

# Top mass determination from the $J/\Psi$ +lepton invariant mass in top decay at the LHC and ILC

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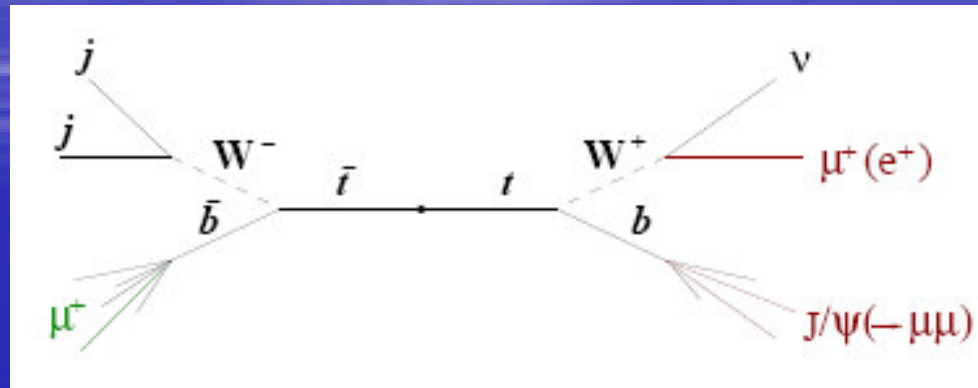
## Outline

- Top mass measurement at the LHC
- Method and numbers
- Theoretical predictions
- The ILC case and LHC/ILC synergy
- Comparison to other extraction methods
- Prospects and conclusions

