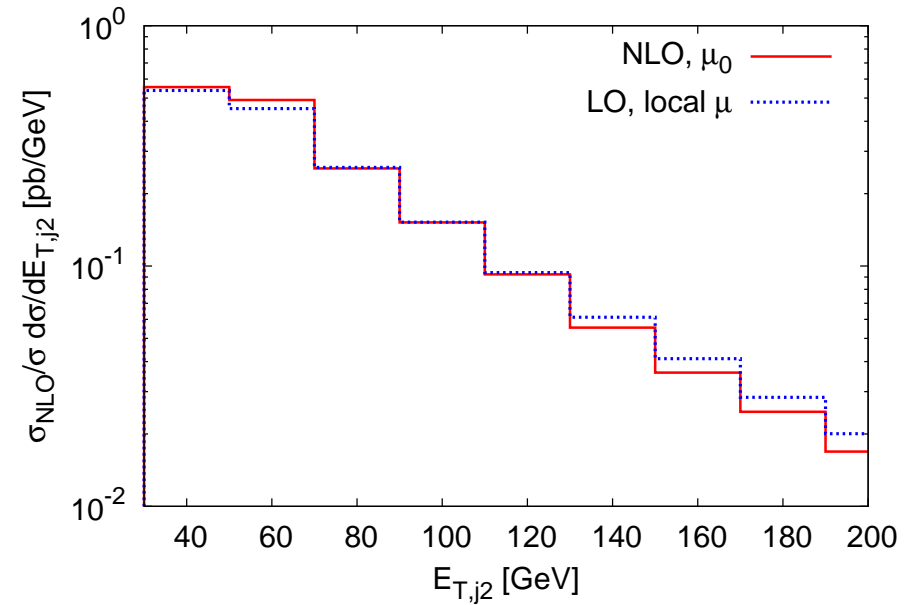
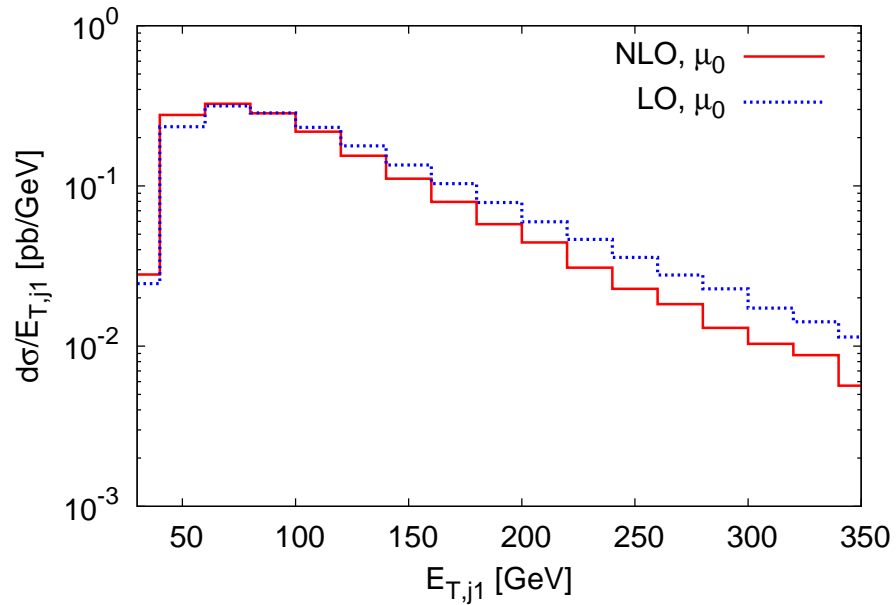


very large NLO scale dependence for $\mu = x \cdot E_{TW}$

Caution: Small scale dependence with $\mu_0 = H_T$ gives underestimate of NLO error

... and using Rocket science

Jet E_T distributions of two leading jets (Giulia Zanderighi)



Blackhat uses $\mu_0 = E_{TW}$: no sign for huge NLO corrections?

Avoid large K-factors in distributions by choosing local scale in LO results (inspired by k_T clustering)

Progress on VBFNLO

Originally: NLO QCD predictions for vector boson fusion processes at the LHC:

$qq \rightarrow qqH$ Han, Valencia, Willenbrock (1992); Figy, Oleari, DZ (2003); Campbell, Ellis, Berger (2004)

- Higgs coupling measurements

$qq \rightarrow qqZ$ and $qq \rightarrow qqW$ Oleari, DZ: hep-ph/0310156

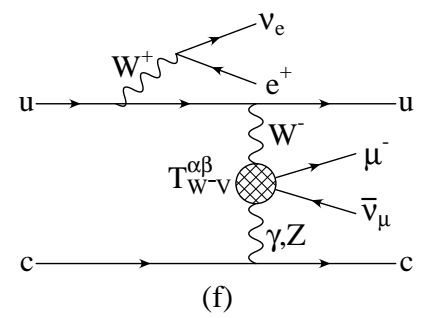
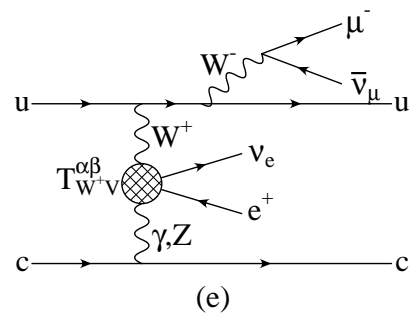
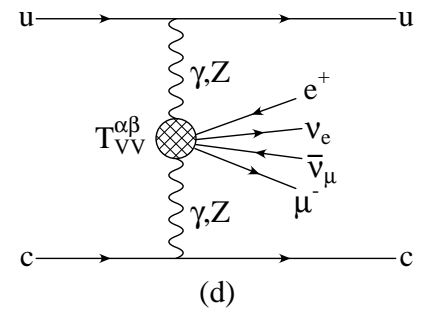
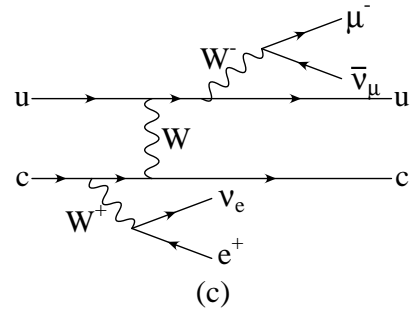
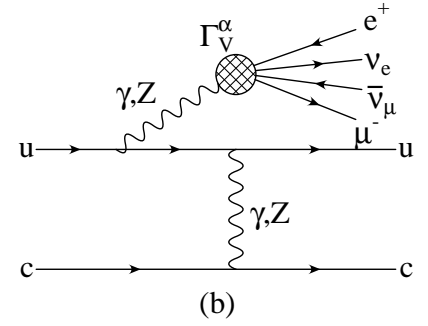
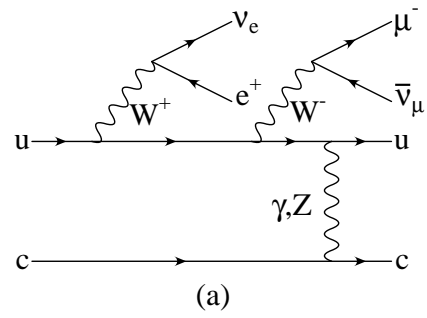
- $Z \rightarrow \tau\tau$ as background for $H \rightarrow \tau\tau$
- measure central jet veto acceptance at LHC

$qq \rightarrow qqWW, qq \rightarrow qqZZ, qq \rightarrow qqWZ$ Jäger, Oleari, Bozzi, DZ: hep-ph/0603177,
hep-ph/0604200, hep-ph/0701105, arXiv:0907.0580

- $qqWW$ is background to $H \rightarrow WW$ in VBF
- underlying process is weak boson scattering: $WW \rightarrow WW, WW \rightarrow ZZ, WZ \rightarrow WZ$ etc.

