

# Weakly coupled $Z'$ bosons at the LHC and ILC

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1. Introduction
2. Search for weakly coupled  $Z'$ 's
3. Parameter determination

PRD 70, 015008 [hep-ph/0403288]

## Introduction

Additional neutral gauge bosons expected in many extensions of SM:

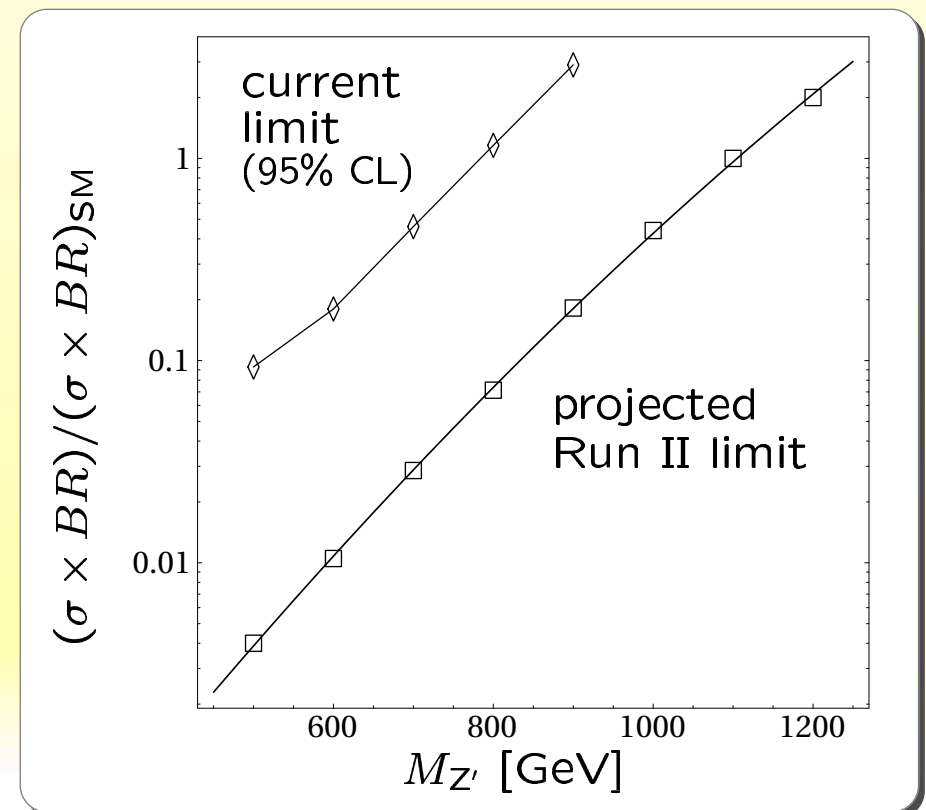
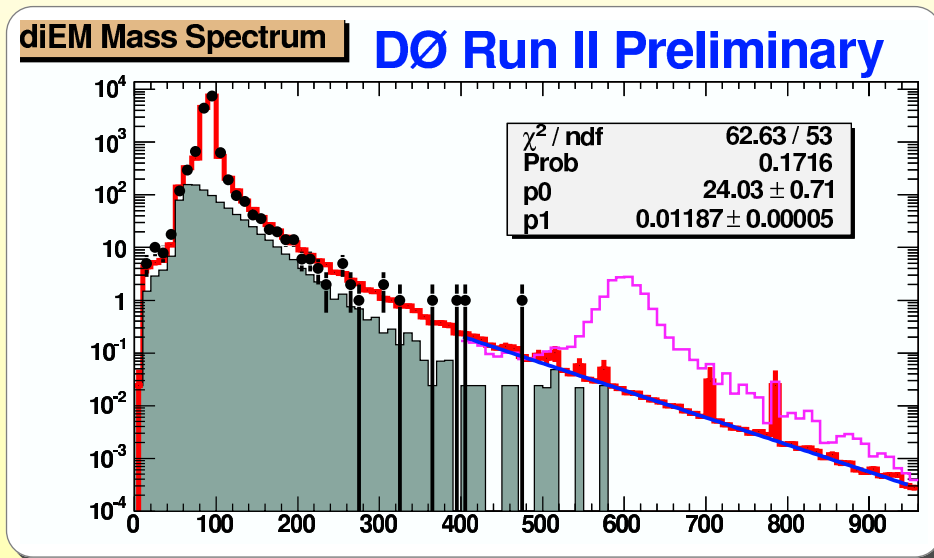
- **Unified gauge groups** (SU(5), SO(10),  $E_6$ , LR-symmetry, ...)
- **Dynamical electroweak symmetry breaking**  
(Technicolor, Topcolor, ...)
- **Little Higgs models**  
→ extra gauge bosons to cancel large radiative corrections to Higgs potential
- **Extra dimensions**  
KK excitations in models with various geometries and boundary conditions

**Conclusion:** Plethora of new physics models allows wide range of  $Z'$  masses and couplings

# Existing limits for neutral vector bosons (Z's)

## Z' bosons at the Tevatron

- Search for new physics signals in Drell-Yan with lepton final state:  
 $p\bar{p} \rightarrow Z' + X \rightarrow l^+l^- + X$
- Main background:  $p\bar{p} \rightarrow \gamma^*, Z^* + X \rightarrow l^+l^- + X$



# Z' bosons at LEP

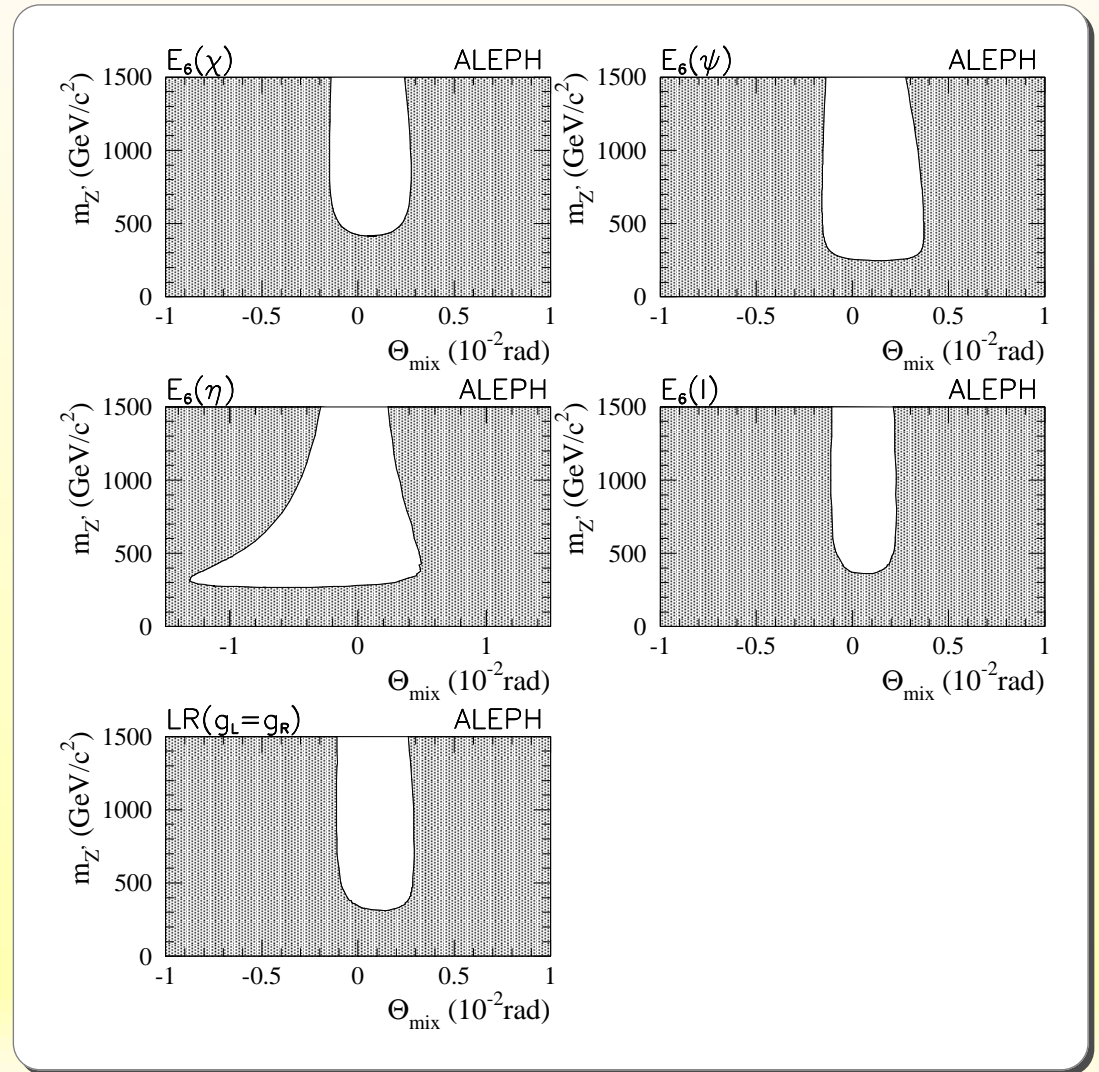
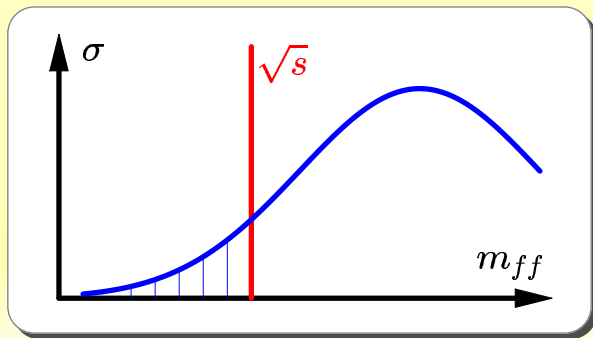
Heavy Z' bosons  $M_{Z'} > 200$  GeV:

ALEPH '00

- Z-Z' mixing effects  
→ measurable at LEP1
- Off-shell propagator effects of Z' modify

$$e^+e^- \xrightarrow{\gamma, Z, Z'} f\bar{f}$$

→ Sensitivity at LEP2  
for  $M_{Z'} > \sqrt{s}$

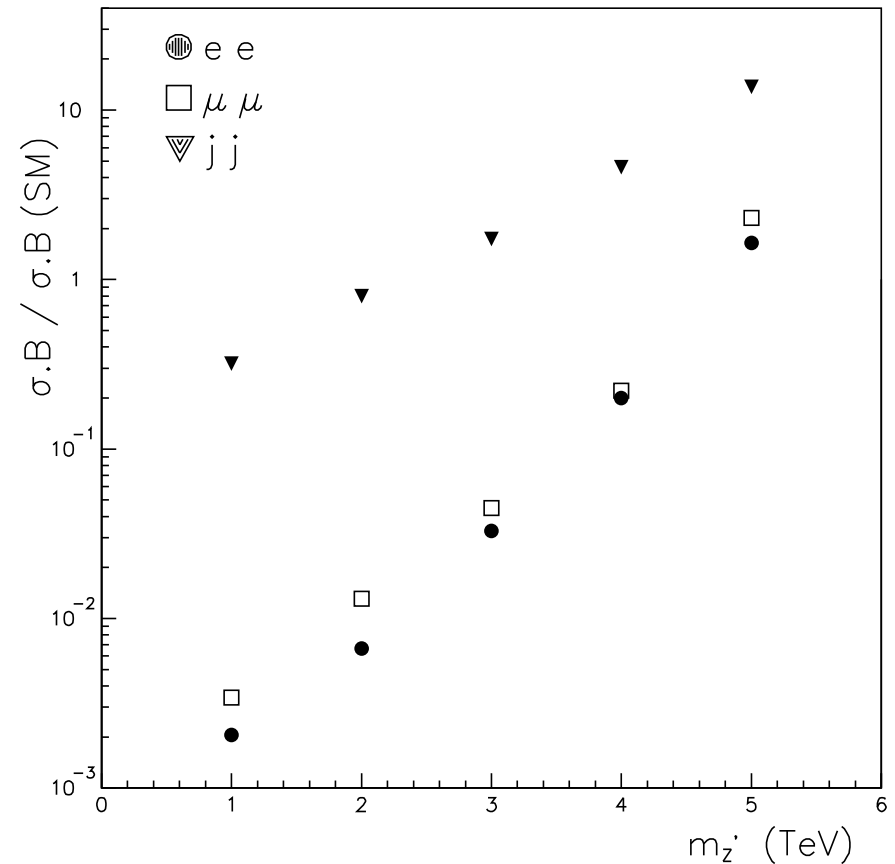


## Z' bosons at the LHC

- Higher energy and more statistics than Tevatron
- Discovery in leptonic channels  
 $pp \rightarrow Z' + X \rightarrow l^+ l^- + X$   
up to  $M_{Z'} \sim 5$  TeV
- Jet channel also possible, but large QCD background

ATLAS TDR '99

5 $\sigma$  discovery contours:



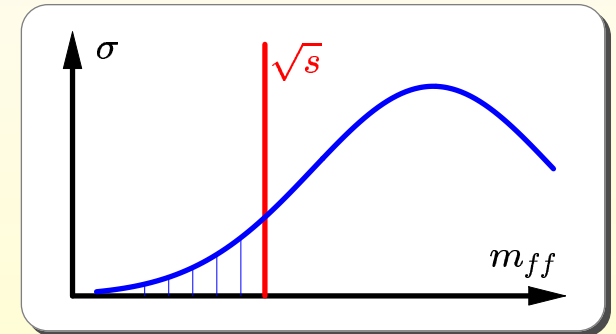
# Z' bosons at a future linear collider

Heavy Z' bosons  $M_{Z'} > 1$  TeV:

- Small Z–Z' mixing  
→ negligible effect on Z-pole data
- Propagator effects of Z' modify

$$e^+e^- \xrightarrow{\gamma, Z, Z'} f\bar{f}$$

→ High luminosity  $500\text{--}1000 \text{ fb}^{-1}$  allows sensitivity for  $M_{Z'} \gg \sqrt{s}$



- Sensitive observables:
  - total cross-section  $\sigma_{\text{tot}}$
  - forward-backward asymmetry  $A_{\text{FB}}$
- With  $e^-$  beam polarization
  - left-right asymmetry  $A_{\text{LR}}$
  - polarization asymmetry  $A_{\text{pol}}$

$$A_{\text{FB}} = \frac{\sigma_{\text{F}} - \sigma_{\text{B}}}{\sigma_{\text{tot}}}$$
$$A_{\text{LR}} = \frac{\sigma_{\text{L}} - \sigma_{\text{R}}}{\sigma_{\text{tot}}}$$
$$A_{\text{pol}} = \frac{(\sigma_{\text{L}} - \sigma_{\text{R}})_{\text{F}} - (\sigma_{\text{L}} - \sigma_{\text{R}})_{\text{B}}}{\sigma_{\text{tot}}}$$