# Top mass measurement at the LHC

Jet measurements are hard at the LHC; check out the lepton signal

A. Kharchilava, hep-ph/9912320:

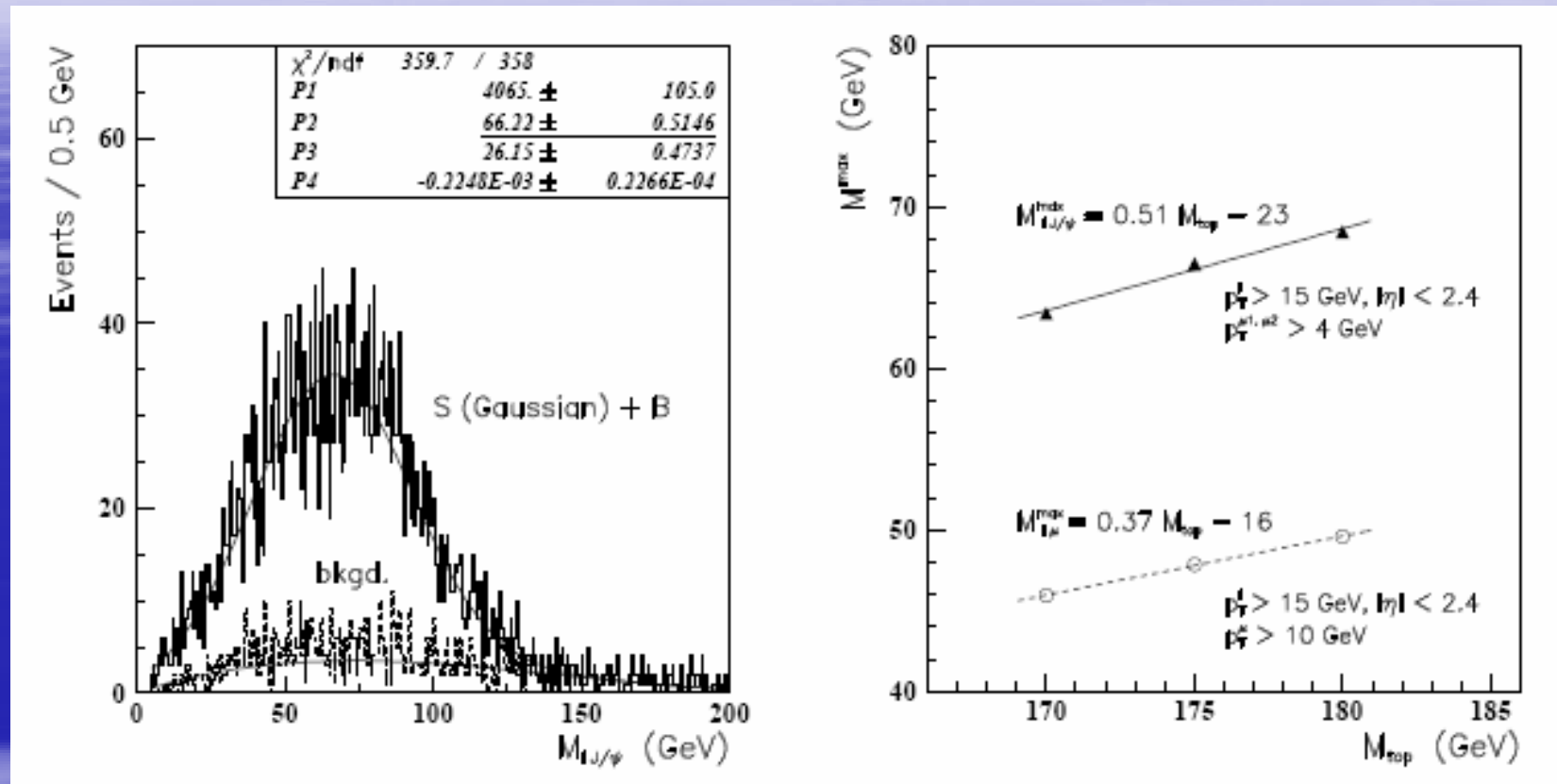


**Method:** study the invariant mass distribution of  $M_{J/\psi-\ell}$  in top decay

- Experimentally very clean signal
- Low branching ratio  $\sim 10^{-5}$ , but
- Compensated by large top production rates
- Expected 1000 events/year at LHC
- Accuracy  $\leq 1$  GeV for 4 years of running.