$qq \rightarrow qqVV$: 3 weak bosons on a quark line

- NLO corrections to $qq \rightarrow qqVV$ contain all loops with a virtual gluon attached to a quark line with one, two or three weak bosons
- Crossing and replacing one quark line by a lepton line yields $q\bar{q} \rightarrow VVV$ production processes with leptonic decays of the weak bosons
- Recycle virtual contributions from NLO corrections to VBF
- Decompose calculation into modules which can be used in different NLO calculations



Extending VBFNLO: VVV and VVj Production at NLO QCD

New processes implemented in 2008 release of VBFNLO:

- Triple weak boson production: $VVV = W^\pm W^\mp W^\pm$, W^+W^-Z and $W^\pm ZZ$ with leptonic decay of the weak bosons and full $H \rightarrow WW$ and $H \rightarrow ZZ$ contributions
Work in collaboration with V. Hankele, S. Prestel, C. Oleari and F. Campanario

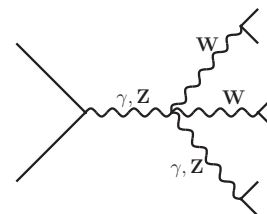
New processes already available for future releases:

- $W^+W^-\gamma$ and $ZZ\gamma$ production with leptonic decay of weak bosons
Work in collaboration with G. Bozzi and F. Campanario
- $W^\pm\gamma j$ production (with W leptonic decay and final state photon radiation)
Work in collaboration with C. Englert, F. Campanario and M. Spannowsky

Code is available at <http://www-itp.particle.uni-karlsruhe.de/~vbfnlweb>

VVV Production: Motivation

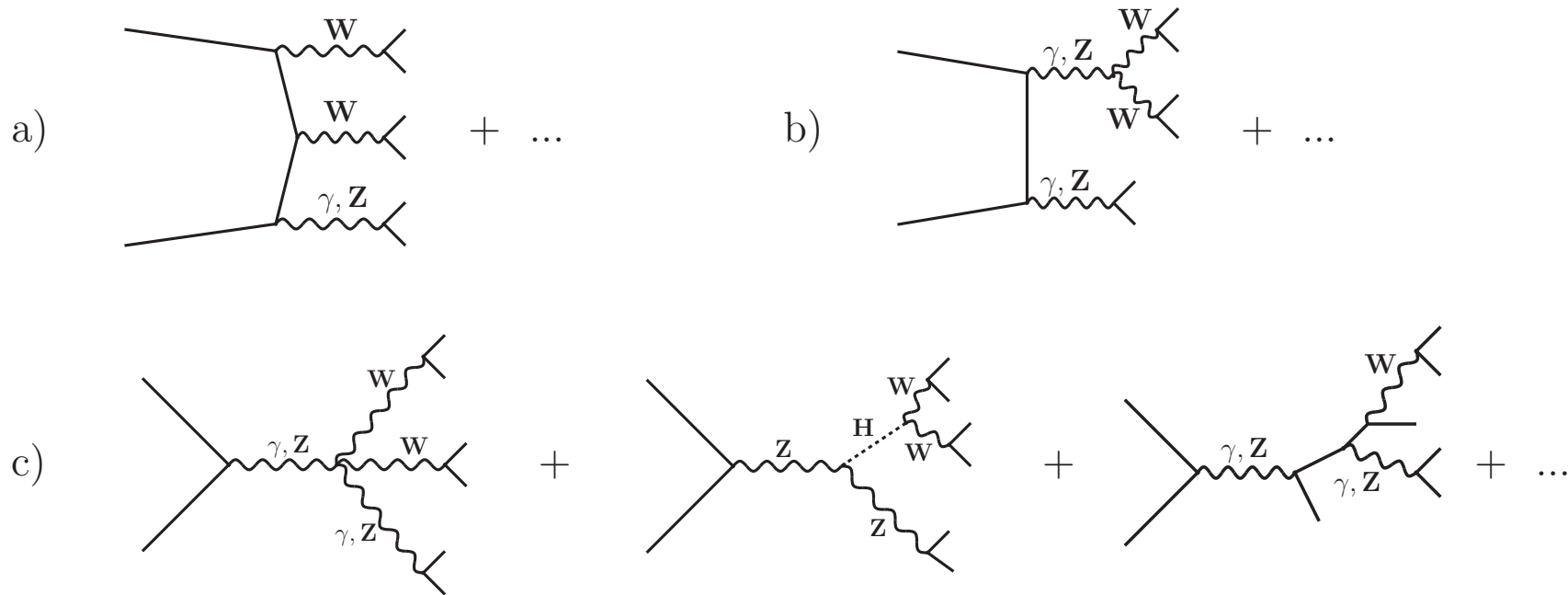
- Standard Model background for SUSY processes with multi-lepton + \cancel{p}_T signature
- Possibility to obtain information about quartic electroweak couplings.



- QCD corrections to $pp \rightarrow VVV + X$ on experimentalist's wishlist:
[The QCD, EW, and Higgs Working Group: hep-ph/0604120]

process ($V \in \{Z, W, \gamma\}$)	relevant for
1. $pp \rightarrow V V \text{ jet}$	$t\bar{t}H$, new physics
2. $pp \rightarrow t\bar{t} b\bar{b}$	$t\bar{t}H$
3. $pp \rightarrow t\bar{t} + 2 \text{ jets}$	$t\bar{t}H$
4. $pp \rightarrow V V b\bar{b}$	VBF $\rightarrow H \rightarrow VV$, $t\bar{t}H$, new physics
5. $pp \rightarrow V V + 2 \text{ jets}$	VBF $\rightarrow H \rightarrow VV$
6. $pp \rightarrow V + 3 \text{ jets}$	various new physics signatures
7. $pp \rightarrow V V V$	SUSY trilepton

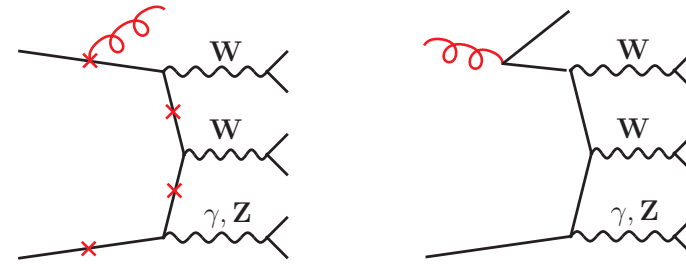
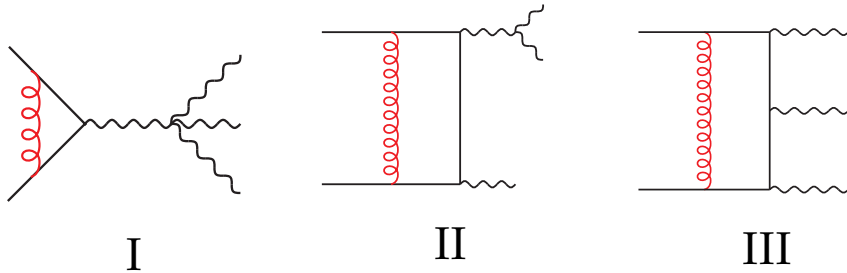
Example: Contributions to WWZ production