## Projected sensitivity

- Look for deviations from SM background

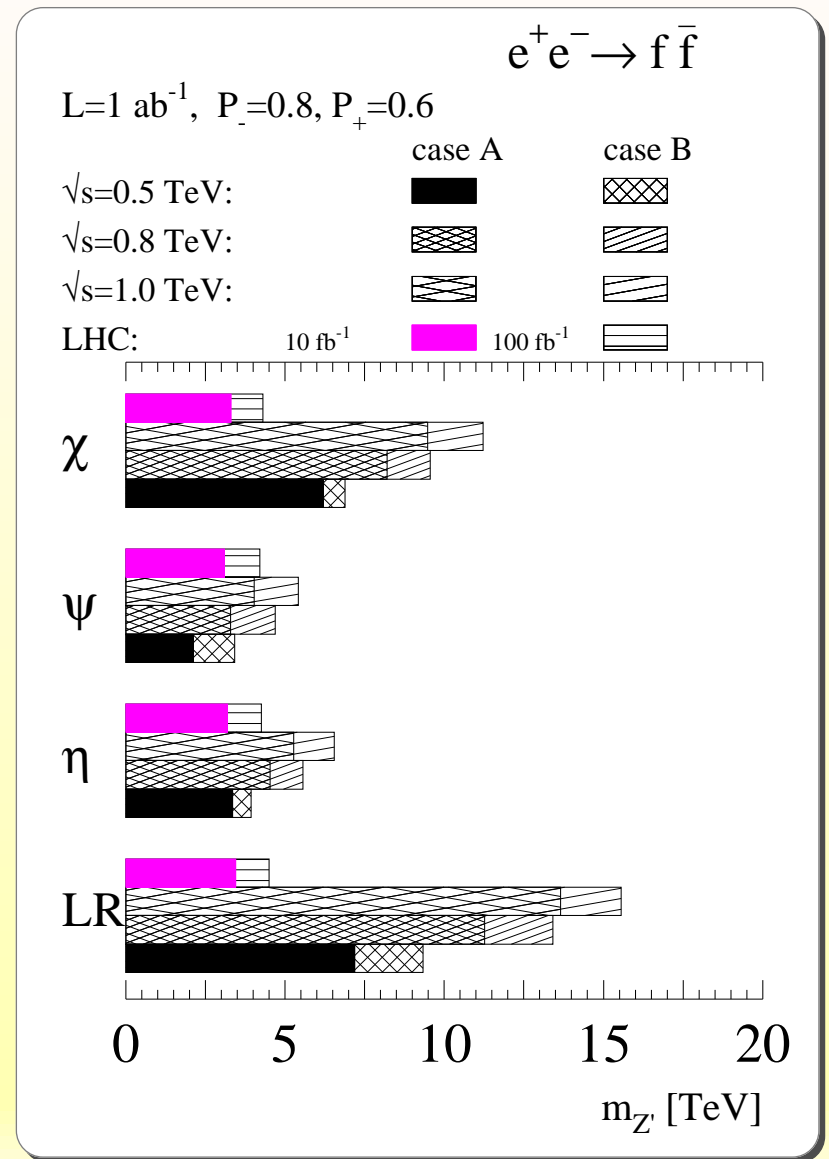
$$e^+e^- \xrightarrow{\gamma^*, Z^*} f\bar{f}$$

- Assume  $P(e^-) = 80\%$   
 $P(e^+) = 60\%$   
 (slight improvement from  $e^+$  pol.)

- Combine all observables  
 $\sigma_{\text{tot}}, A_{\text{FB}}, A_{\text{LR}}, A_{\text{pol}}$

case A,B : different assumptions  
 about sys. errors

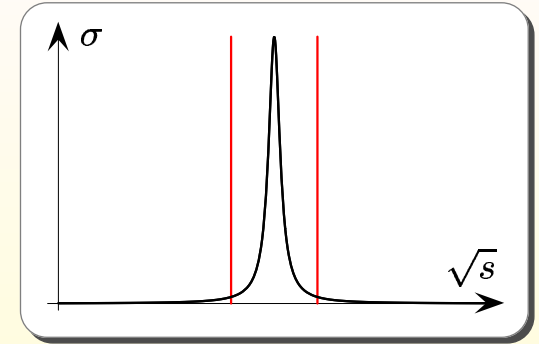
S. Riemann '00



# Search for weakly coupled neutral vector bosons

Weakly coupled  $Z'$  form narrow resonance

→ Can only be produced in  $e^+e^- \rightarrow Z' \rightarrow f\bar{f}$   
for  $M_{Z'} \approx \sqrt{s}$



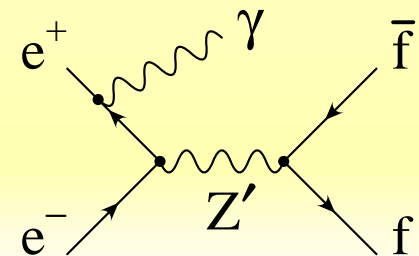
For  $\Delta E > \Gamma_{Z'}$  :

$$\int d(\sqrt{s}) \sigma[e^+e^- \rightarrow Z' \rightarrow f\bar{f}] = \frac{6\pi^2 \Gamma_{Z'}}{M_{Z'}^2} \text{Br}(Z' \rightarrow e^+e^-) \text{Br}(Z' \rightarrow f\bar{f}),$$

Most stringent constraints on narrow  $Z'$  with  $M_{Z'} < \sqrt{s}$  from  
 $e^+e^- \rightarrow Z' + n\gamma \rightarrow f\bar{f} + n\gamma$

Leike '99  
Appelquist, Dobrescu, Hopper '03

$$[e^+e^-]_s \xrightarrow{\text{beamstr.}} [e^+e^-]_{s' < s} \rightarrow Z' \rightarrow f\bar{f}$$





## Initial state-radiation

Leading effects due to initial-state  $\gamma$  radiation collinear to beam

Structure function method:

Kuraev, Fadin '85  
Altarelli, Martinelli '86

$$\sigma[e^+e^- \rightarrow f\bar{f} + n\gamma](s) = \int_0^1 dx_+ \int_0^1 dx_- \Gamma_{ee}(x_+, s) \Gamma_{ee}(x_-, s) \times \sigma[e^+e^- \rightarrow f\bar{f}](sx_+x_-),$$

Structure function include large logarithms

$L = \log(s/m_e^2)$ , known to  $\mathcal{O}(\alpha^5 L^5)$

Przybycień '95

$$\Gamma_{ee}(x, s) = \delta(1-x) + \frac{\alpha}{2\pi} L \frac{1+x^2}{1-x} + \left(\frac{\alpha}{2\pi}\right)^2 L^2 \dots$$

## Beamstrahlung:

Beam disruption due to beam-beam interaction

Detailed simulations with *Guinea-Pig*  
included in *Circe* (*Κιρκη*)

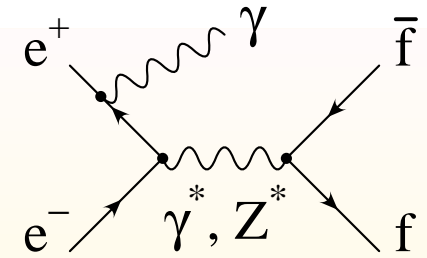
Schulte '99

Ohl '97

Dominant background:

$$e^+e^- \rightarrow \gamma^*/Z^* + n\gamma \rightarrow f\bar{f} + n\gamma$$

$$[e^+e^-]_s \xrightarrow{\text{beamstr.}} [e^+e^-]_{s' < s} \rightarrow \gamma^*/Z^* \rightarrow f\bar{f}$$



**Signal:** narrow peak over background in  $f\bar{f}$  invariant mass spectrum

→ good momentum resolution crucial to improve S/B

$\mu^+\mu^-$ : momentum resolution of central tracker:  
 $\Delta(1/p) = 5 \cdot 10^{-5} \text{ GeV}^{-1}$

jet-jet: jet energy resolution from hadronic calo.:

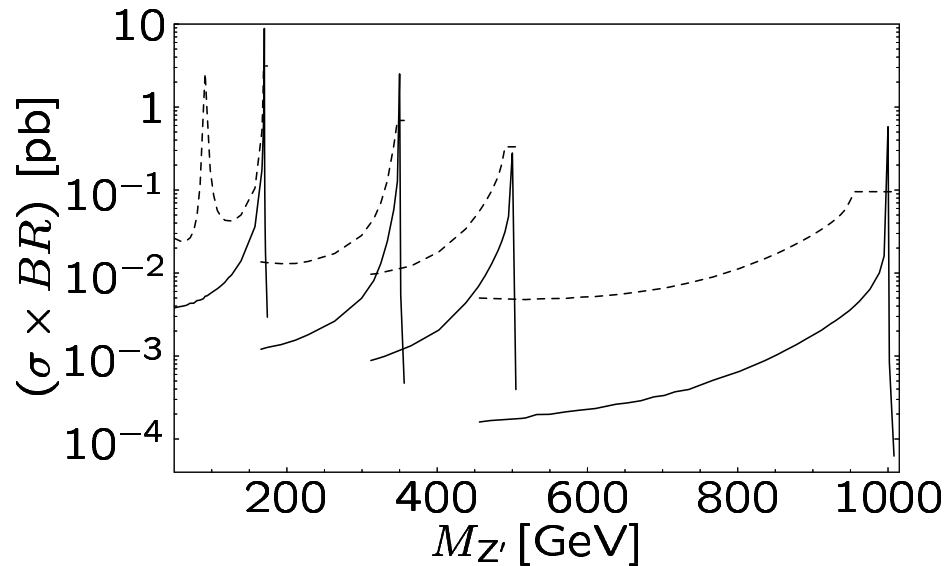
$$\frac{\Delta E_j}{E_j} \approx \frac{35\%}{\sqrt{E/\text{GeV}}} \oplus 3\%$$