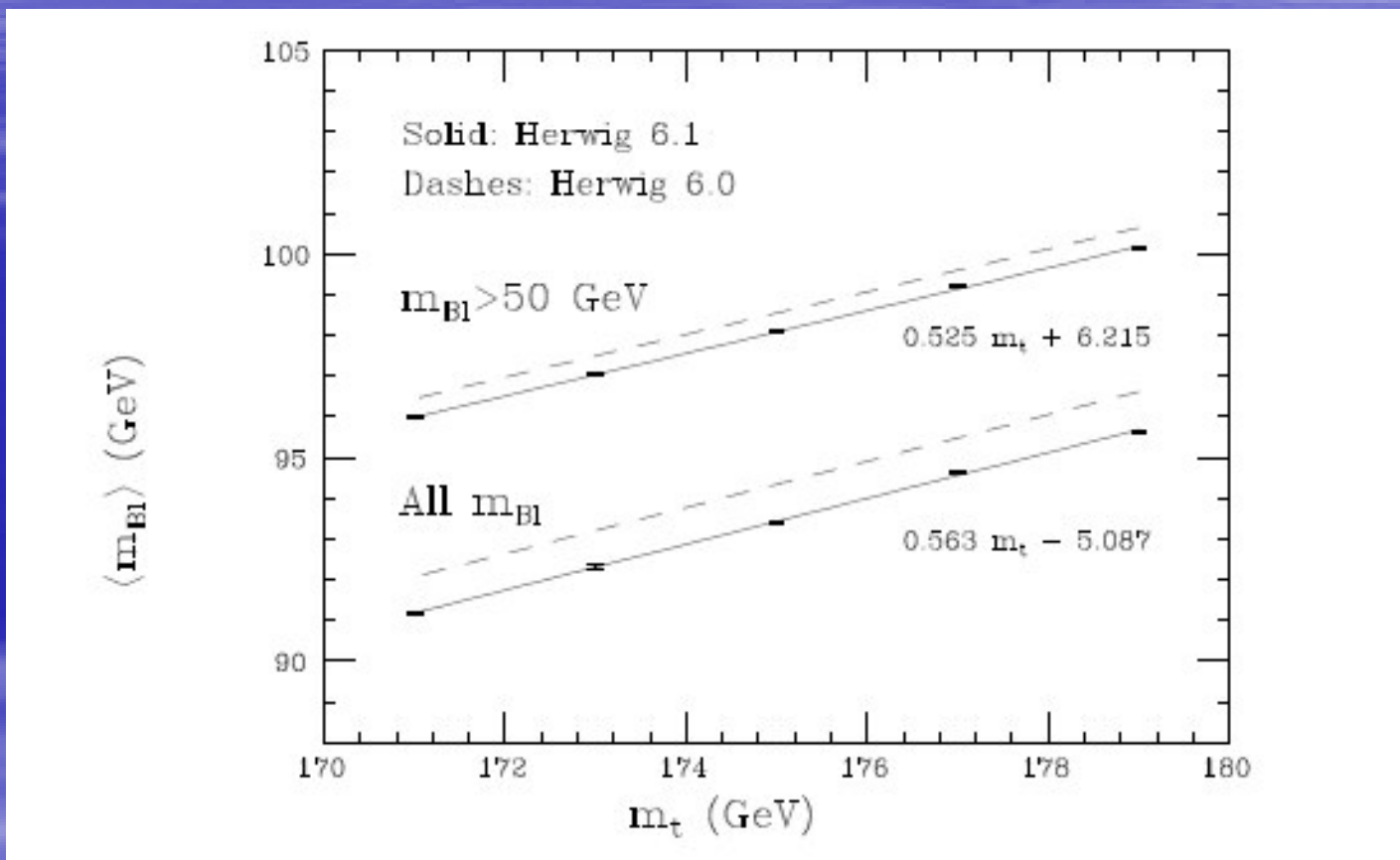
# Top mass determination method

A. Kharchilava, hep-ph/9912320



- The top mass is correlated with the position of the peak of  $M_{J/\psi-\ell}$
- Above studies obtained from PYTHIA 5.7 or HERWIG 5.9

- Further studies with MC's:  
Corcella, Mangano and Seymour: hep-ph/0004179
- Based on HERWIG 6.0 and 6.1
- Only the B production was studied there; not the  $B \rightarrow J/\Psi$  transition



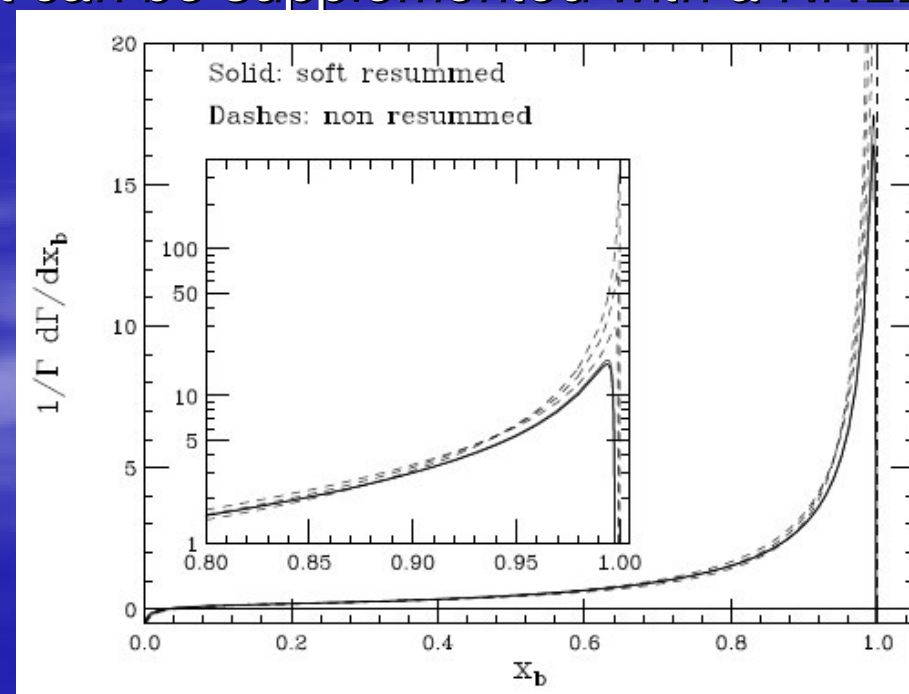
- Large difference (1.0~1.5 GeV) in  $M_{top}$  between the two versions.
- A significant fraction (~0.5 GeV) of that difference comes from the hadronization.