- All resonant and non-resonant matrix elements as well as spin correlations of final state leptons and Higgs contribution included.
- Interference terms due to identical particles in the final state have been neglected.
- All fermion mass effects neglected. ($H\tau\tau$ -coupling = 0)

1-loop matrix elements and real emission matrix elements

Three different topologies:

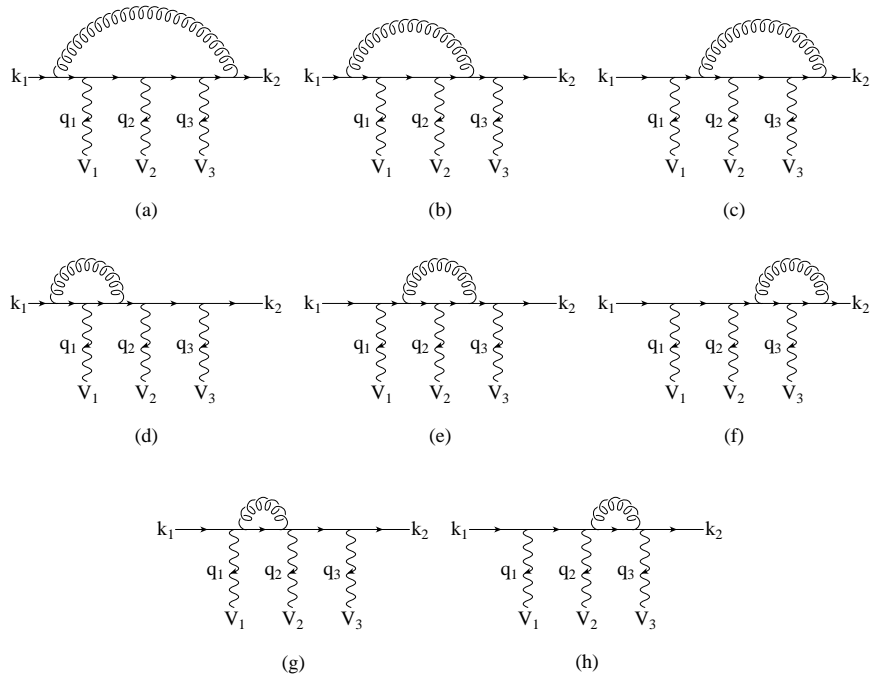


- I Vertex correction proportional to Born matrix element.
- II Maximally 4-point integrals appear.
- III Up to five external legs (Pentagons):
 - Two independent calculations.
 - Numerically stable results with Denner Dittmaier method.

- Two different classes: final state gluon and initial state gluon.
- Each of them consists of several hundred Feynman-Graphs.
- Soft and collinear singularities subtracted with Catani-Seymour prescription

qqVVV amplitude: pentline corrections

Virtual corrections involve up to pentagons



The external vector bosons correspond to $V \rightarrow l_1 \bar{l}_2$ decay currents or quark currents

The sum of all QCD corrections to a single quark line is simple

$$\mathcal{M}_V^{(i)} = \mathcal{M}_B^{(i)} \frac{\alpha_s(\mu_R)}{4\pi} C_F \left(\frac{4\pi\mu_R^2}{Q^2} \right)^\epsilon \Gamma(1 + \epsilon) \left[-\frac{2}{\epsilon^2} - \frac{3}{\epsilon} + c_{\text{virt}} \right] + \widetilde{\mathcal{M}}_{V_1 V_2 V_3, \tau}^{(i)}(q_1, q_2, q_3) + \mathcal{O}(\epsilon)$$

- Divergent terms sum to Born sub-amplitude
- Use amplitude techniques to calculate finite remainder of virtual amplitudes

Denner-Dittmaier reduction of pentagon tensors is stable: indication of numerical problems for less than 0.2% of phase space points

Virtual corrections

Born sub-amplitude is multiplied by same factor as found for pure vertex corrections
 \Rightarrow when summing all Feynman graphs the divergent terms multiply the complete \mathcal{M}_B

Complete virtual corrections

$$\mathcal{M}_V = \mathcal{M}_B F(Q) \left[-\frac{2}{\epsilon^2} - \frac{3}{\epsilon} + \frac{4\pi^2}{3} - 8 \right] + \widetilde{\mathcal{M}}_V$$

where $\widetilde{\mathcal{M}}_V$ is finite, and is calculated with amplitude techniques.

The interference contribution in the cross-section calculation is then given by

$$2 \operatorname{Re} [\mathcal{M}_V \mathcal{M}_B^*] = 2 |\mathcal{M}_B|^2 F(Q) \left[-\frac{2}{\epsilon^2} - \frac{3}{\epsilon} + \frac{4\pi^2}{3} - 8 \right] + 2 \operatorname{Re} [\widetilde{\mathcal{M}}_V \mathcal{M}_B^*]$$

The divergent term, proportional to $|\mathcal{M}_B|^2$, cancels against the subtraction terms which have the same structure as for single W or Z production.

Input variables for LHC phenomenology

- PDFs: CTEQ6L1 at LO and CTEQ6M, $\alpha_S(m_Z) = 0.118$ at NLO.

- Cuts and Masses:

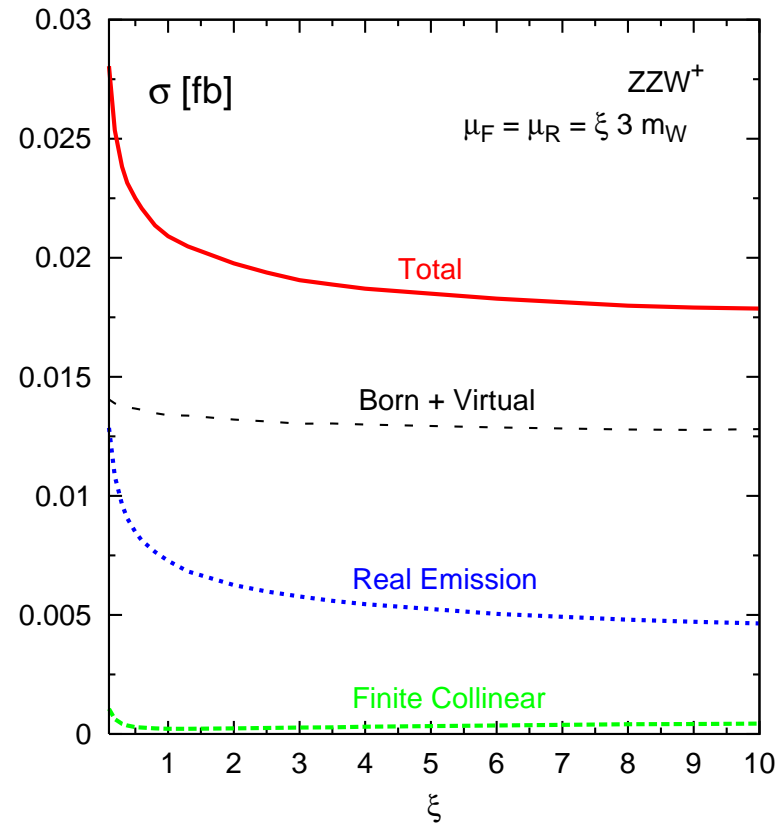
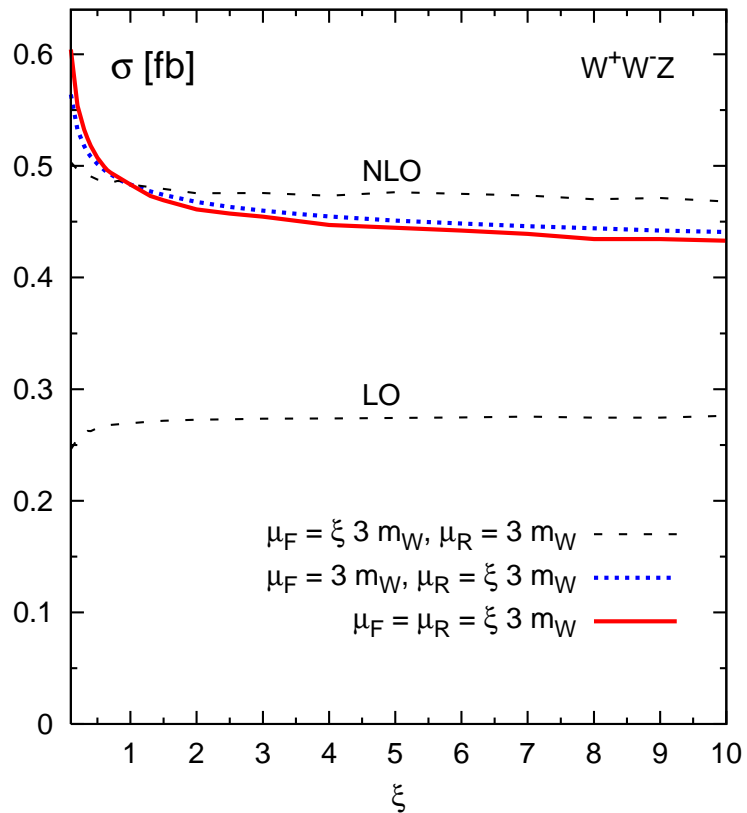
$$p_{T_\ell} > 10 \text{ GeV}, \quad |\eta_\ell| < 2.5, \quad m_{\ell+\ell^-} > 15 \text{ GeV}, \quad m_H = 120 \text{ GeV}.$$

- Renormalization- and Factorization Scale: $\mu_F = \mu_R = 3 m_W$.

Following results are for electrons and/or muons in the final state:

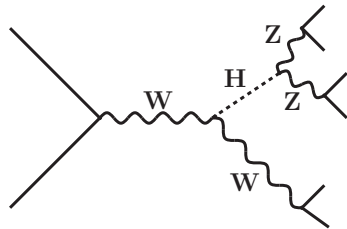
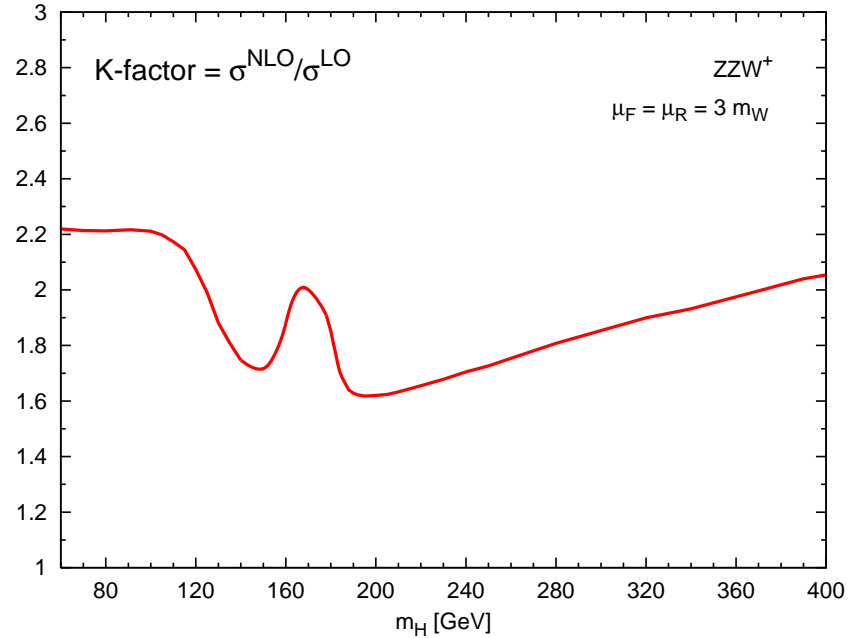
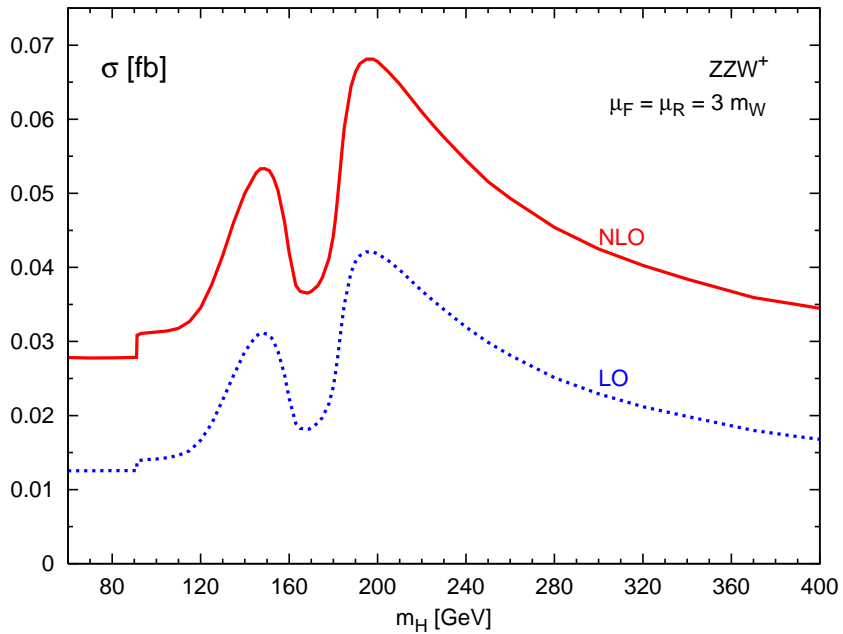
⇒ Combinatorial factor of 8/4 for the W^+W^-Z/ZZW^\pm production compared to three different lepton families in the final state.