TESLA TDR '01

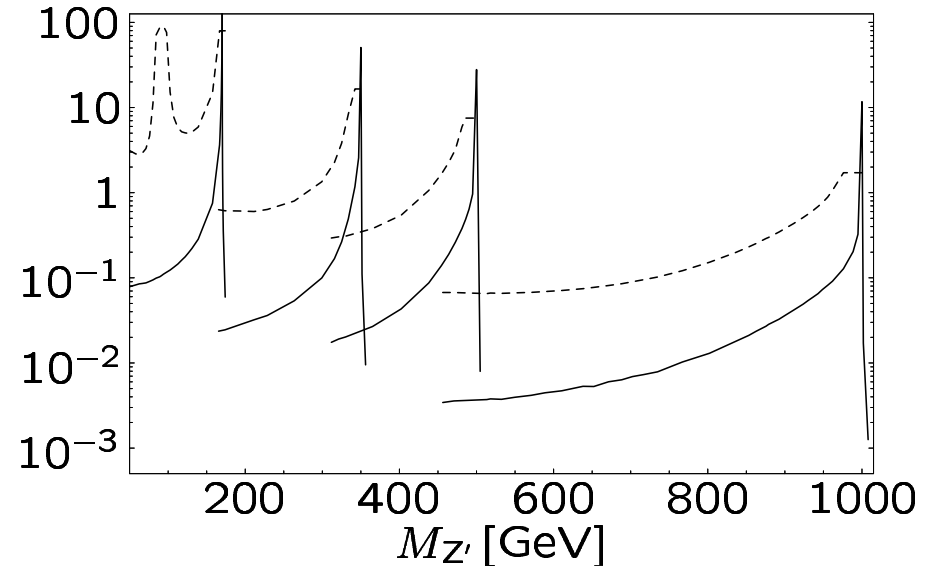
## Typical cross-sections

Consider  $Z'$  boson with same coupling quantum numbers as  $Z$   
 $g_{Z'} = g_Z/30$