Clearly, because of the intrinsic uncertainties in these studies, they must be supported by a dedicated calculation.

What are the prospects for such a calculation and what are its expected uncertainties?

- An NLO + NLL calculation is easy to do (in progress). It is available for a related observable: b-energy spectrum in top decay.
- One can perform resummation of large logs with much better control and accuracy compared to any other approach.
- An NNLO level result is also feasible. It can be supplemented with a NNLL resummation (already possible).

Uncertainties at perturbative level are well under control!



# How about the non-perturbative effects?

## From the $b \rightarrow B$ transition:

This is presently extracted from LEP data. Extractions of both the whole non-perturbative function and of some of its moments is possible!

DELPHI Collaboration

	$\langle x \rangle$	$\langle x^2 \rangle$	$\langle x^3 \rangle$	$\langle x^4 \rangle$
$e^+e^-$ data $\sigma_N^B$	$0.7153 \pm 0.0052$	$0.5401 \pm 0.0064$	$0.4236 \pm 0.0065$	$0.3406 \pm 0.0064$

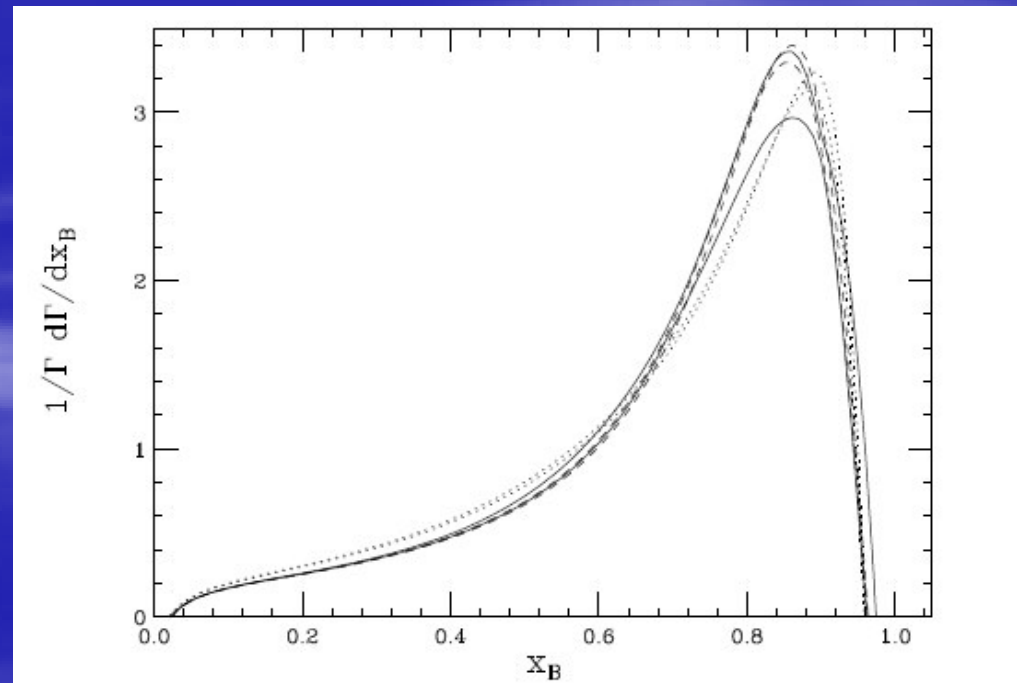
Cacciari, Corcella and A.M. hep-ph/0209204