Scale Dependence



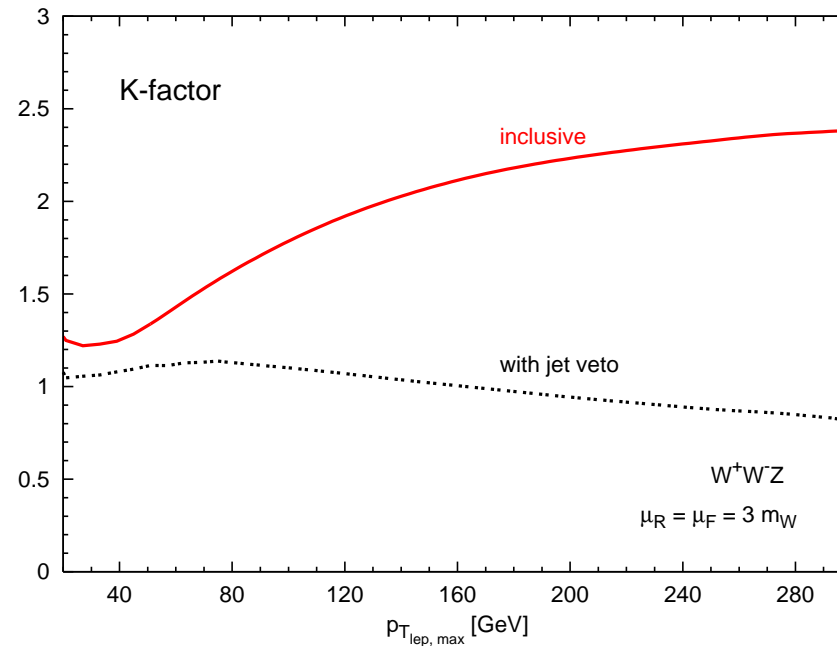
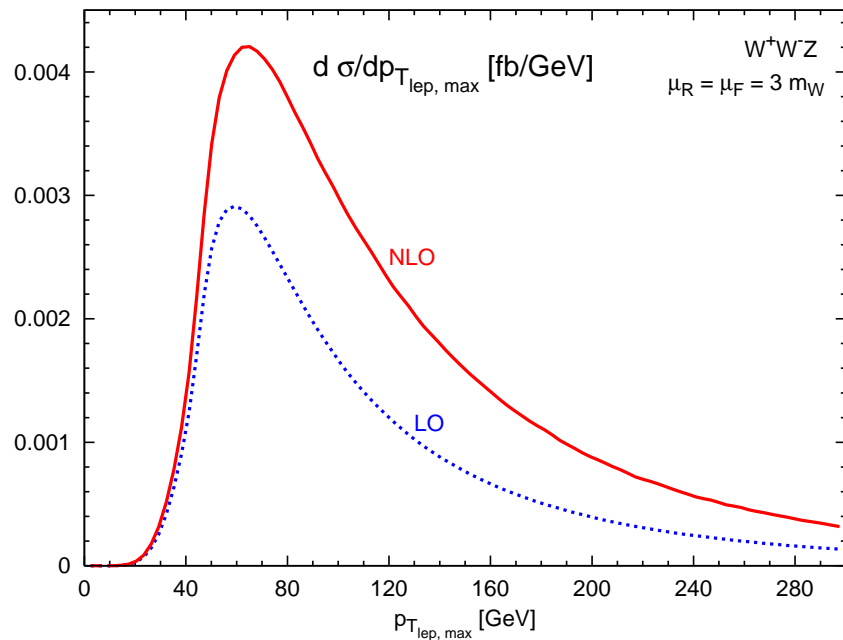
- At LO only small μ_F -dependence, no $\alpha_s(\mu_R)$.
- At NLO scale dependence is dominated by $\alpha_s(\mu_R)$.
- Real emission contribution drives overall scale dependence at NLO.

Higgs mass dependence



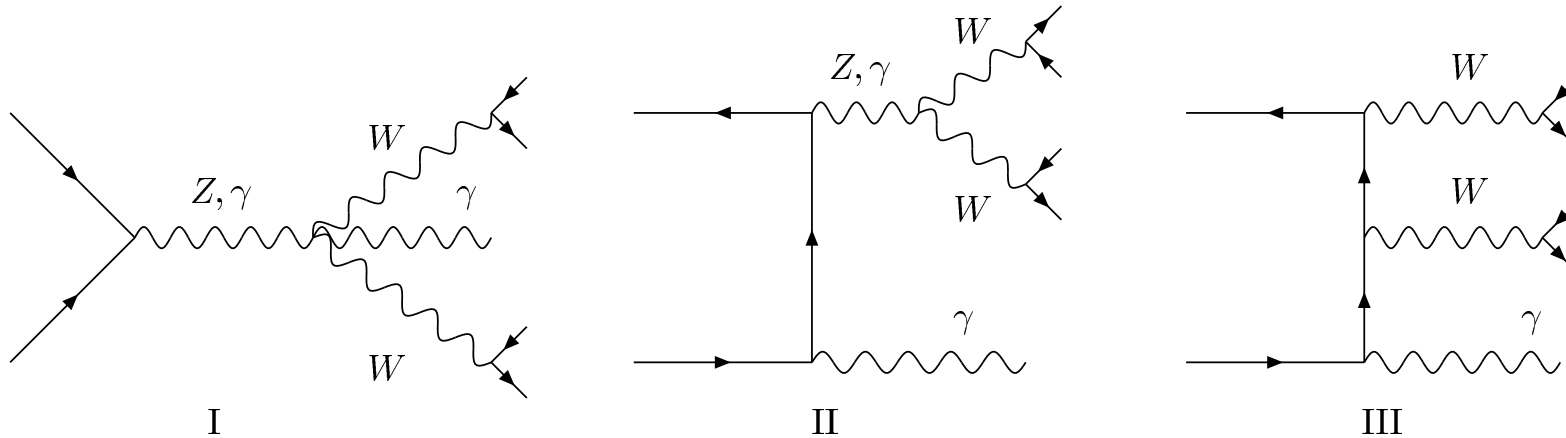
- Cross section reflects behavior of $BR(H \rightarrow ZZ)$
- K-factor is reduced by Higgs contribution.
 K-factor for $pp \rightarrow ZH$ production is about $K = 1.3$
 \implies Different K-factor for resonance production (see also Wt case, talk by **Chris White**)

Differential cross section and K-factor for the highest- p_T -lepton



- K-factor increases with transverse momentum (p_T) by almost a factor of 2.
- Strong phase space dependence due to events with high p_T jets recoiling against the leptons.
- Veto on jets with $p_T > 50$ GeV leads to fairly flat K-factor.

Extension to $W^+W^-\gamma$ and $ZZ\gamma$ Production



New elements of calculation:

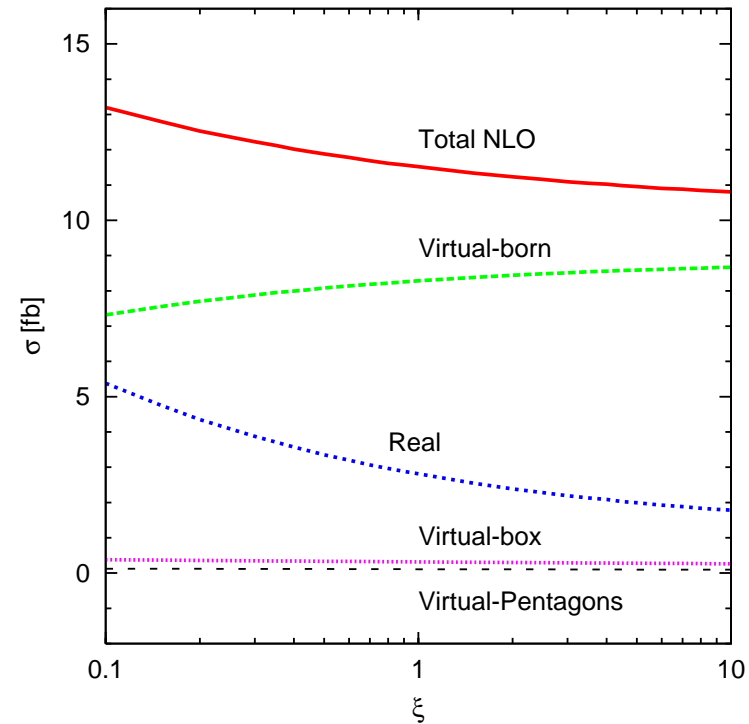
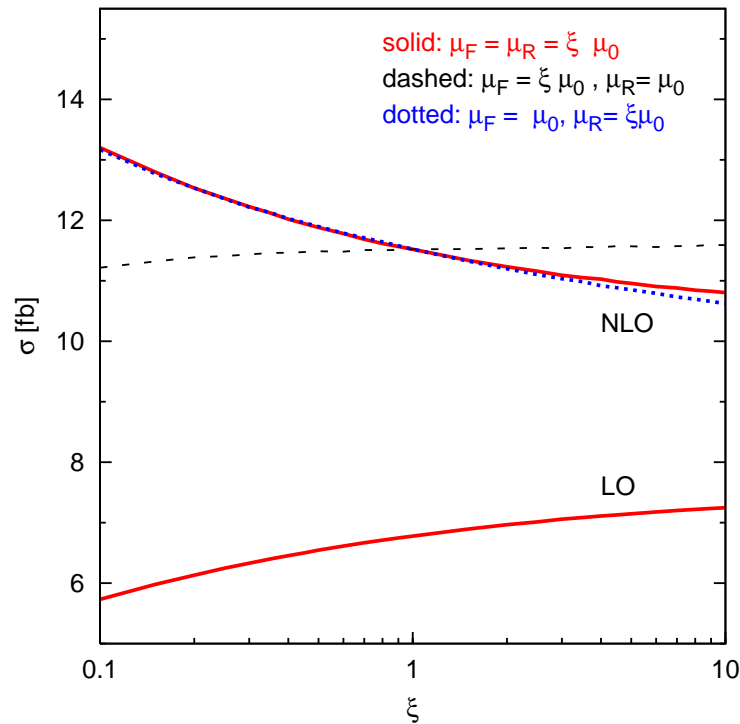
- Different infrared divergence structure of individual loop integrals but same final virtual expressions in terms of finite parts of C_{ij} , D_{ij} , and E_{ij} functions
- Photon isolation from jets for real emission contributions: use Frixione isolation

$$\sum_i E_{T_i} \theta(\delta - R_{i\gamma}) \leq p_{T\gamma} \frac{1 - \cos \delta}{1 - \cos \delta_0} \quad (\text{for all } \delta \leq \delta_0)$$

- Final state photon radiation becomes important: adapt phase space to this

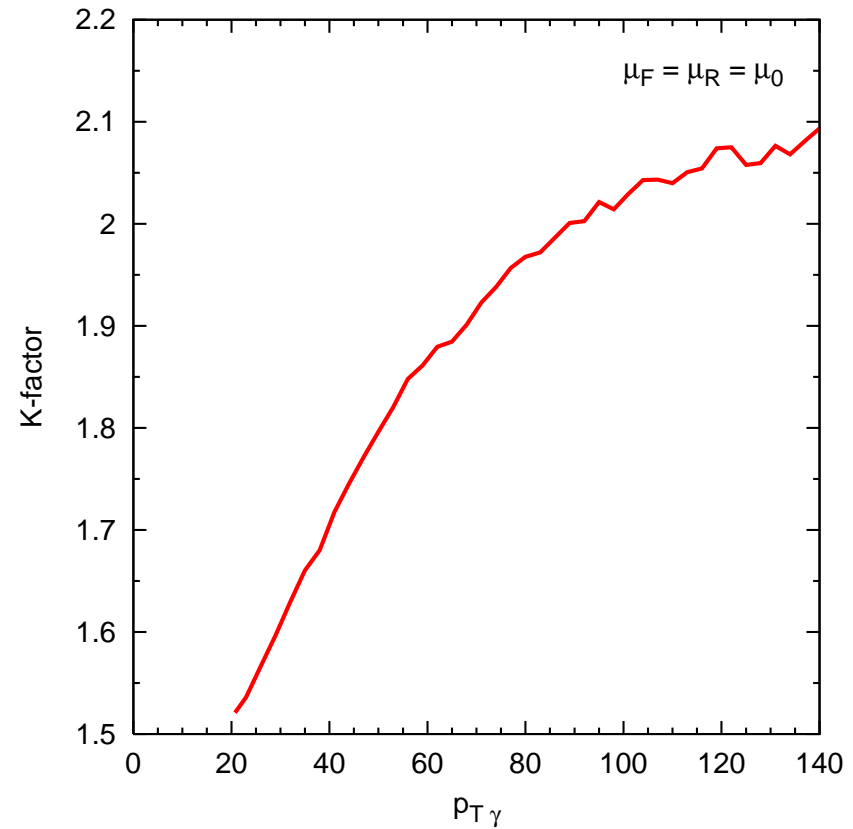
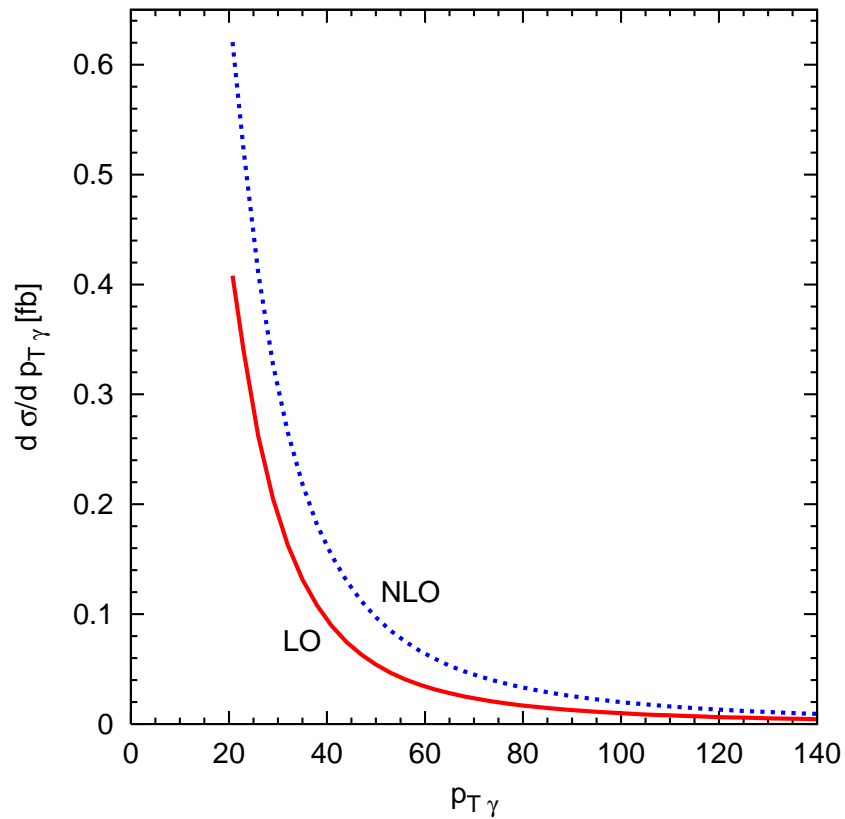
Scale dependence of integrated cross sections