$\mu^+\mu^-$  channel



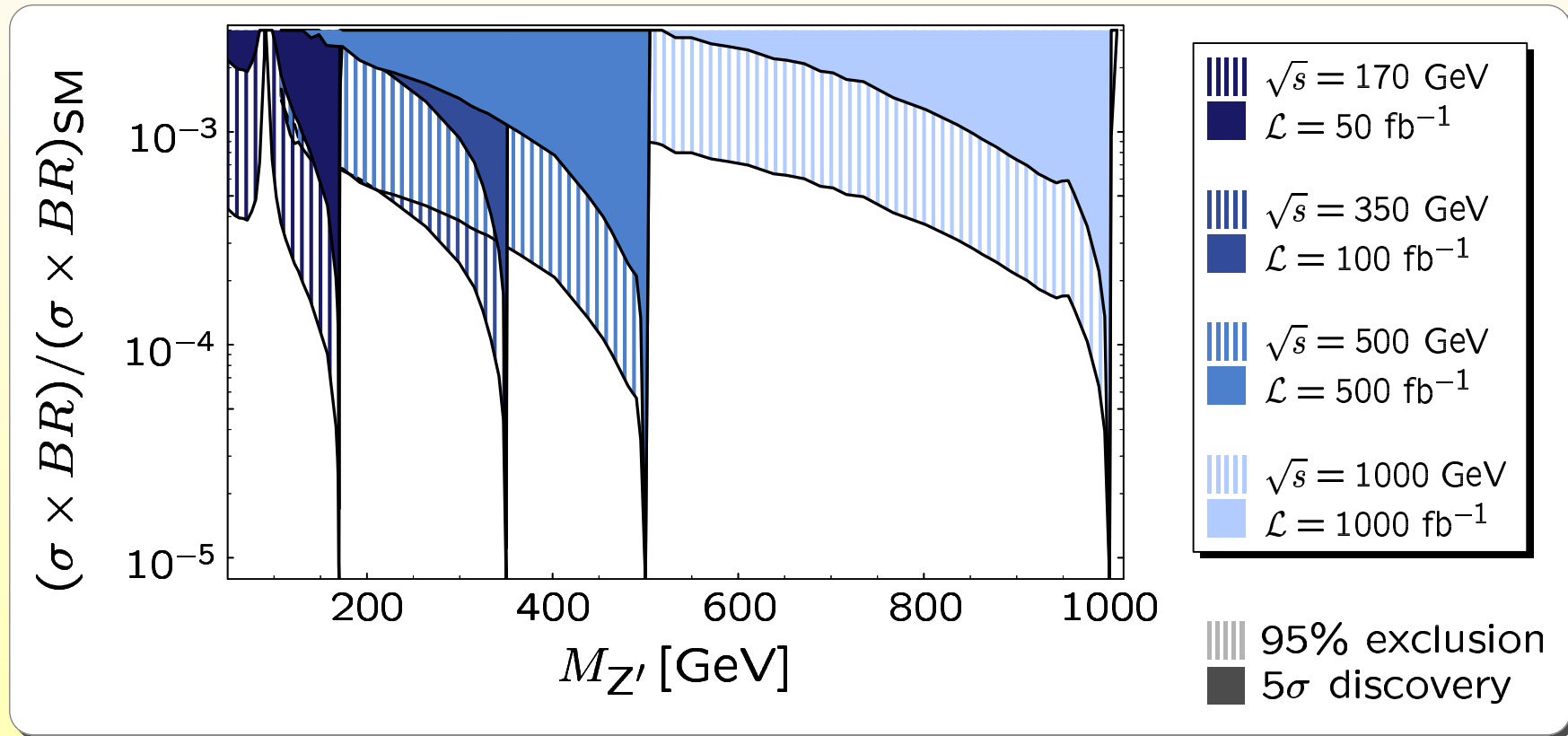
di-jet channel



— signal  
- - - SM background

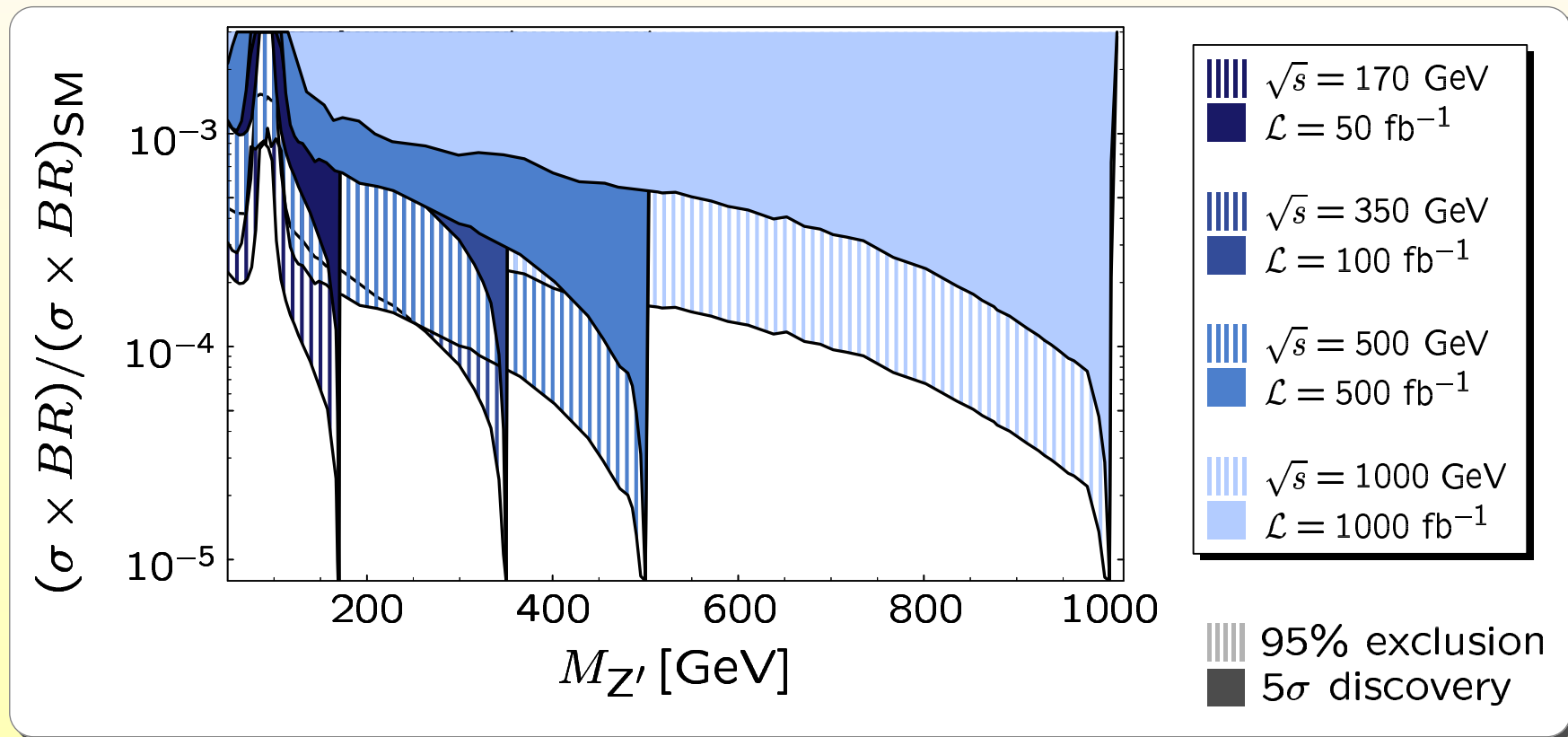
## Results for $\mu^+\mu^-$ channel

Cuts:  $\cos\theta_\mu \leq 0.94$        $\Delta E_{\mu\mu} \approx 5 \cdot 10^{-5} \text{ GeV}^{-1} \cdot s$



## Results for di-jet channel

Cuts:  $\cos \theta_\mu \leq 0.94$        $\Delta E_{jj} = 2 \sqrt{0.06125 \text{ GeV} \cdot \sqrt{s} + 0.000225 s}$



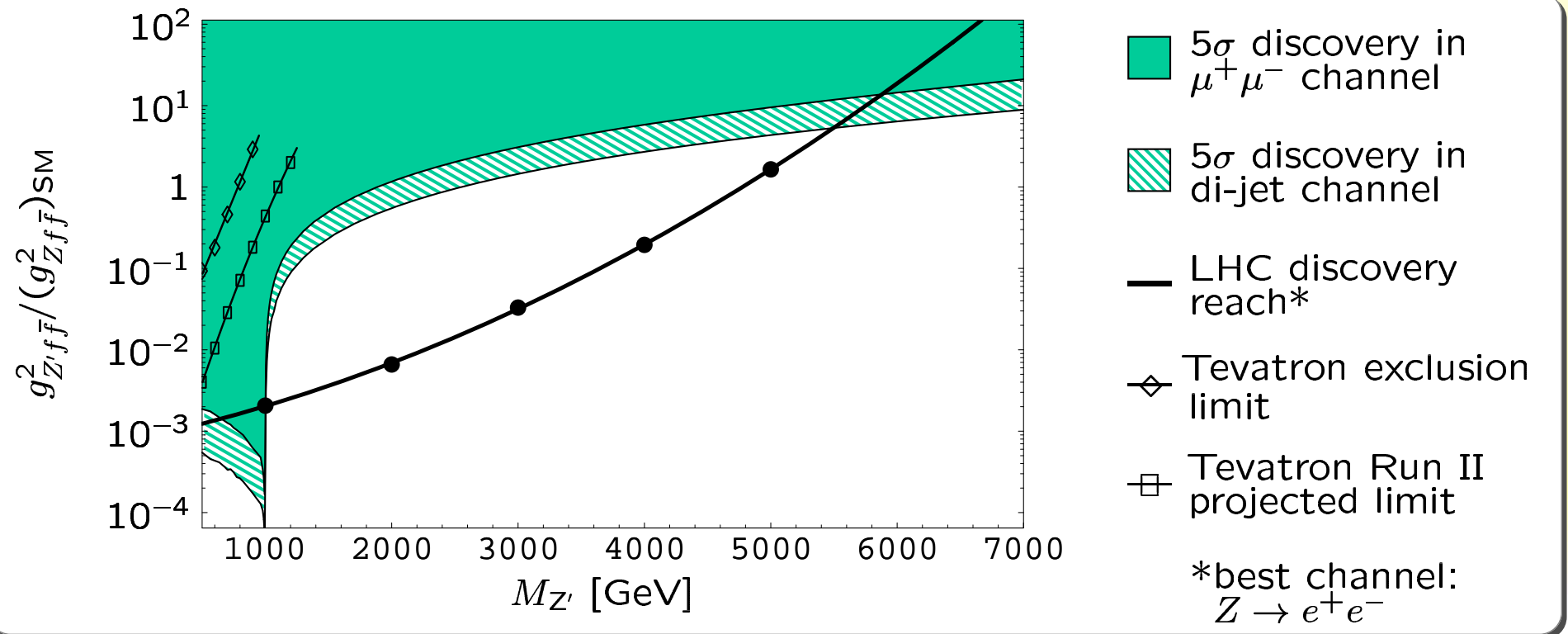
## Comparison with hadron colliders

Combination of searches with radiative-return method for  $M_{Z'} < \sqrt{s}$  and contact-interaction method for  $M_{Z'} > \sqrt{s}$  :

Sensitivity to high masses  $M_{Z'}$ , but only moderate coupling strength  $g_{Z'f\bar{f}}^2/(g_{Zf\bar{f}}^2)_{SM}$

Example for  $BR = BR_{SM}$ :