$t$ -decay $\Gamma_N^B$ [A]	0.7231	0.5555	0.4440	0.3637
$t$ -decay $\Gamma_N^B$ [B]	0.7228	0.5553	0.4435	0.3633

Uncertainties are at:

$\pm 0.5\% \sim 1\%$  for  $n=1$

$\pm 7\%$  for  $n=10$



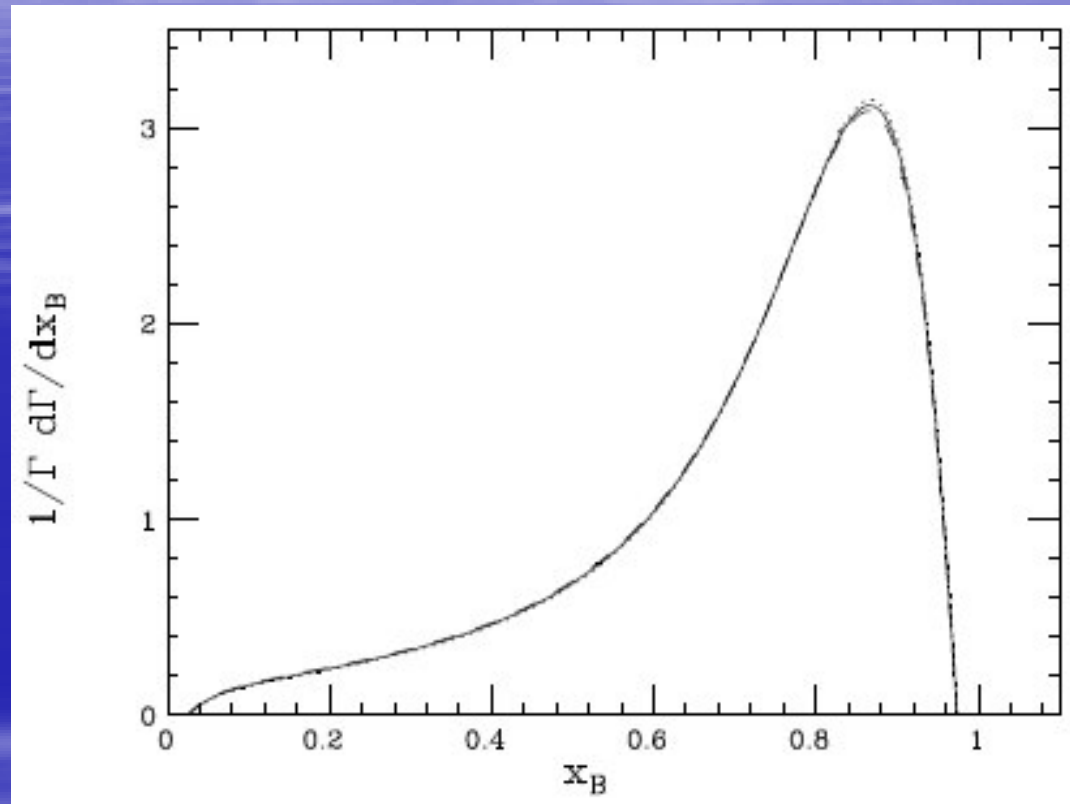
# How about the non-perturbative effects?

From the  $B \rightarrow J/\Psi$  transition:

- Can be modeled from data on B-decays from B-factories.
- Has been applied for the study of the transverse momentum distribution of B-mesons at the Tevatron (Cacciari et al. hep-ph/0312132).
- Their prediction was compared with the result from MC@NLO.
- The conclusion was that improvement in the modeling of the  $B \rightarrow J/\Psi$  transition in the MC is needed.

## A related observable: B-energy in top decay.

- This observable is also sensitive to the value of the top quark.



- The normalized energy distribution for three values of  $M_{\text{top}}$ :
- $M_{\text{top}} = 170, 175, 180$  GeV
- The correlation  $\langle E_B \rangle \approx \text{const. } M_{\text{top}}$  is similar to the  $J/\Psi + \text{lepton}$  case.
- The experimental prospects on that variable have not been detailed.