Variation of μ_F, μ_R about $\mu_0 = m_{WW\gamma}$



- Behaviour similar to VVV production: LO scale variation much smaller than NLO correction
- NLO scale dependence largely due to real emission contributions \implies jet veto will reduce it
- Box and pentagon contributions ($\tilde{\mathcal{M}}_V$ terms) are quite small: 3% and $< 1\%$ of total

NLO Corrections to Distributions: p_T of photon



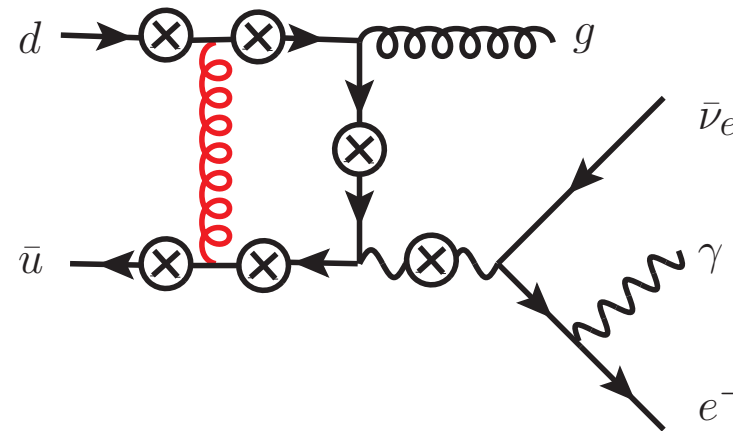
Strong phase space dependence of K-factors (depends on LO scale choice)

NLO QCD Corrections to $W\gamma j$ Production

- Provide NLO QCD corrections including leptonic W decay, e.g.

$$pp \rightarrow e^+ \nu_e \gamma j, \quad pp \rightarrow e^- \bar{\nu}_e \gamma j$$

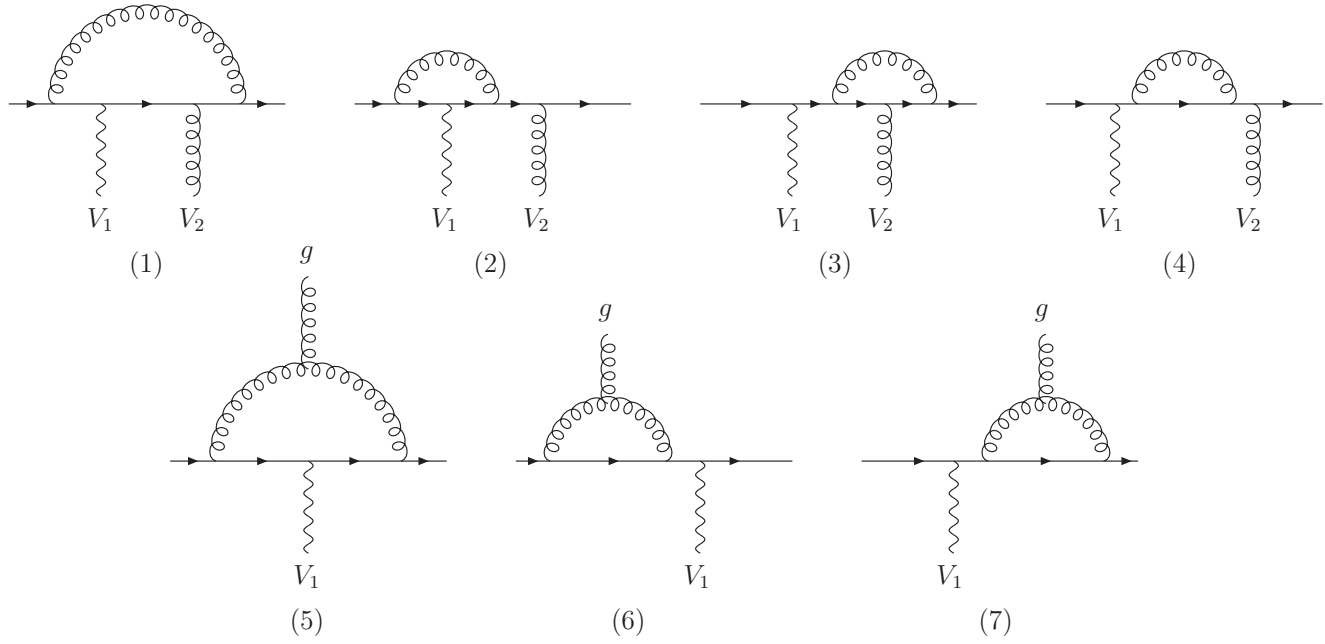
- Sizable cross section at LHC (1.2 pb) and Tevatron (15 fb) for $p_{Tj}, p_{T\gamma} > 50$ GeV and separation cuts (later)
- Measurement of anomalous $WW\gamma$ coupling: veto on jets in $W\gamma$ events requires good knowledge of cross section and distributions: want NLO
- Photon isolation à la Frixione probed at NLO level



- Initial and final state photon radiation. Final radiation from lepton is important
- Virtual corrections up to pentagons
- External gluon already at tree level \implies *nonabelian* boxes with three gluon vertex
- Larger number of subtraction terms

Virtual Corrections: nonabelian Contributions

Example: non-abelian extension of boxline graphs. Keep modular structure of calculation



$$\begin{aligned}
 & \left(C_F - \frac{1}{2} C_A \right) \left(A_1(12) + A_3(12) \right) \\
 & + C_F \left(A_2(12) + A_4(12) \right)
 \end{aligned}$$

$$C_A \left(A_5 + A_6 + A_7 \right)$$

Combine to two boxline amplitudes $M_V(12)$ and $M_V(21)$ and new nonabelian combination

$$M_V(12, \text{boxline}) = \left(C_F - \frac{1}{2} C_A \right) \sum_{i=1,4} A_i(12)$$

$$M_V(na) = \frac{1}{2} C_A \left(A_2(12) + A_4(12) + A_3(21) + A_4(21) \right) + C_A \left(A_5 + A_6 + A_7 \right)$$

Scale dependence: LHC and Tevatron

Identify lepton, photon and one or more jets with k_T -algorithm ($D = 0.7$)