$\sqrt{s} = 1000 \text{ GeV}$ ,  $\int \mathcal{L} = 1000 \text{ fb}^{-1}$

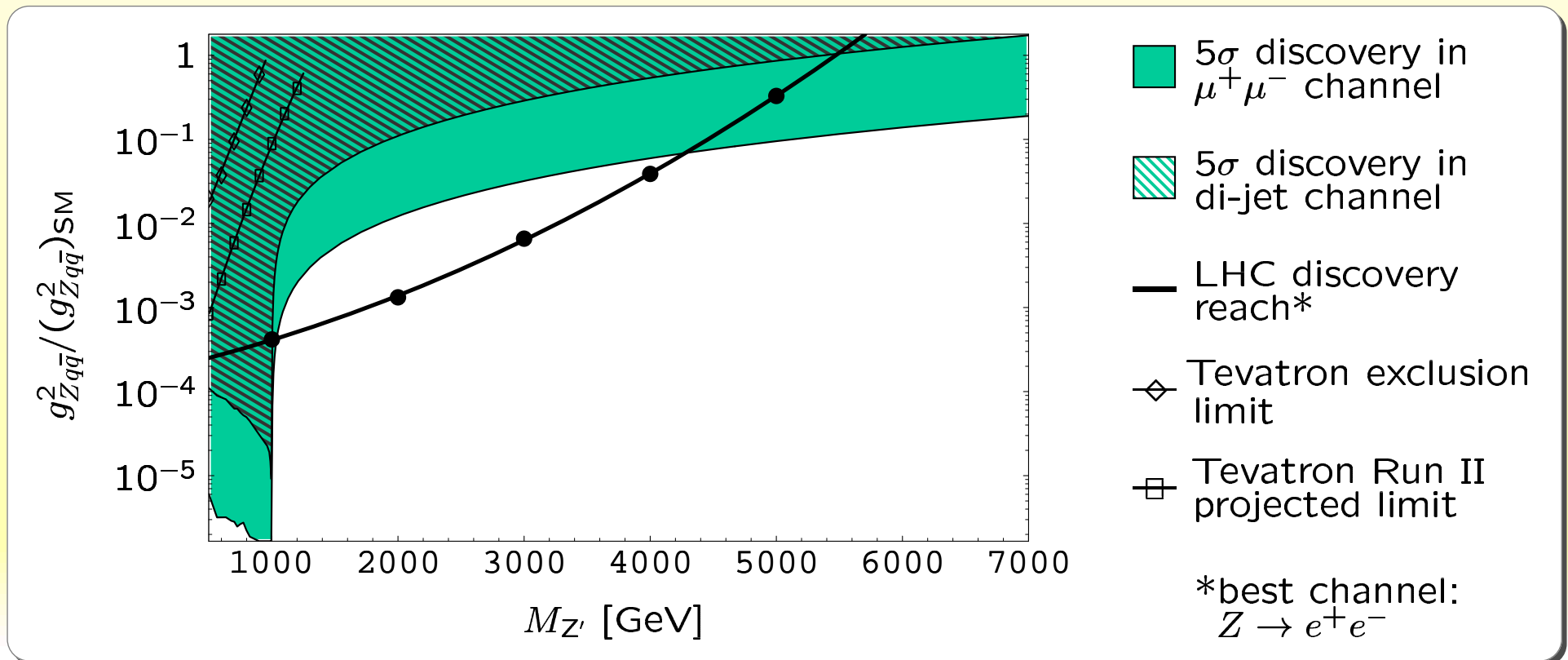


## Special case: $Z_{B-L}$

$Z'$  has pure  $B - L$  couplings  $\rightarrow$  corresponding to  $z_u = z_q$

$\Rightarrow$  No mixing between  $Z$  and  $Z'$  (i.e. no constraints from  $Z$ -pole)

$$\sqrt{s} = 1000 \text{ GeV}, \int \mathcal{L} = 1000 \text{ fb}^{-1}$$



## Parameter determination at LHC

Only relative couplings:

$$\gamma_L^l = \frac{(g_L^l)^2}{(g_L^l)^2 + (g_R^l)^2},$$

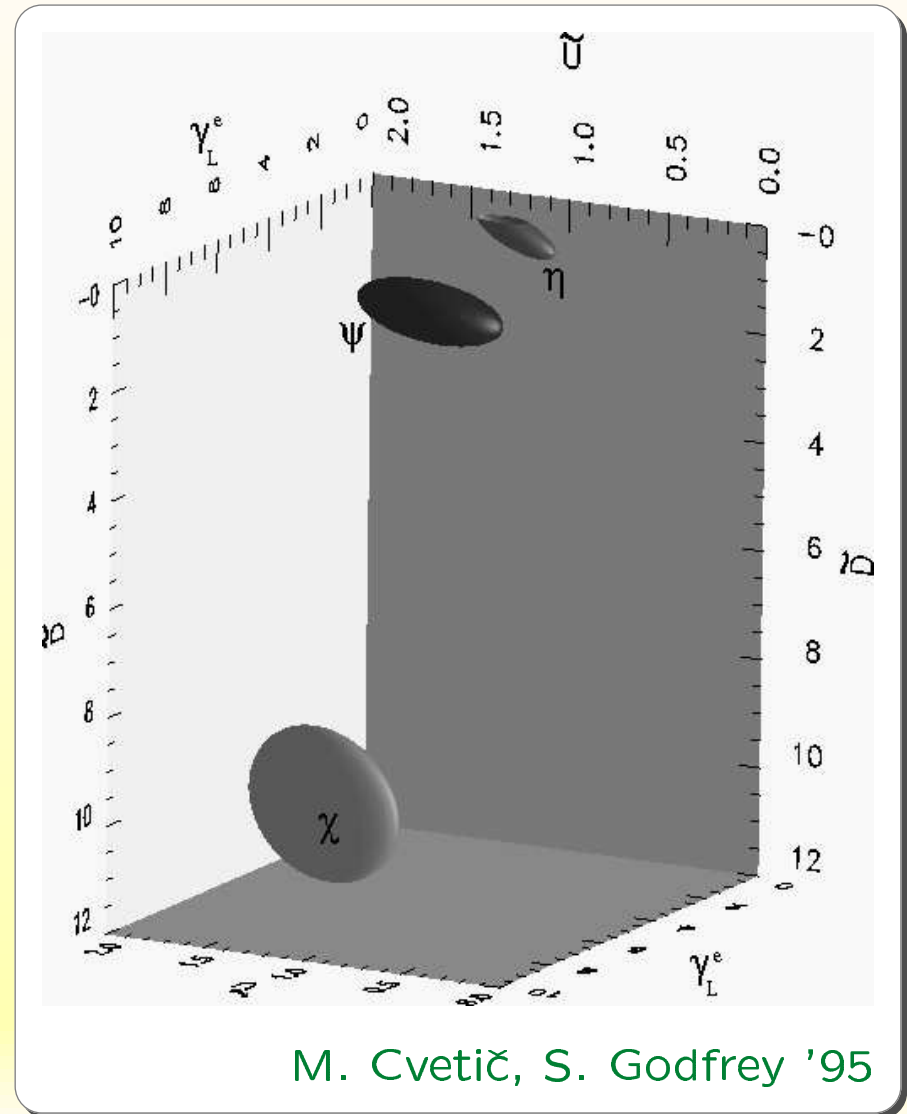
$$\gamma_L^q = \frac{(g_L^q)^2}{(g_L^q)^2 + (g_R^q)^2},$$

$$\tilde{U} = \frac{(g_R^u)^2}{(g_L^q)^2}, \quad \tilde{D} = \frac{(g_R^d)^2}{(g_L^q)^2}$$

Sensitive observables:

- forw.-backw. asymmetry  $A_{FB}$
- rapidity distribution
- associated production  
 $pp \rightarrow Z'Z, Z'\gamma, Z'W^\pm$

→ Good accuracy,  
but ambiguity in signs





# Parameter determination at linear collider

Determination of couplings of heavy  $Z'$  bosons  $M_{Z'} > 1$  TeV:

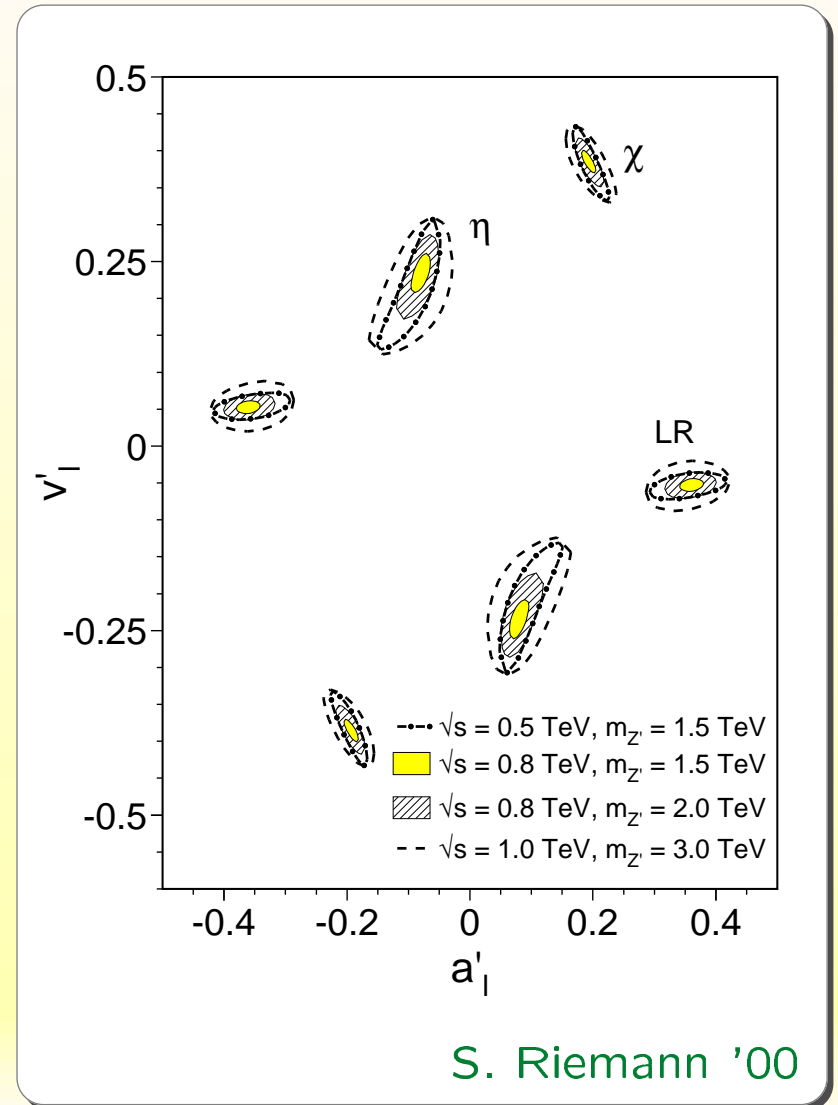
- Measure deviation from SM bkgd.  
 $e^+e^- \rightarrow \gamma^*, Z^* \rightarrow f\bar{f}$   
in cross-section and asymmetries