# The ILC case

One can also perform the measurement of  $M_{J/\psi-\ell}$  at ILC!

- Ignoring top production and decay correlations (excellent approx.):

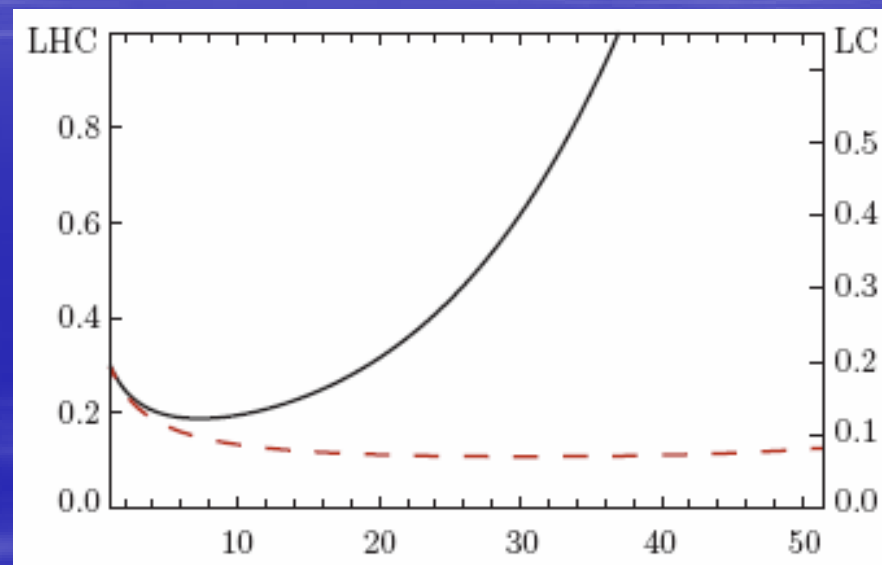
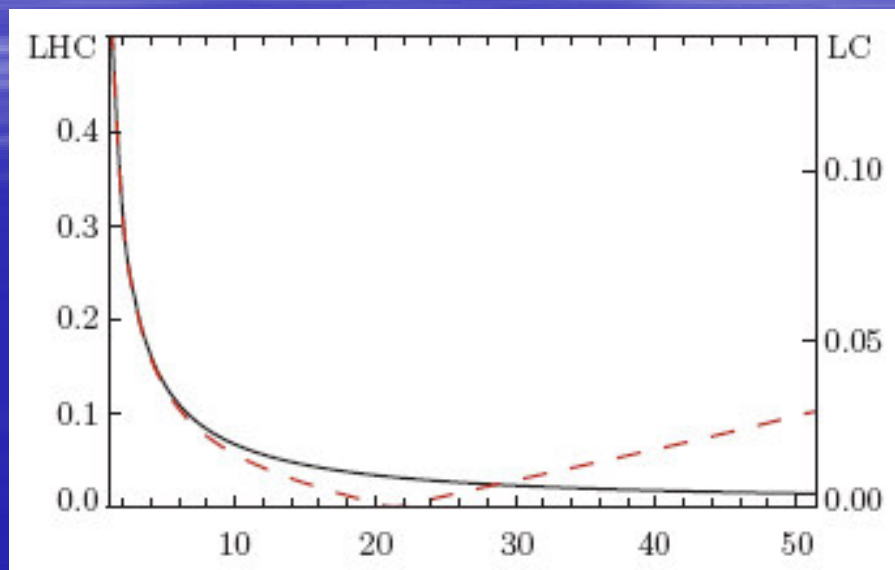
$$\frac{1}{\sigma} \frac{d\sigma}{dM_{J/\Psi\ell}} = \frac{1}{\Gamma} \frac{d\Gamma}{dM_{J/\Psi\ell}}$$

- The accuracy for the same measurement is expected to be comparable at the one for LHC.
- **However**, an extraction permitting much better accuracy was claimed by: M. Nekrasov, hep-ph/0412219.
- His method relies on extraction of  $M_{\text{top}}$  from higher moments ( $n \approx 15$ ) of the invariant mass distribution.
- There (at the level of b-quark production) the following uncertainties were found:  $\delta M_{\text{top}} \leq 500 \text{ MeV}$  (LHC) and  $\delta M_{\text{top}} \leq 200 \text{ MeV}$  (LC).