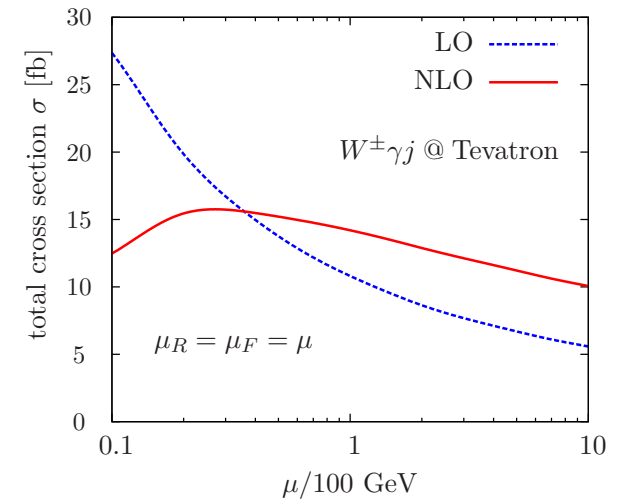
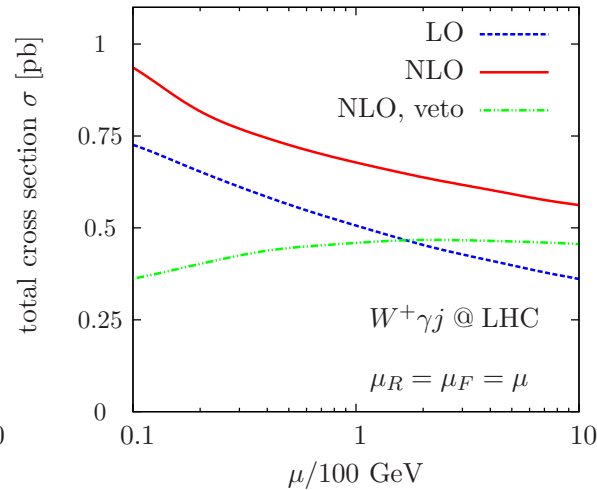
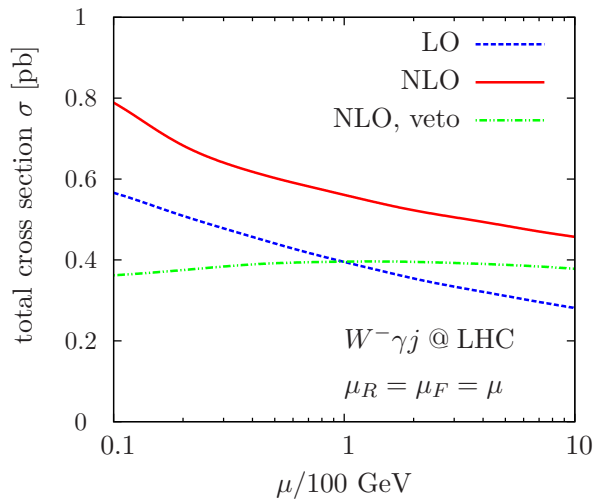
$$p_{Tj,\gamma} \geq 50 \text{ GeV}, \quad |y_j| \leq 4.5, \quad |\eta_\gamma| \leq 2.5,$$

$$p_{Tl} \geq 20 \text{ GeV}, \quad |\eta_l| \leq 2.5$$

$$R_{l,\gamma}, R_{l,j} > 0.2$$

Frixione isolation of photons with $\delta_0 = 1$

Cross sections are for $W \rightarrow e\nu_e$ only

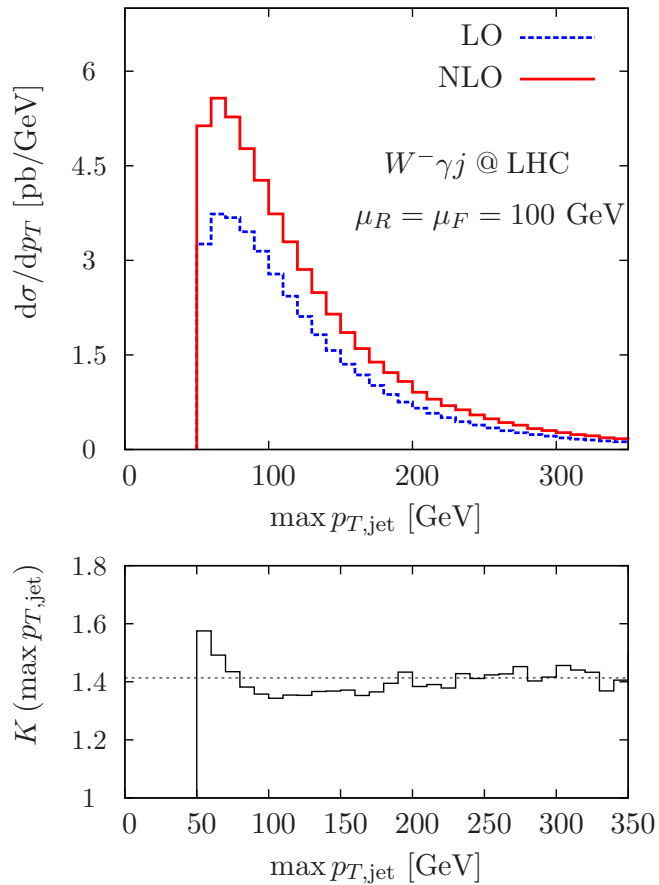


Scale variation at LHC for $\mu_F = \mu_R = 2^{\pm 1} \cdot 100 \text{ GeV}$: ±11% at LO reduced to ±7% at NLO

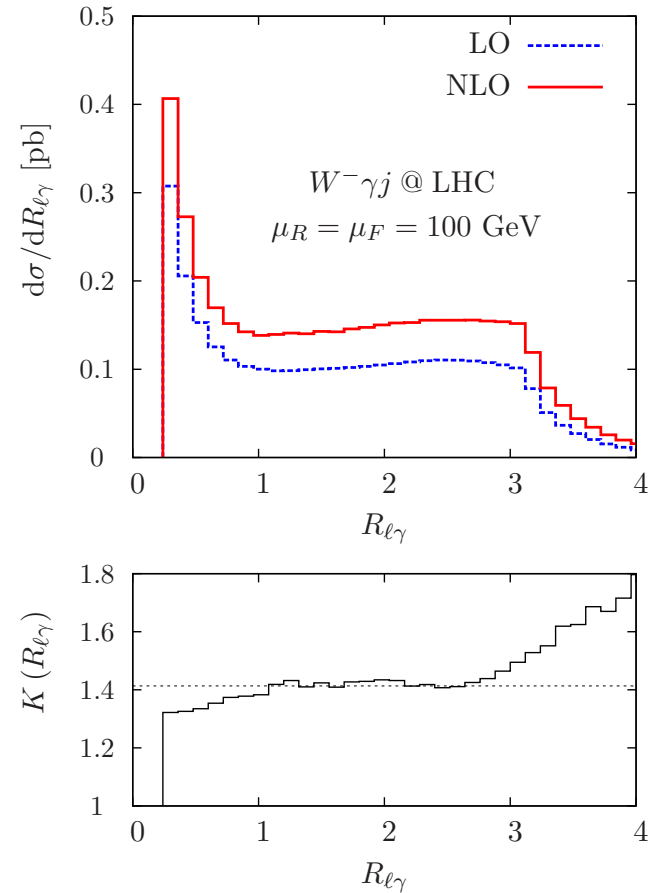
Almost flat behaviour for veto of additional jets of $p_T > 50 \text{ GeV}$ should be taken as accidental and not as a measure of NLO uncertainties

NLO corrections to distributions

p_T of hardest jet



lepton photon separation



- Clear shape changes of distributions when going from LO to NLO
- Average K-factor of 1.4 at LHC is significantly larger than LO scale variation

Conclusions

- Much progress on Higgs physics, Monte Carlo tools, NLO corrections in recent years
- We are all ready for LHC data

Thank you, Nikolas, for a great workshop