- Only sensitive to ratio of  $Z'$  couplings and  $Z'$  mass

$$a_f^N = a'_f \sqrt{\frac{s}{M_{Z'}^2 - s}},$$

$$v_f^N = v'_f \sqrt{\frac{s}{M_{Z'}^2 - s}}$$

- If  $Z'$  discovered at LHC  
→ Use LHC mass measurement  
as input



## Determination of couplings of light $Z'$ bosons $M_{Z'} < 1$ TeV:

Example:  $Z_{B-L}$  boson with  $M_{Z'} = 400$  GeV and  $\tilde{g}_l = g_{Z'u} = 0.006$

$$\Rightarrow (\sigma \times BR)/(\sigma \times BR)_{SM} \simeq 1.2 \times 10^{-3}, \quad \Gamma_{Z'} \simeq 0.6 \text{ MeV}$$

Total width too small to be resolved

→ Difficult to determine **absolute** coupling strength

→ Still possible to determine **relative** coupling ratios

• From left-right asymmetry:

$$A_{LR} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R}$$

Using 80% polarized  $e^-$  and

$10 \text{ fb}^{-1}$  each for L- and R-polarized  $e^-$  at  $\sqrt{s} = 400$  GeV

$$\left( \frac{g_{Z'ee}^L}{g_{Z'ee}^R} \right)^2 = \frac{P + A_{LR}}{P - A_{LR}} \Rightarrow \frac{\delta(g_{Z'ee}^L/g_{Z'ee}^R)}{g_{Z'ee}^L/g_{Z'ee}^R} \simeq 0.01$$

$P$  = Polarization degree

- From forward-backward asymmetry:

$$A_{\text{FB}} = \frac{\sigma_{\text{F}} - \sigma_{\text{B}}}{\sigma_{\text{F}} + \sigma_{\text{B}}}$$

Consider  $e^+e^- \rightarrow \mu^+\mu^-$  and assuming lepton universality

Using  $20 \text{ fb}^{-1}$  at  $\sqrt{s} = 400 \text{ GeV}$

$$\left( \frac{g_{Z'u}^{\text{F}}}{g_{Z'u}^{\text{B}}} \right)^2 = \frac{\sqrt{C} + \sqrt{A_{\text{FB}}}}{\sqrt{C} - \sqrt{A_{\text{FB}}}} \quad C = \frac{\cos \theta_{\text{max}}}{1 + \frac{1}{3} \cos \theta_{\text{max}}}$$

$$\Rightarrow \frac{\delta(g_{Z'u}^{\text{F}}/g_{Z'u}^{\text{B}})}{g_{Z'u}^{\text{F}}/g_{Z'u}^{\text{B}}} \simeq 0.14.$$

Combining with previous result from  $A_{\text{LR}}$ ,  $\frac{\delta(g_{Z'ee}^{\text{L}}/g_{Z'ee}^{\text{R}})}{g_{Z'ee}^{\text{L}}/g_{Z'ee}^{\text{R}}} \simeq 0.01$  :

$$\Rightarrow \frac{\delta(g_{Z'\mu\mu}^{\text{F}}/g_{Z'\mu\mu}^{\text{B}})}{g_{Z'\mu\mu}^{\text{F}}/g_{Z'\mu\mu}^{\text{B}}} \simeq 0.01.$$