Note that in the above error analysis, the results from the previous LHC analysis are used (i.e. the same uncertainty from b-fragmentation).

- Systematic errors (in GeV) for LHC and LC as a function of the moments at the level of b-quark production.

Nekrasov, hep-ph/0412219.



- However:** recall the increasing uncertainty of the non-perturbative transition with increasing moments that was shown previously.
- Note that improved extraction of the non-perturbative fragmentation function with NNLO + NNLL accuracy may decrease the errors at higher moments.

# The LHC/ILC synergy

- Concurrent running of both machines will permit simultaneous analysis of the two measurements.
- That may lead to improving of the experimental techniques used in these experiments or of the method itself.
- However, if ILC gets its GigaZ regime, then the improvement can be very different:
- From GigaZ 2-3 times improvement in the b-measurements is expected.
- If that is translated into similar precision in the extraction of the b->B non-perturbative fragmentation function, then the method described here can produce results with  $\delta M_{\text{top}} \leq 300 \text{ MeV}$  without the use of higher moments!
- Clearly, a concurrent running will permit the LHC data to be reanalyzed while LHC is still running.

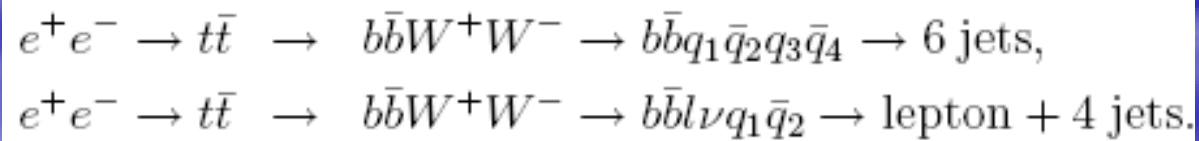
# Comparison to other methods for extraction of the top mass

## Case A) LHC alone:

- Then this is the the best method for determination of  $M_{\text{top}}$  with error of  $\delta M_{\text{top}} \leq 1 \text{ GeV}$ . Note that the systematics (for the LHC study) are (+600-800) MeV. However  $\sim 2/3$  of that is from the b-fragmentation!

## Case B) LHC + ILC + GigaZ:

- This method can produce (theory)  $\delta M_{\text{top}} \leq 300 \text{ MeV}$  or even less.
- Exactly the same if not better than the results from a direct reconstruction of the top-decay products: Chekanov, hep-ph/0206264.



- With results of  $\delta M_{\text{top}} \leq (340-425) \text{ MeV}$  or  $\delta M_{\text{top}} \leq 250 \text{ MeV}$  resp.
- Top threshold scan is expected to give  $\delta M_{\text{top}} \leq 100 \text{ MeV}$ .

# Conclusions

- I have reviewed a method for obtaining  $M_{\text{top}}$ , that is based on a study of the invariant mass of the decay products (all leptons) of the top quark.
- This method has the best precision for LHC with  $\delta M_{\text{top}} \leq 1 \text{ GeV}$ .
- The largest ( $\sim 2/3$ ) systematic error comes from b-fragmentation.
- A concurrent running of LHC/ILC can lead to non-trivial “interference”.
- A GigaZ regime can reduce the b-fragmentation uncertainty 2-3 times.
- **Then:** the expected uncertainty is around  $\delta M_{\text{top}} \leq 300 \text{ MeV}$ .  
This method will be competitive (or better) than the methods based on the reconstruction of the final state of the decaying top pair, and close to the top-threshold scanning method.
- **This is a method with potential that has to be explored in detail!**