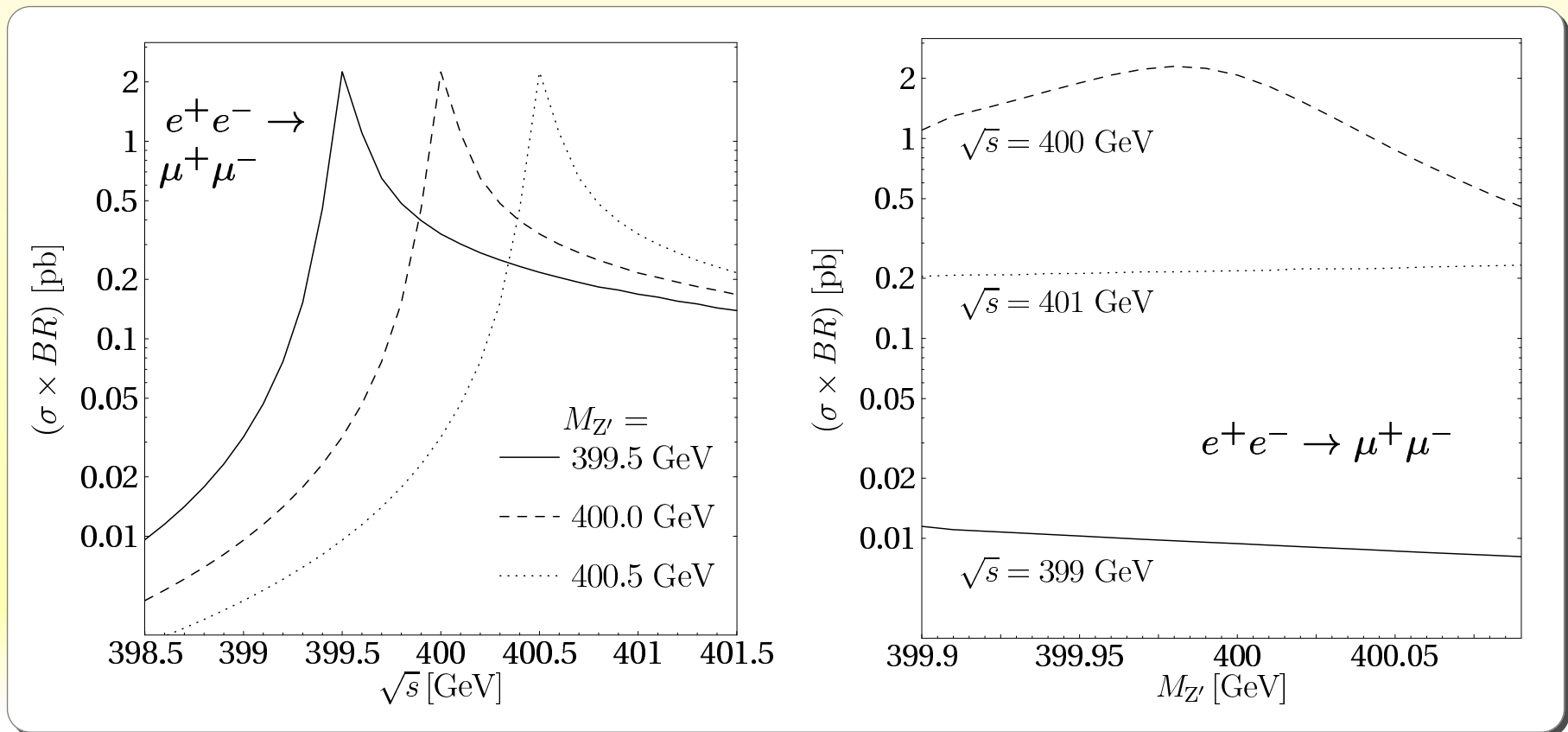
# Mass measurement

Precise determination of mass from scan around resonance region

Resonance line-shape distorted due to beam energy spread

→ Initial-state radiation calculable to high accuracy

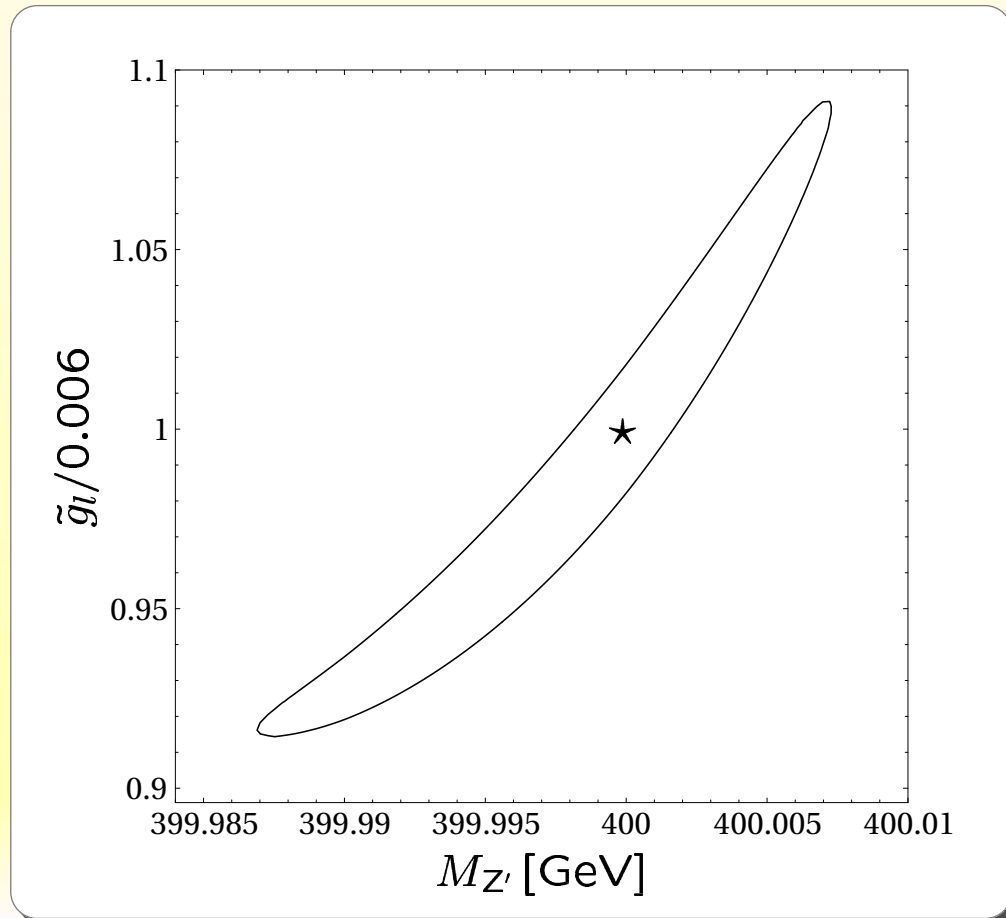
→ Beamstrahlung determined from measuring Bhabha scattering



## Mass measurement from cross-section $e^+e^- \rightarrow \mu^+\mu^-$

Scan around resonance:

$\sqrt{s} = 399, 400, 401$  GeV width  $10 \text{ fb}^{-1}$  each



Beam energy spread causes strong correlation between mass  $M_{Z'}$  and coupling  $\tilde{g}_l$

Fit result:

$$M_{Z'} = 400.0^{+0.007+0.040}_{-0.013-0.040} \text{ GeV}$$

↑

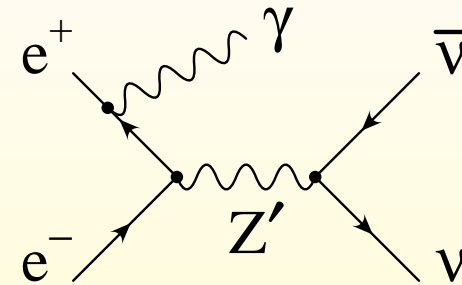
Systematics dominated by uncertainty in beam energy

## Special case: Invisible $Z'$ decays

Invisible decay modes, e.g.  $Z' \rightarrow \nu\bar{\nu}$

Experimentally accessible by using  
hard photon for tagging

$$e^+e^- \rightarrow \gamma\nu\bar{\nu}$$



Carena, de Gouvêa, Freitas, Schmitt '03

$Z'$  peak translates into peak in  $E_\gamma$  spectrum

$$E_\gamma = \sqrt{s}(1 - m_{\nu\bar{\nu}})$$

Search limits in  $(\sigma \times BR)$  are weaker than in visible channels by roughly  
a factor  $\log(s/m_e^2) \approx 25-28$

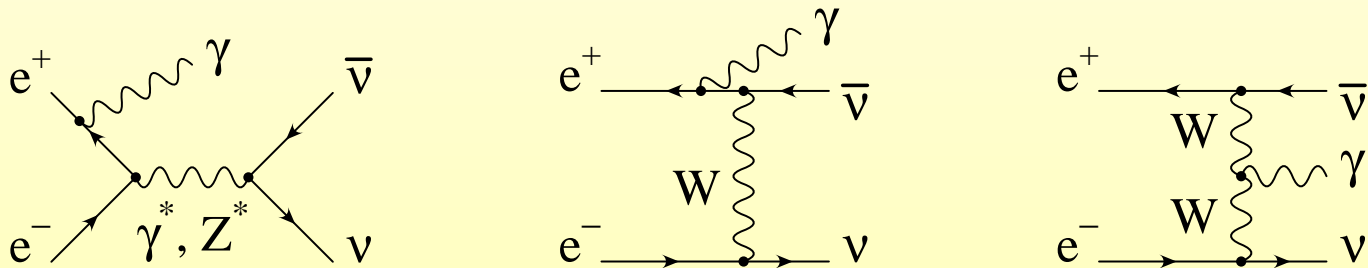
## Determination of absolute branching ratios

Measurement of invisible decay channels allows determination of **absolute** BRs

**Constraint:** Not feasible for very weakly coupled  $Z'$  bosons due to photon phase-space

→ Cannot exploit resonance enhancement

**Background:** SM contributions to  $e^+e^- \rightarrow \gamma\nu\bar{\nu}$



**Signal identification:** Peak in  $E_\gamma$  spectrum over background

**Photon energy resolution:**

$$E_\gamma \text{ resolution from em. calo.: } \frac{\Delta E_\gamma}{E_\gamma} \approx \frac{10\%}{\sqrt{E_\gamma/\text{GeV}}} \oplus 1\%$$

TESLA TDR '01

Example:  $Z_{B-L}$  boson with  $M_{Z'} = 400$  GeV and  $\tilde{g}_l = g_{Z' l} = 0.1$

Use  $100 \text{ fb}^{-1}$  at  $\sqrt{s} = 420$  GeV

$N_{\text{sig}} = 5700$ ,  $N_{\text{bkgd}} = 20000$

$\rightarrow \delta\sigma_{\nu\bar{\nu}\gamma}/\sigma_{\nu\bar{\nu}\gamma} = 2.8\%$  (stat.)

Subtraction of background and deconvolution of photon spectrum:

$\delta(\sigma \times BR_{\nu\bar{\nu}})/(\sigma \times BR_{\nu\bar{\nu}}) = 3.1\%$

Combination with visible modes:

Visible cross-sections from peak measurements

$\rightarrow$  negligible error

$\Rightarrow$

Channel	BR measurement	rel. error
$l^+l^-$	$0.469 \pm 0.0035$	0.8%
$q\bar{q}, q \neq t$	$0.261 \pm 0.002$	0.8%
$t\bar{t}$	$0.035 \pm 0.0003$	0.8%
$\nu\bar{\nu}$	$0.235 \pm 0.0055$	2.5%



## Summary

- Possibility of new vector bosons with mass  $M_{Z'} \sim 1$  TeV is one standard scenario of physics beyond the Standard Model
- Next generation of colliders can study new neutral vector bosons with masses up to  $M_{Z'} \approx 10$  TeV or couplings down to  $g_{Z'} \sim 10^{-3}$ 
  - Complementarity between LHC and linear collider
- Linear collider provides unique opportunities for very weakly coupled  $Z'$  bosons ( $M_{Z'} < \sqrt{s}$ )
- Precise determination of  $Z'$  parameters possible for  $M_{Z'} < \sqrt{s}$ 
  - can be improved by tuning accelerator on  $Z'$  resonance and using polarized beams

## Backup slides

## Projected limits for Tevatron Run II

Extrapolate current limits  
to end of Run II

- Assume integrated luminosity of  $4 \text{ fb}^{-1}$
- Scale signal rates
- Background very low
- Combine experiments

